



Handwritten Notes  
On  
Ray Optics



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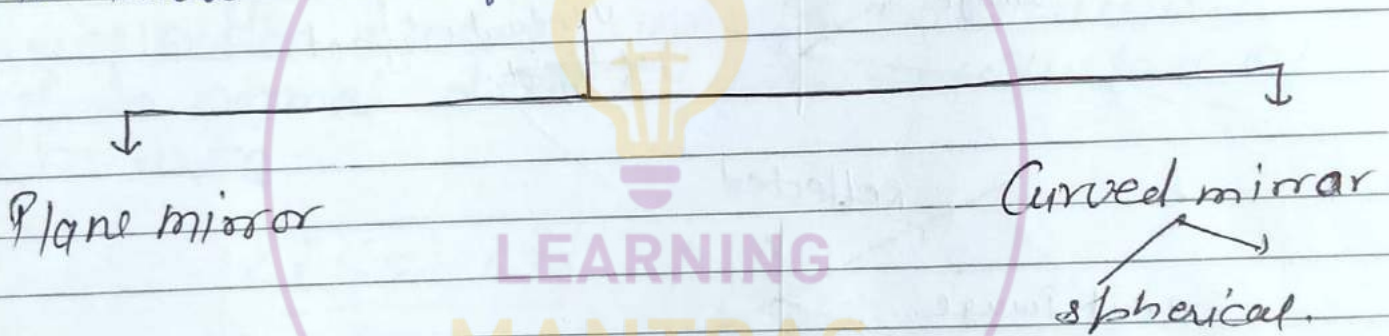
# Ray optics

\* Some important definition:

## Reflection:

Bouncing back of light in same medium is known as reflection.

(2) highly polished surface used for reflection is known as reflector or mirror



## \* Ray's:

source to  $\infty$  parallel,

\* One end fixed and other not terminating end is known as Ray

\* Collection of ray is known as beam

## \* Object:

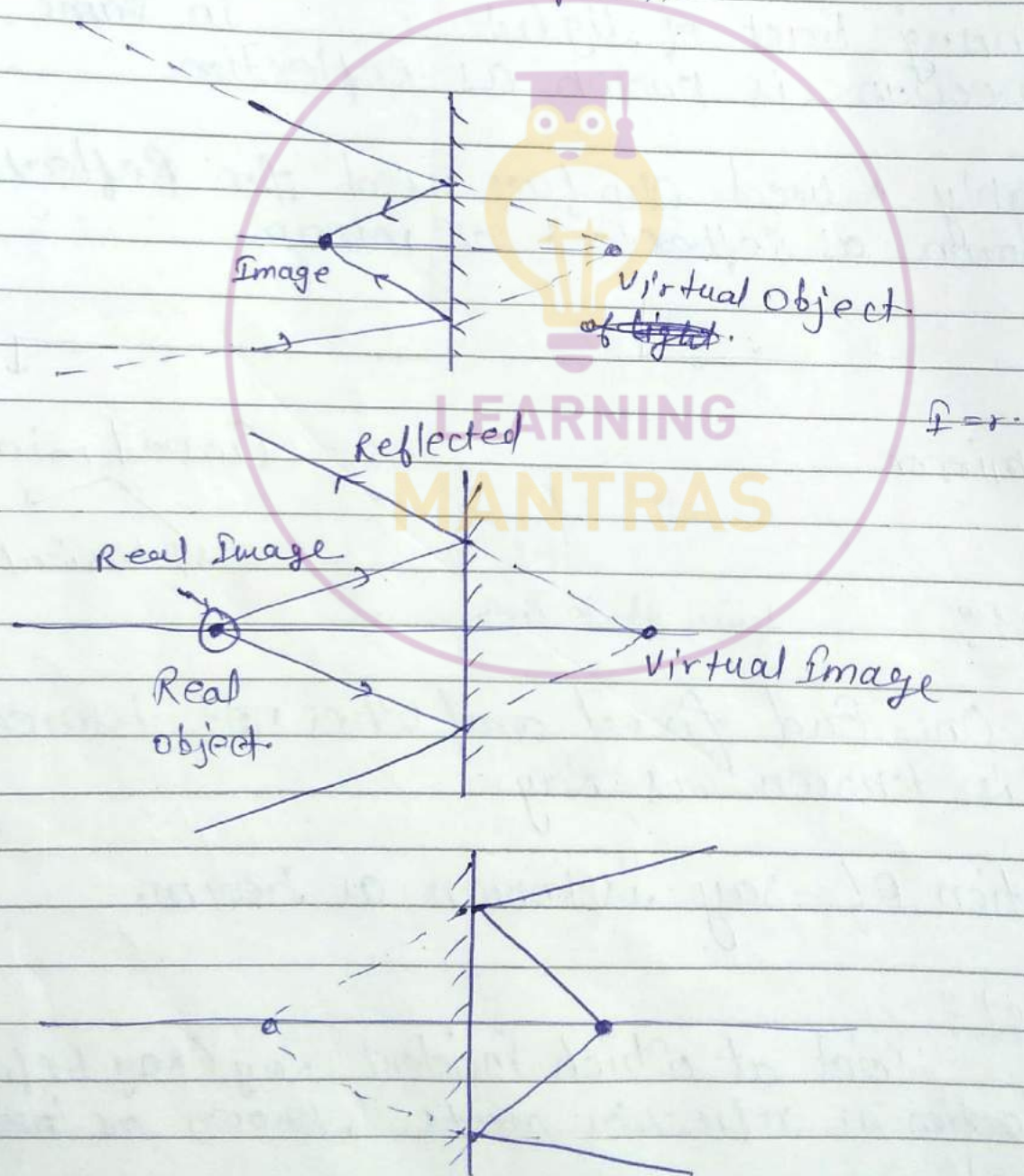
Point at which incident Ray (Ray before reflection) or reflection meets is known as ~~incident~~ Object.

Object is classified into two type

① Real object!

Incident Ray actually meet this Point

② Virtual object! Incident Ray appears to meet this point



\* Image: Point at which Reflected or Refracted Ray meet is known as Image.

\* Law of Reflection:

Law 1: Incident ray, Normal & Reflected ray, all three lies in the same Plane.

$$\hat{i} \cdot [\hat{n} \times \hat{r}] = 0$$

Law 2:

Angle of Incidence is equal to angle of reflection where angle is measured from normal drawn from the surface of mirror.

$$\angle i = \angle r$$

$$\hat{r} = \hat{i} - 2(\hat{i} \cdot \hat{n})\hat{n}$$

\* Plane mirror:

\* Plane mirror forms virtual Image of real object & real Image of virtual object.

\*

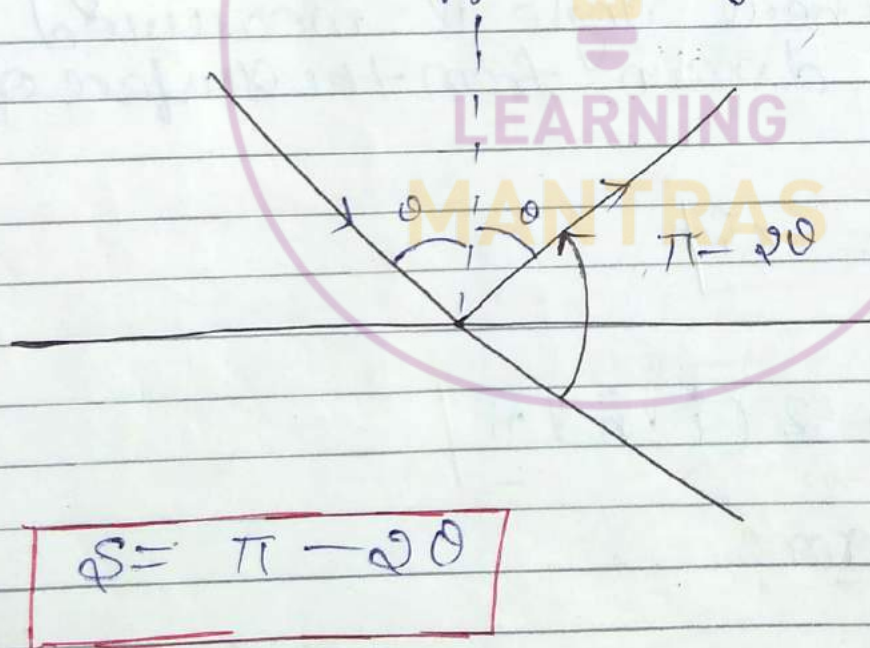
\* Plane mirror performs lateral inversion  
(Left hand coordinate system into right  
hand coordinate system).

\* To find Time of Analog clock in mirror  
Subtract the given time with

11:59:60

\* Distance of Image from the Plane mirror is  
same as that of distance of object from  
it.

\* Deviation suffered by a ray:-

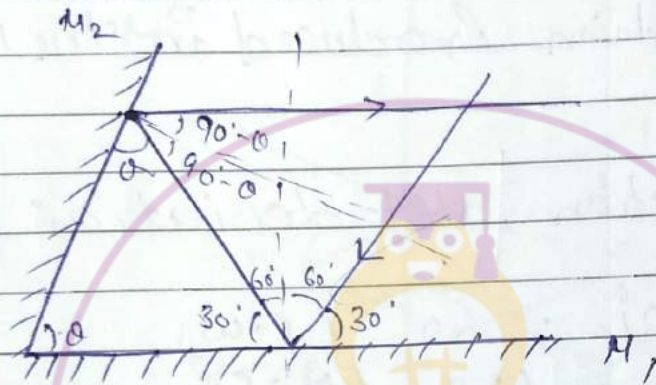


$$\delta = \pi - 2i$$

\* Image formed in plane mirror is erect  
if object is placed Principal axis

\* We trace its path or image formed on object itself mean  $i = 0$

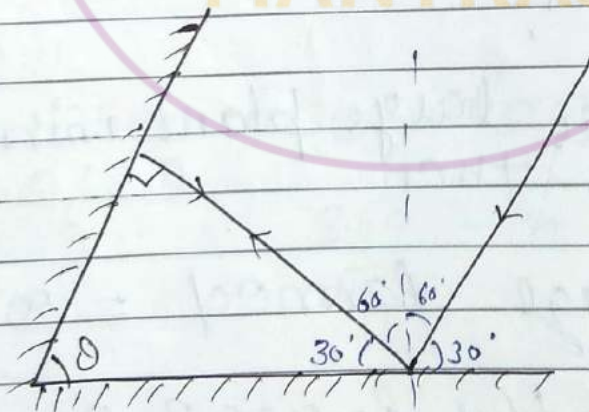
Q. what should be the angle b/w two mirror if ray passes parallel to mirror 1 after 2nd reflection.



$$2\theta + 30 = 180$$

$$\theta = 75$$

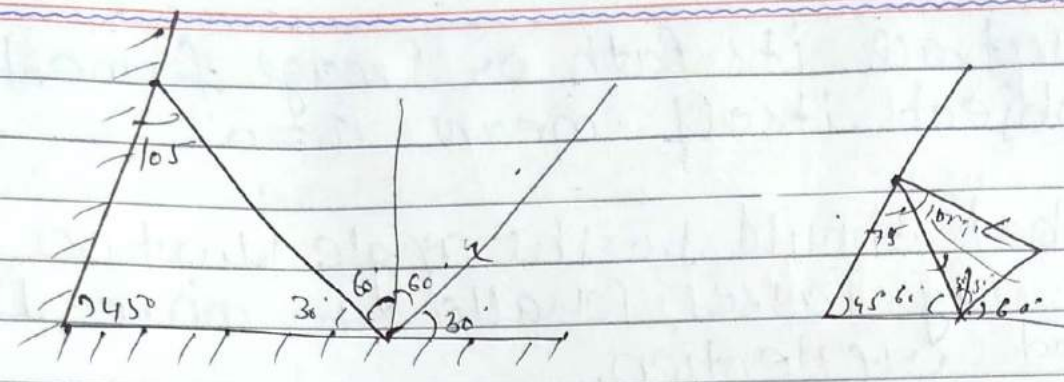
Ans:



Find the angle b/w two mirror if ray retrace its path after 2nd reflection.

$$\theta = 60$$

Q.



find net deviation produced in the incident ray.

After 3 reflection, net deviation

Ans

$$s_1 = 180 - 2i = 60^\circ \text{ (c.w)}$$

$$s_2 = 180 - 2i = 180^\circ \text{ (A.c)}$$

$$s_3 = 180 - 2i = 120^\circ \text{ (A.c)}$$

Net deviation  $210^\circ$  (A.c)

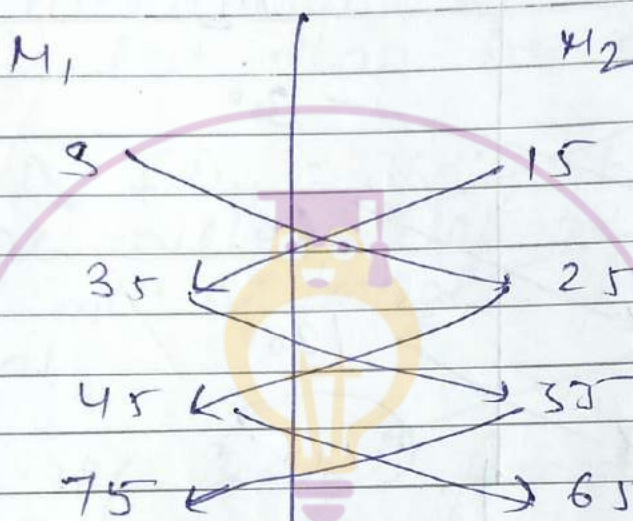
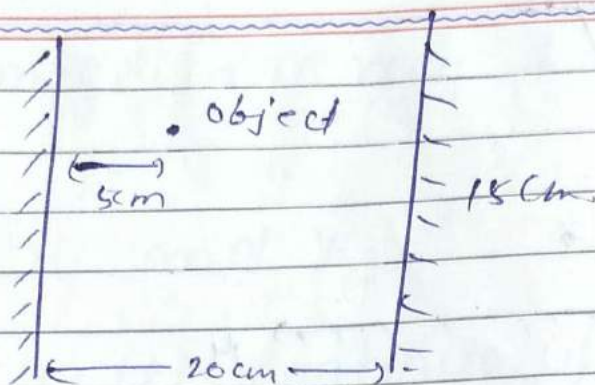
\* No. of Images:

Case: If three large plane mirror are placed " , then

No. of Image formed =  $\infty$

Q. find the dist. b/w Image 2 of mirror 1 & 3 image of mirror 2.

17/11

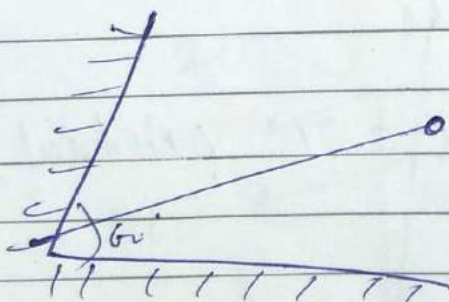


$$35 + 55 + 20 = 110 \text{ cm}$$

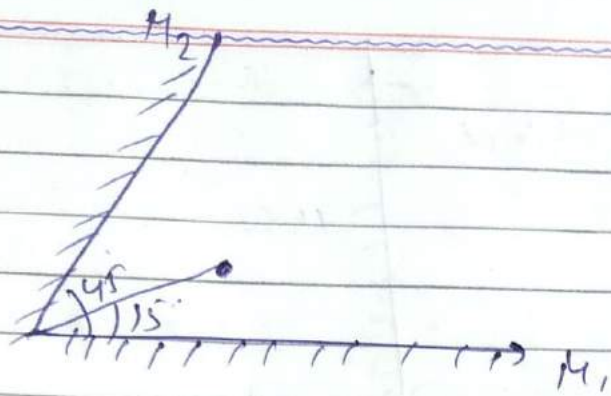
Case:  $\theta \neq 90^\circ$

When two mirrors are at an angle of  $\theta$

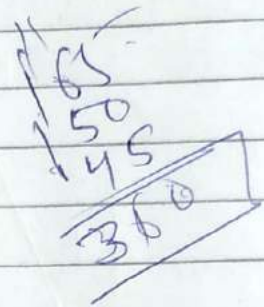
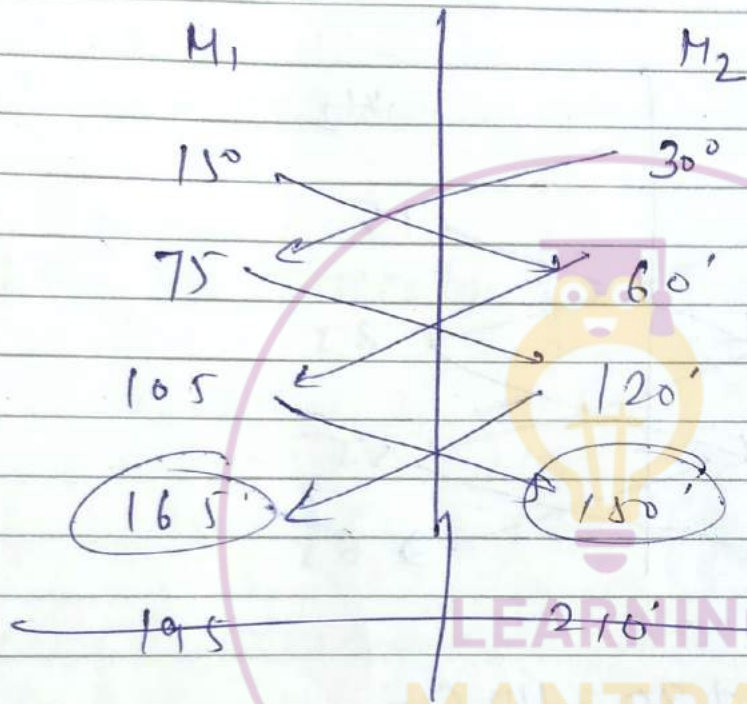
$$\frac{360}{\theta} = n$$







$$\frac{360}{45}$$



$$\left( \frac{180}{3} \right) \text{ or } \left( \frac{180}{45} \right)$$

$$\text{If } \theta_1 + \theta_2 + \theta_{M1} = 360$$

then overlapped image

$$\text{Here } 165 + 180 + 45 = 360$$

So, no. of Images = 7 (Actual)

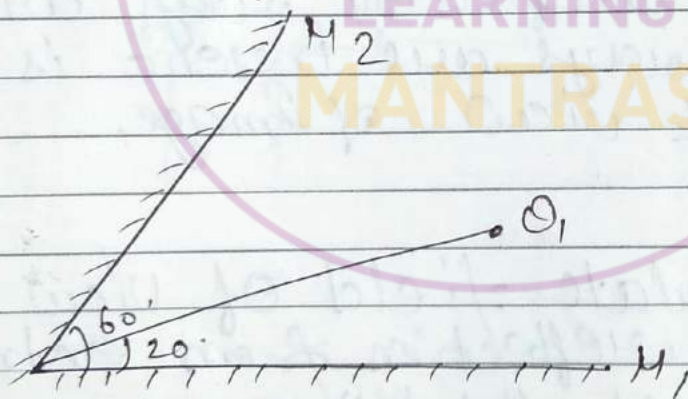
\* Angle of Image in mirror  $\neq \theta_1$

" " " " " 2 =  $\theta_2$   
 " b/w  $M_1$  and  $M_2$  =  $\theta_M$

\* This process will continue upto the instant when some of the angle  $\theta_1$  and  $\theta_2$  is less than or equal to  $180^\circ$

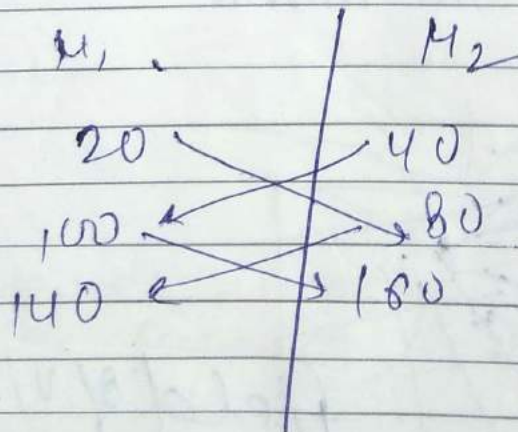
\* If  $\theta_1 + \theta_2 + \theta_M = 360^\circ$ , then two of the image will overlap on each other therefore no. of images form will be  $n-1$

Q. find no. of image formed in!



$$n = \frac{360}{60} - 1$$

60 (except)



$$\frac{140}{100} = \frac{160}{80} = \frac{360}{360}$$

$$140 + 180 + 60 = 360$$

So,  $n-1$  ~~form~~ Images.

$$6-1 = 5 \text{ Images.}$$

\* Field of view!

\* Field of view for object!

Space in which incident rays are present of object

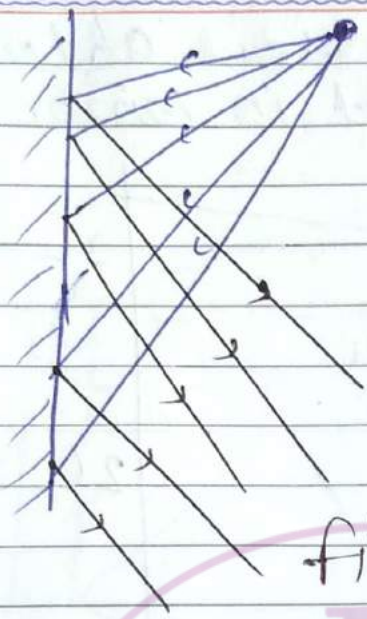
\* Field of view of image!

Space in which reflected rays are present is known as field of view of image.

Note!

To calculate field of view always take reflection from extreme corner of the mirror.

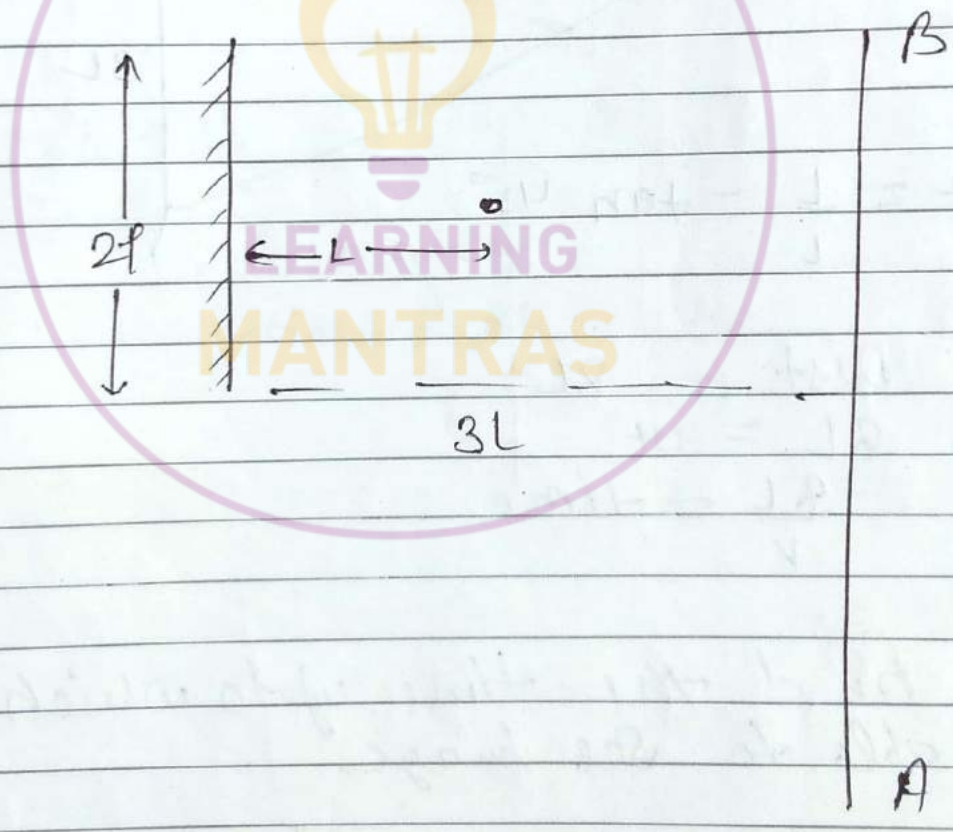




• → can't see the image.

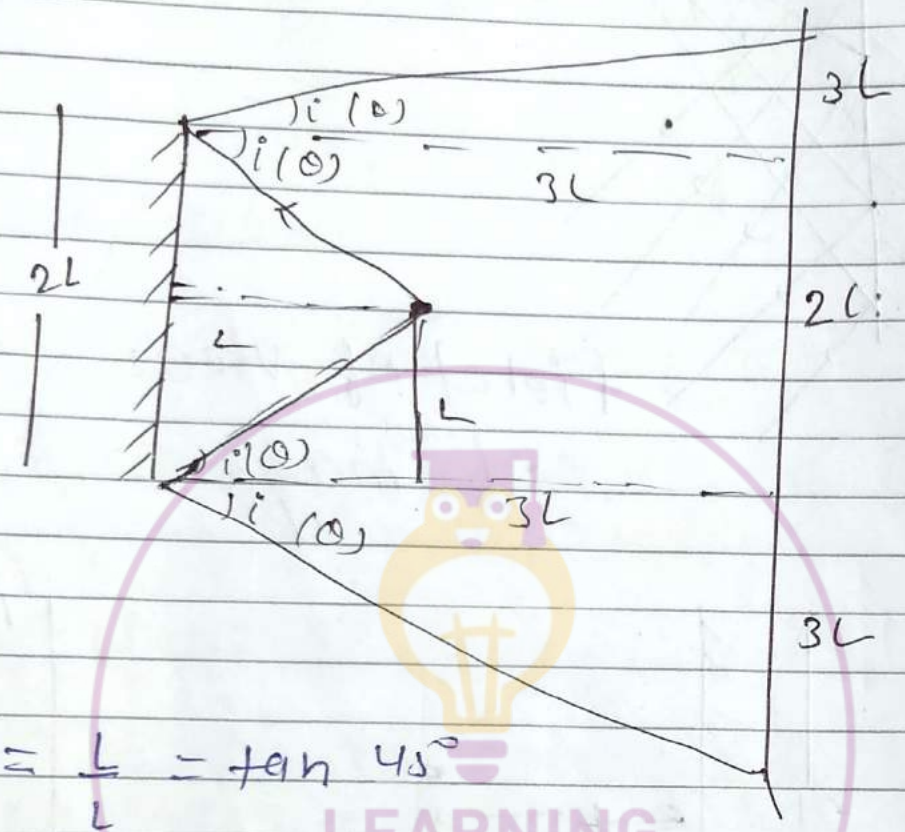
field of view of image

Q.



An observer is moving  $\parallel$  to mirror on line AB with constant velocity  $v$ .

Q. Find time upto which he is able to see image of object in mirror.



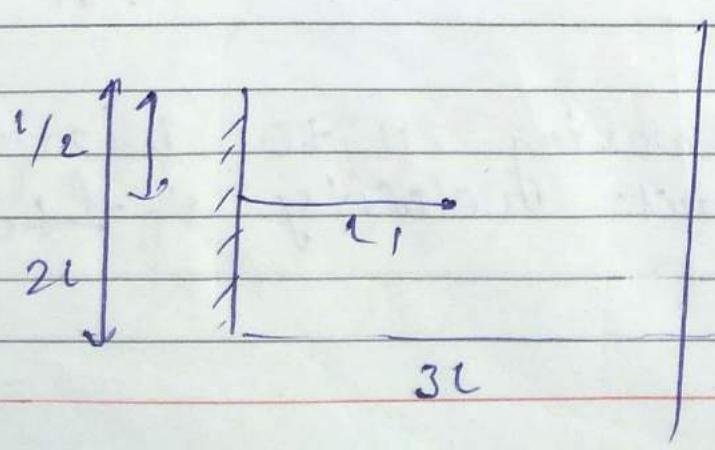
$$\tan \theta = \frac{L}{L} = \tan 45^\circ$$

Dist =  $8L$

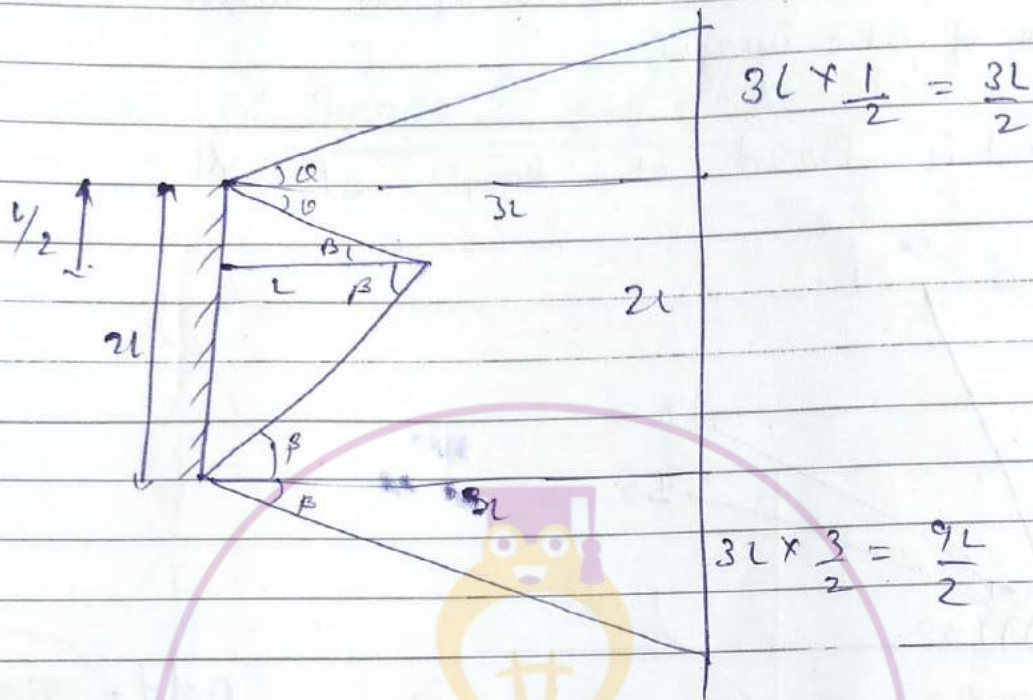
$$8L = vt$$

$$\frac{8L}{v} = \text{time.}$$

Ques. Find the time upto which he is able to see image.



$$\tan \theta = \frac{1}{2}, \quad \tan \beta = \frac{3}{2}$$



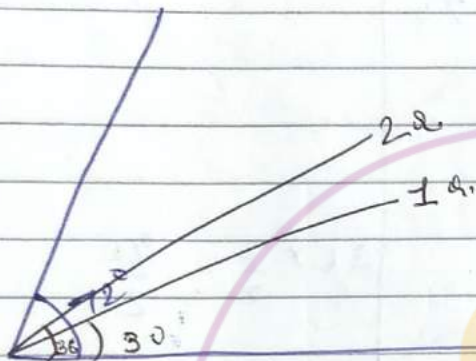
$$\frac{9L}{2} + 2L + \frac{3L}{2}$$

$$\text{Dist} = 8L$$

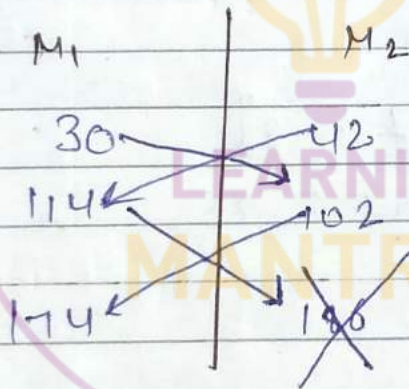
$$\text{Time} = \frac{8L}{v}$$

Q. Angle b/w two mirror is  $72^\circ$  and that object is placed at an angle of  $30^\circ$  from one of the mirror find no. of the image.

2) If object is placed at angle of  $36^\circ$ .



$$\text{Odd} = (n, n-1)$$



(5)

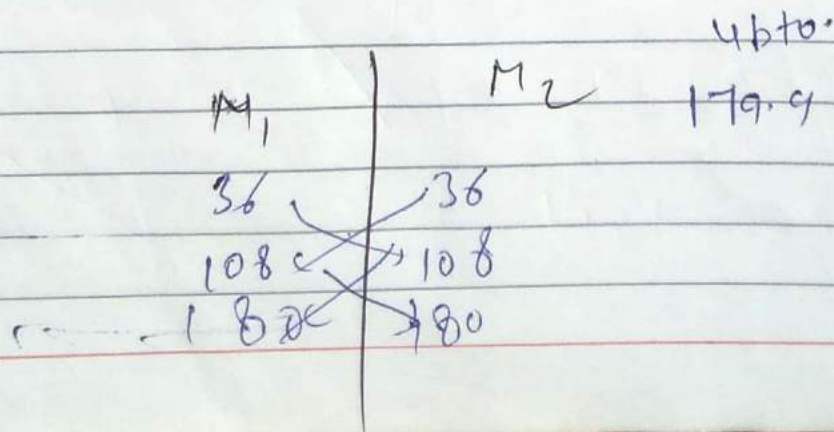
$$\begin{array}{r} 130 \\ 174 \\ \hline 304 \\ 360 \\ \hline 72 \end{array}$$

$$\theta_1 + \theta_2 + \theta_M = 360$$

$$174 + 102 + 72 = 348$$

Overlapping Images = 5

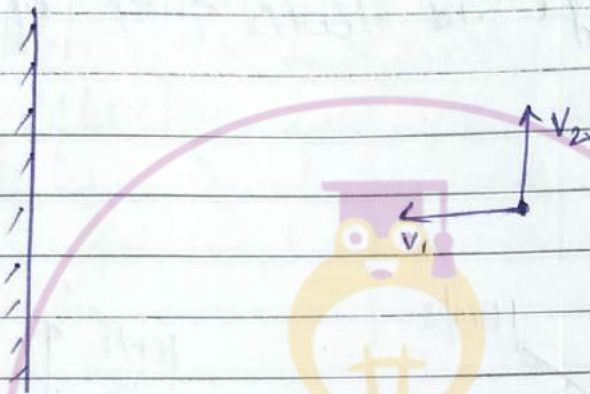
Overlapping



$$108 + 108 + 72 =$$

## \* Velocity of Image in the Plane Mirror:

\*



Case = 1

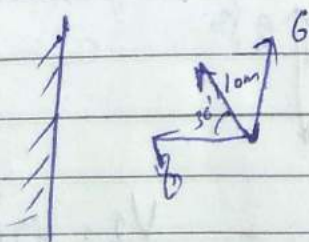
\* When object is moving ~~that~~ ~~is~~  
 → if Velocity of object is Parallel to Plane of mirror  
 Velocity of ~~the~~ image will be same as that of  
 Velocity of object ~~is~~

$$\vec{v}_{O \parallel M} = \vec{v}_{I \parallel M}$$

→ if object moves Perpendicular to the mirror

$$\vec{v}_I \perp M = -v_{obj. \perp M}$$

Ex<sup>e</sup>



$$v_o = -8i + 6j$$

$$v_i = 8i + 6j$$

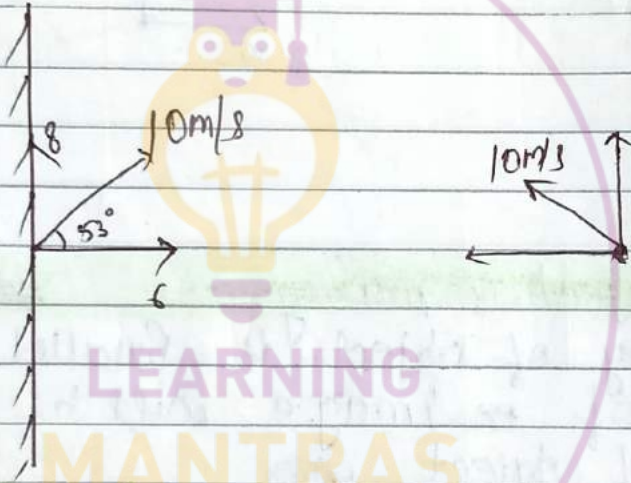


Case: 2 when mirror is moving.

\* When Velocity of mirror is  $\parallel$  to its plane there will be no effect on Velocity of Image

\* When Velocity of mirror is  $\perp$  to its plane Velocity of Image is twice that of Velocity of mirror

Ex:



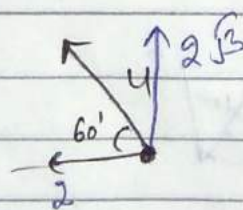
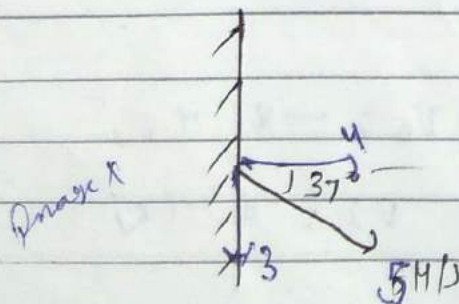
$$\vec{V}_M = 6\hat{i} + 8\hat{j}$$

$$\vec{V}_I = 12\hat{i} + 0\hat{j}$$

$$2\vec{V}_M \perp M = \vec{V}_I \perp M$$

find ~~the~~ Image of ~~object~~ object

a.



$$= \vec{V}_I = 10\hat{i} + 2\sqrt{3}\hat{j}$$

Important

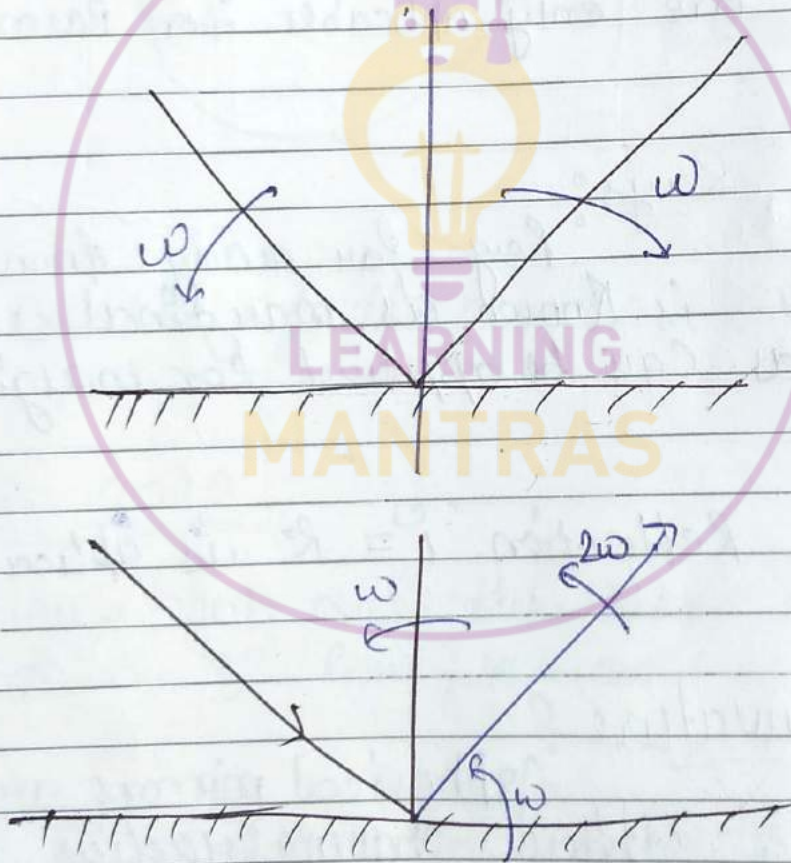
$$+O_2 \rightarrow I_2$$

field of view

## \* Angular Velocity!

If incident ray is rotated by angular velocity  $\omega$  reflected ray will also rotate with same angular velocity with opposite sense.

If mirror is rotated by angular velocity  $\omega$  in then reflected ray will move with angular velocity  $2\omega$  in same direction.



## \* Spherical mirror!

Some Imp. definitions:

### \* Paraxial Rays:

All rays close to principle axis is known as Paraxial Rays

Angle of incidence for Paraxial Rays is Less than  $1-10^\circ$   
All formulas are only applicable for Paraxial rays only.

### \* Marginal Rays:

Rays far away from axis  
\* Principle axis is known as marginal rays  
No formulas can be applied for marginal rays

\* Only law of Reflection  $i = r$  is applicable for it

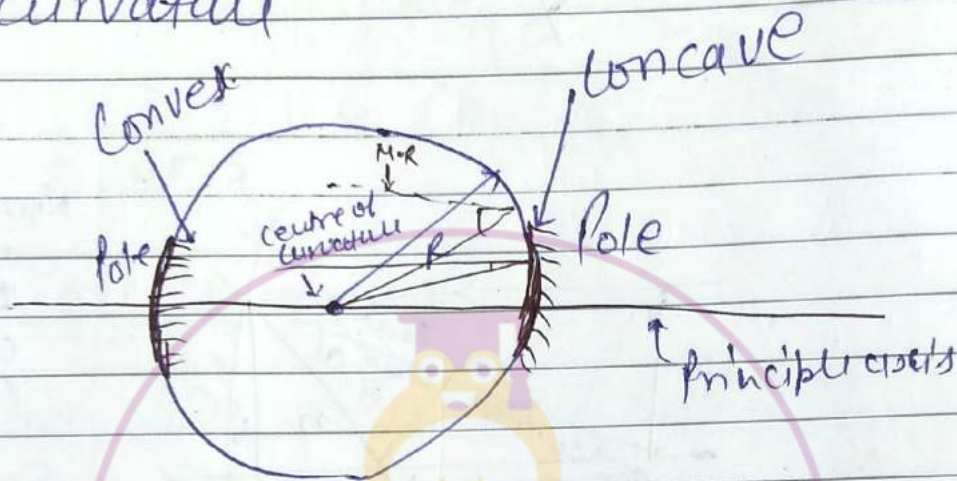
### \* Radius of Curvature:

Spherical mirrors are the part of Big sphere having <sup>same</sup> radius  $R$ .

This radius is known as radius of curvature

## \* Centre of Curvature :

Centre of the sphere from which spherical mirrors is made is known as centre of curvature.



## \* Pole :

Centre of the mirror is known as pole.

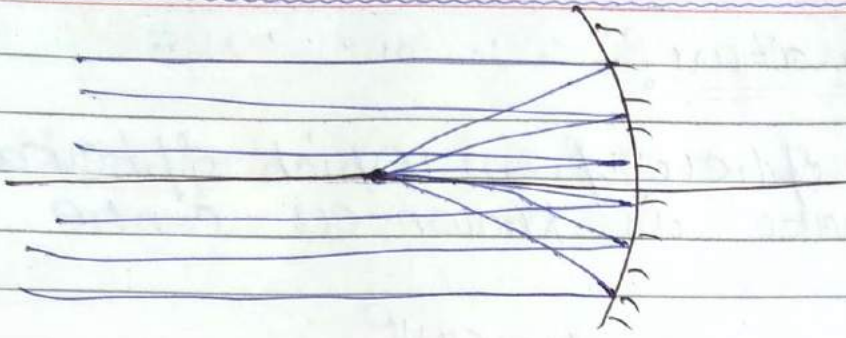
## \* Principle axis :

Line joining pole and the centre of curvature is known as principle axis.

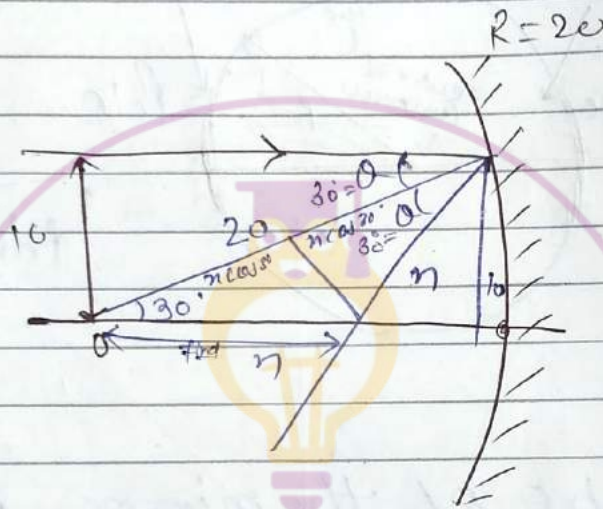
## \* Focus :

Only define for paraxial rays. Point at which all paraxial rays pass through principle axis after reflection is known as focus.

Plane Mirror  
 $\pi/2$   
 Concave



Ques



Normal will also pass through centre of curvature

find the distance where Reflected Ray will cross principle axis after reflection  
 find the dist. from point O.

Ans:  
 For Body

$$2x \cos 30 = 20$$

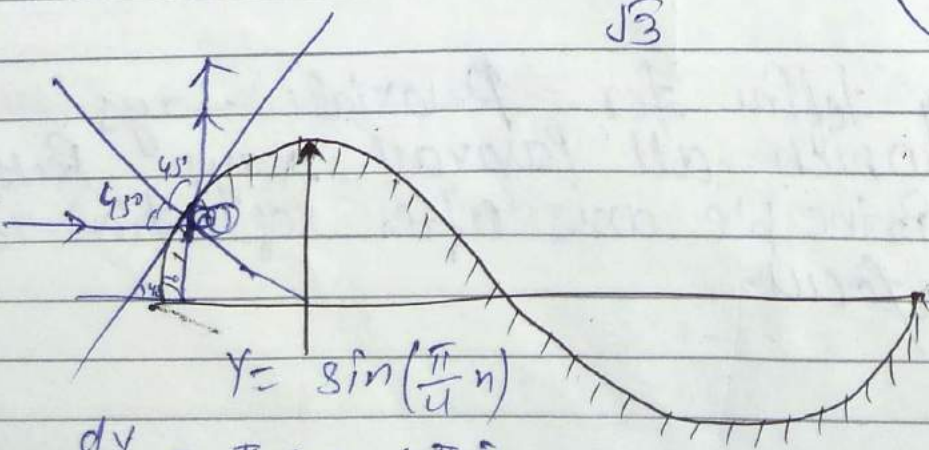
$$n\sqrt{3} = 20$$

$$n = \frac{20}{\sqrt{3}}$$

say  $f = \frac{R}{2}$   
 say  $f = 10 \rightarrow 10 \text{ mm}$

$$f = \frac{R}{2}$$

Q.2



$$y = \sin\left(\frac{\pi}{4} n\right)$$

$$\frac{dy}{dx} = \frac{\pi}{4} \cos\left(\frac{\pi}{4} n\right) = 1$$

Incident ray after reflection become normal.

find the point of incidence.

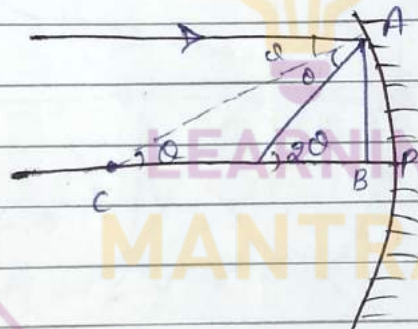
$$\cos\left(\frac{\pi}{4}\right) = \frac{4}{\pi}$$

$$\frac{\pi}{4} = \cos^{-1}\left(\frac{4}{\pi}\right)$$

For  
Spherical Mirrors:

1) Relation b/w focus and Radius of curvature!

Imp.  
for Board



$$\tan \theta = \frac{AB}{BC} \approx \frac{AB}{BP} \quad \text{--- (I)}$$

$$\tan 2\theta = \frac{AB}{BD} \approx \frac{AB}{DP} \quad \text{--- (II)}$$

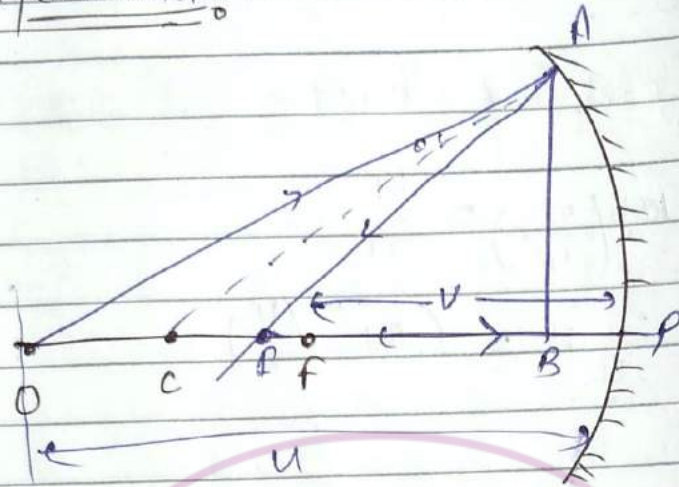
$$\frac{AB}{DP} = \frac{2AB}{CP}$$

$$CP = 2DP$$

$$R = 2f$$

Board

\* Mirror's formula



In  $\triangle ABO$

$$\tan \alpha = \frac{AB}{PO}$$

In  $\triangle A'B'O$

$$\tan r = \frac{A'B'}{PO}$$

In  $\triangle ABC$

$$\tan \beta = \frac{AB}{PC}$$

$$\beta + \theta = r \quad \text{--- (i)}$$

$$\alpha + \theta = \beta \quad \text{--- (ii)}$$

$$\beta - \alpha = r - \beta$$

$$2\beta = r + \alpha$$

$$2 \left[ \frac{AB}{R} \right] = \frac{AB}{u} + \frac{AB}{v}$$

$$\boxed{\frac{1}{f} = \frac{1}{u} + \frac{1}{v}} \quad \text{--- Learn}$$

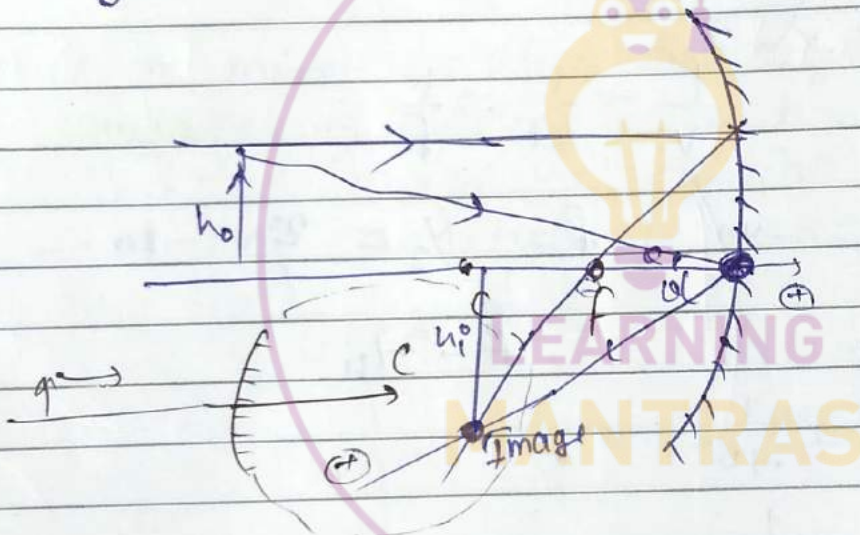
Learn

## \* Sign Conventions

\* All the distances are measured from poles

\* Dist. above Principle axis is taken as Positive.  
and Dist. below Principle axis is taken as -ve.

In the direction of Ray we will take Positive  
and opp. to the dirn of the ray we will take  
Negative.



$$\frac{+h_o}{-u} = \frac{+h}{+v}$$

$$\frac{-u}{u} = \frac{h_i}{h_o}$$

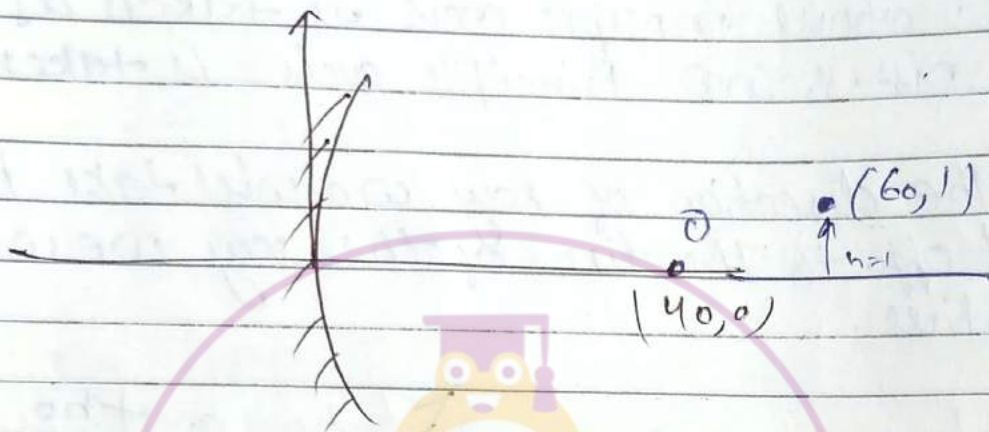
\* Magnification!

$$M = \frac{-v}{u}$$

$$\frac{-v}{u} = \frac{h_i}{h_o}$$



Ques: A Concave mirror is shown in diagram radius of curvature of mirror is 20 cm. find the image of a point  $(40, 0)$  Origin at  $(60, 1)$



$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$v = ? \quad u = -40 \quad f = \frac{R}{2} = \frac{20}{2} = -10$$

$$\frac{1}{v} + \frac{1}{-40} = \frac{1}{-10}$$

$$\frac{1}{v} - \frac{1}{40} = -\frac{1}{10}$$

$$\frac{1}{v} = -\frac{1}{10} + \frac{1}{40}$$

In the above Ques find the position of image of a point  $(60, 1)$

$$h = 1 \quad y = \text{height} = 0.2$$

$$v = ? ; u = -60, f = -10$$

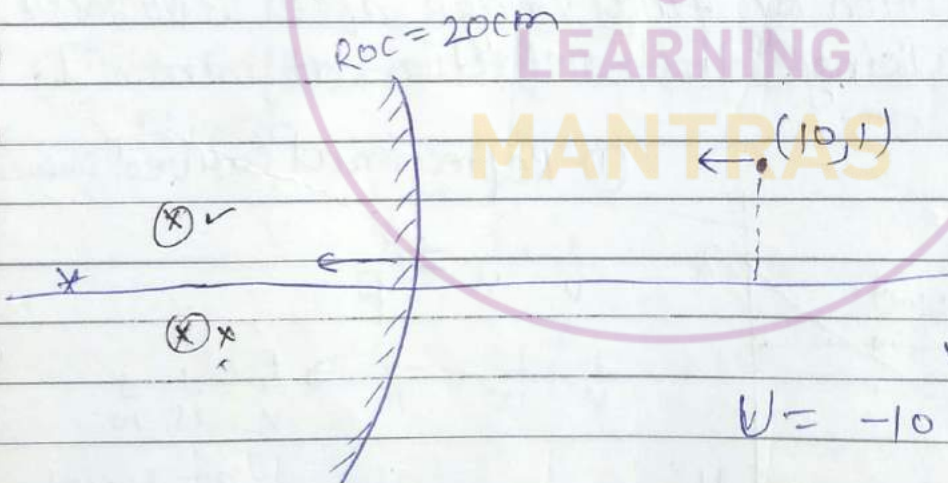
$$v = -12$$

$$h_o = 1 \quad h_i = ?$$

~~$$\frac{h_o}{u} = \frac{h_i}{v}$$~~

$$\frac{h_i}{1} = + \left[ \begin{matrix} +12 \\ -60 \end{matrix} \right]$$

Q. Convex mirror is placed that origin and reflecting surface is facing toward x-axis. Find the image of a point (10, 1) given that radius of curvature is 20cm. Find



$$v = ? \quad R = +20$$

$$u = -10, \quad f = +10$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$= \frac{1}{v} = \frac{1}{10} + \frac{1}{10}$$

$$= \frac{2}{10}$$

$$\frac{h_i}{h_o} = \frac{-v}{u}$$

$$v = +5$$

$$\frac{h_i}{1} = \frac{+(5)}{+10}$$

$$\frac{h_i}{1} = \frac{1}{2}$$

$$h_i = \frac{1}{2}$$

$$v(5, \frac{1}{2})$$

$r = \text{concave}$

Real-Convex mirror  
view

A



## Note

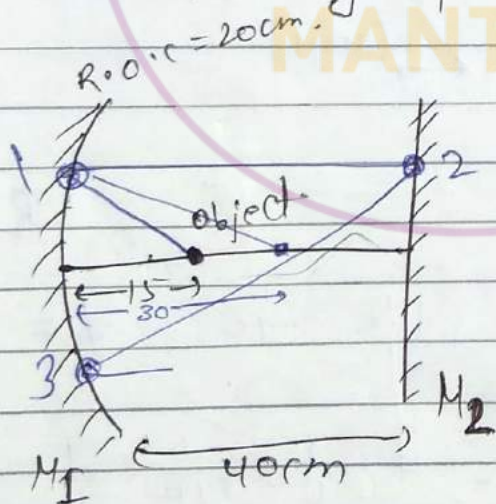
Convex mirror makes Real virtual image of all the real object b/w 0 to F

\* Therefore Convex mirror is used as rear view mirror in the vehicles.

\* These images are diminished (small).

\* Concave mirror is used as looking mirrors and shaving mirror and they produce enlarge image for the object placed b/w 0 and f.

Que: find the position of final image after 3 successive reflection taking first reflection at mirror 1.



① Reflection at curved surface

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{15} = -\frac{1}{10} \Rightarrow \frac{1}{v} = \frac{1}{15} - \frac{1}{10}$$

$$= \frac{2 - 3}{30} = -\frac{1}{30}$$

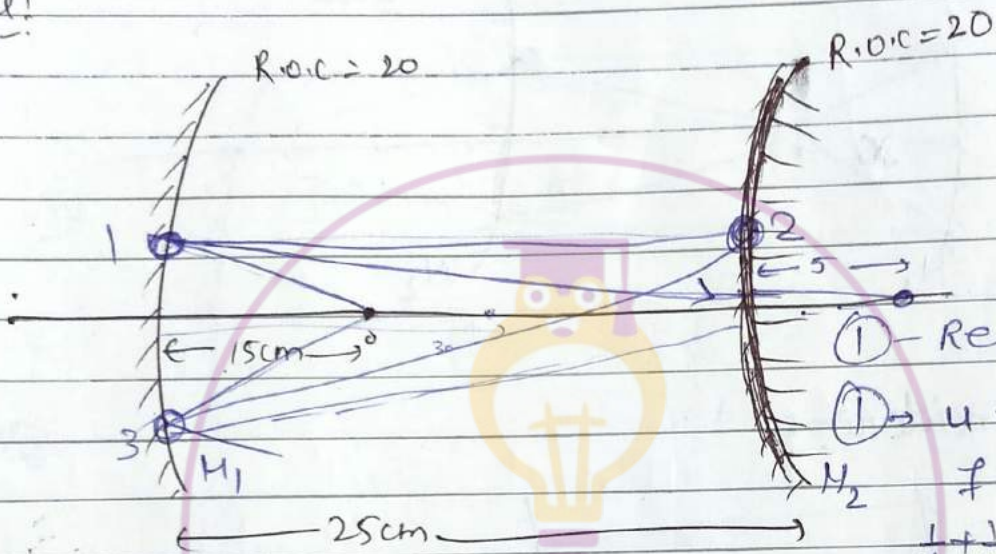
② Reflection surface at Plane  
10 cm behind mirror.

Concave + F

$\frac{1}{3} = \frac{1}{2}$

③  $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$      $u = -15$      $f = -10$

Que!



① - Reflection at concave mirror

①  $u = -15$   
 $f = -10$

$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$

$\frac{1}{v} = \frac{1}{f} - \frac{1}{u} =$

$\frac{-1}{10} + \frac{1}{15} = \frac{-3+2}{30} = \frac{-1}{30}$

$v = -30$

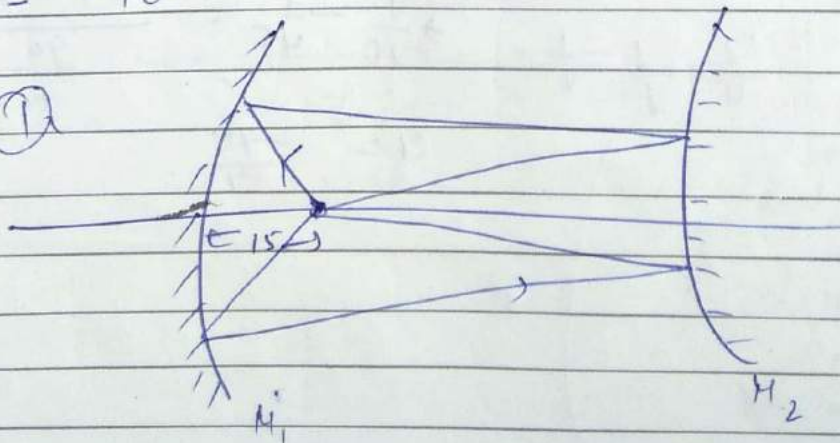
② → Reflection at convex mirror

$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

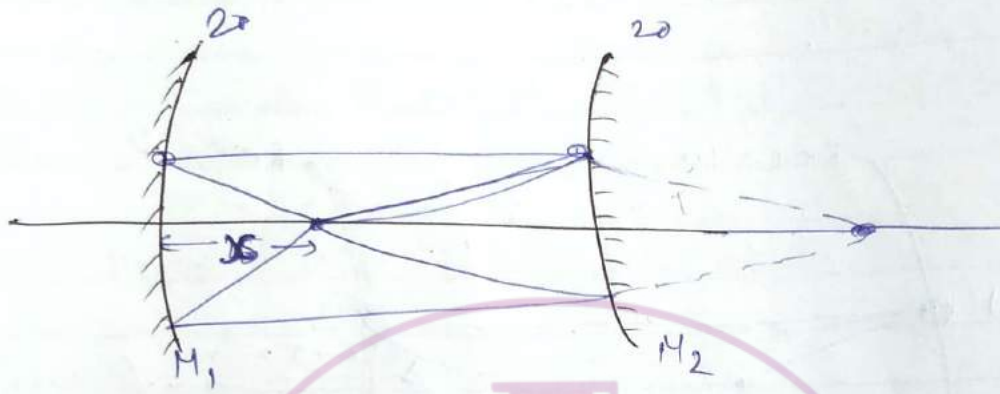
$u = +5$      $f = +10$

$v = -10$

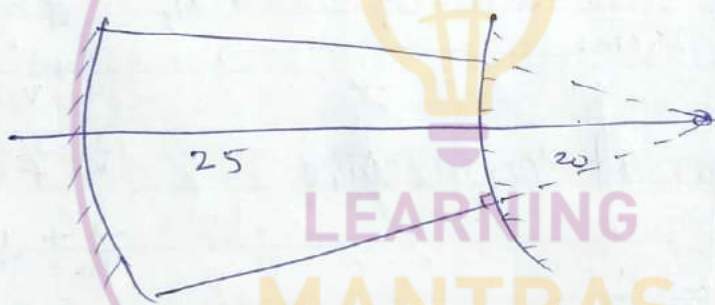
③ Equal as ①



In the above Que find the position of object from the mirror 1 so that ray will retrace its path, after 2nd reflection (at  $M_2$ )



$\angle$  angle of Incidence = 0



$v = -45, f = -10$

$u = ?$

$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$\frac{1}{u} = \frac{1}{f} - \frac{1}{v}$

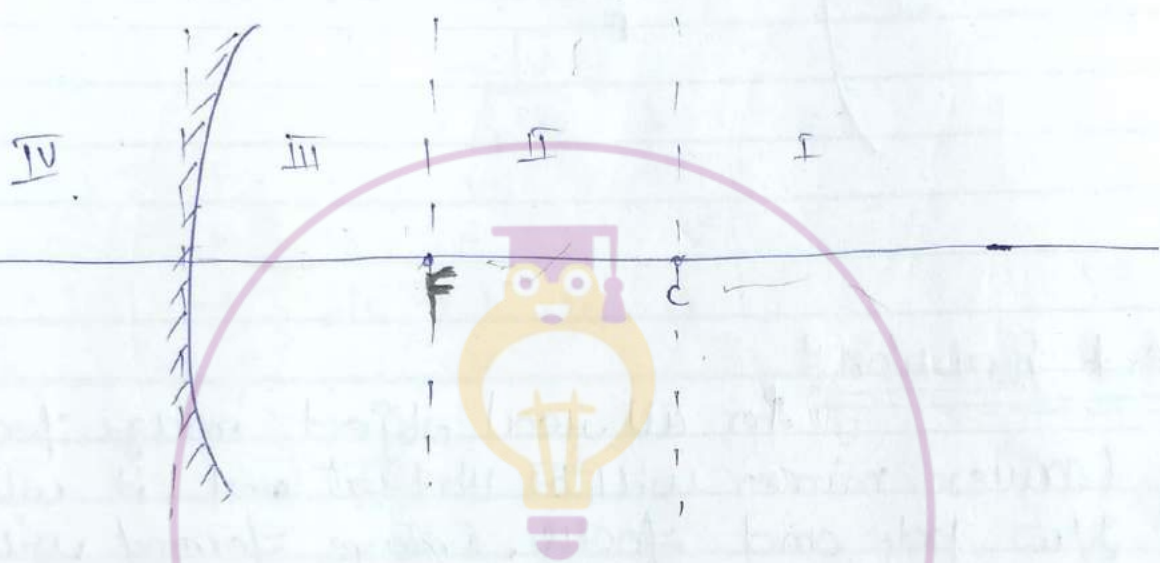
$\Rightarrow \frac{1}{-10} + \frac{1}{45} = \frac{-9 + 2}{90} = \frac{-7}{90}$

$u = \frac{-90}{7}$

\* Important Points for Curved Mirror!

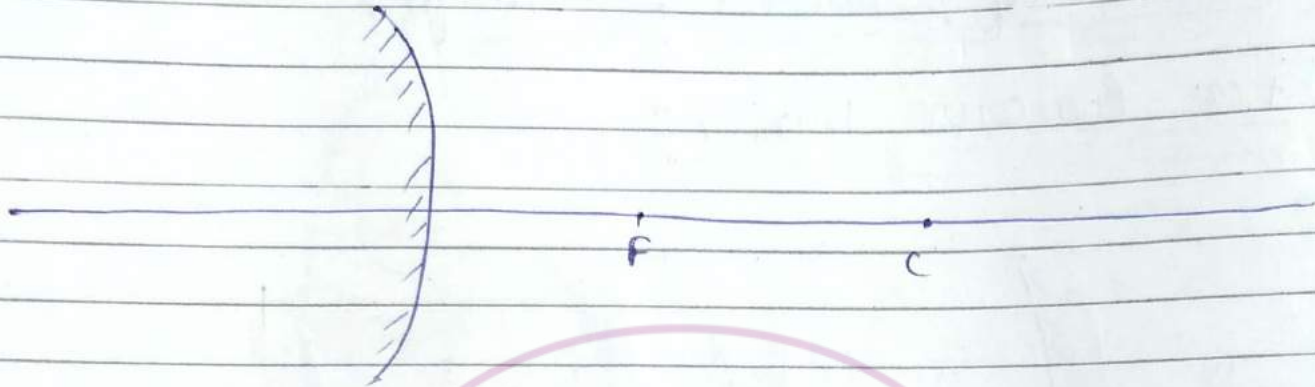
\* Position of & Nature of Image!

(A) for Concave mirror:



| Object Position           | Image Position                    | Nature  |
|---------------------------|-----------------------------------|---|
| $f \geq u \geq 0$<br>real | (0 to $\infty$ )<br>behind mirror | Enlarged (Erect)<br>Real object, virtual Image    |
| between $f$ to $c$        | In front mirror                   | Enlarged, Inverted.<br>Real object, Real Image    |
| beyond $c$<br>$\infty$    | $f$ to $c$<br>$f$                 | diminished<br>Inverted<br>Real object, Real Image |
| behind Mirror             | 0 to $f$                          | diminished, Erect.<br>Virtual object, Real Image  |

\* for Convex mirror

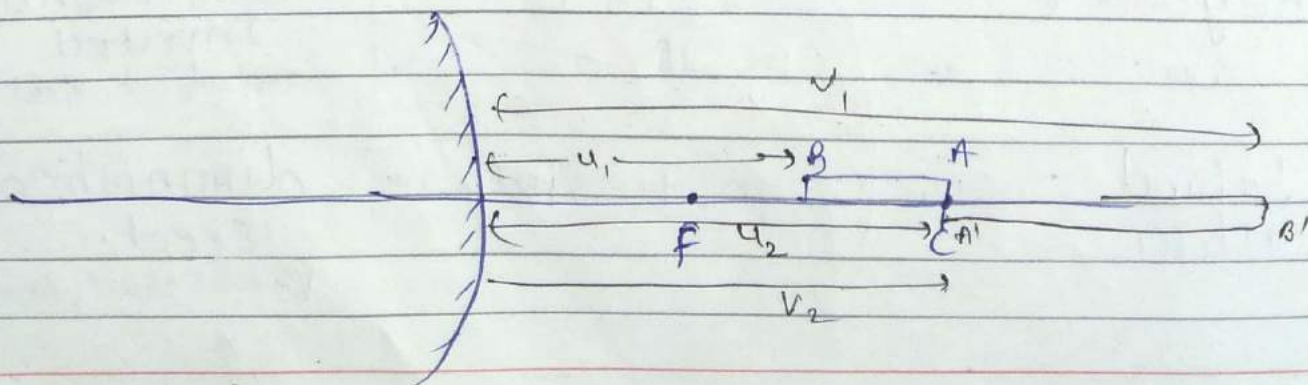


Object Position

(i) for all real object image formed by convex mirror will be virtual and it will be b/w pole and focus. Image formed will be diminished.

(ii) Convex mirror can form real as well as virtual image for virtual object.

(2) Longitudinal magnification:  
When an object is placed along the principle axis image magnification is known as longitudinal magnification.



for all mirrors

$$M = \frac{L_I}{L_O} = \frac{v_1 - v_2}{u_2 - u_1}$$

(ii) if an object is very short.

$$= -\frac{dv}{du}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$-\frac{1}{v^2} dv - \frac{1}{u^2} du = 0$$

$$-\frac{dv}{du} = \frac{v^2}{u^2}$$

Longitudinal  $M_L = M_T^2 \text{ or } \frac{v^2}{u^2}$

Ques: An object of length 10cm is placed along principle axis of a concave mirror having radius of curvature 40 cm. Near end of an object is at a dist. of 30 cm. from the pole find longitudinal magnification and length of image.

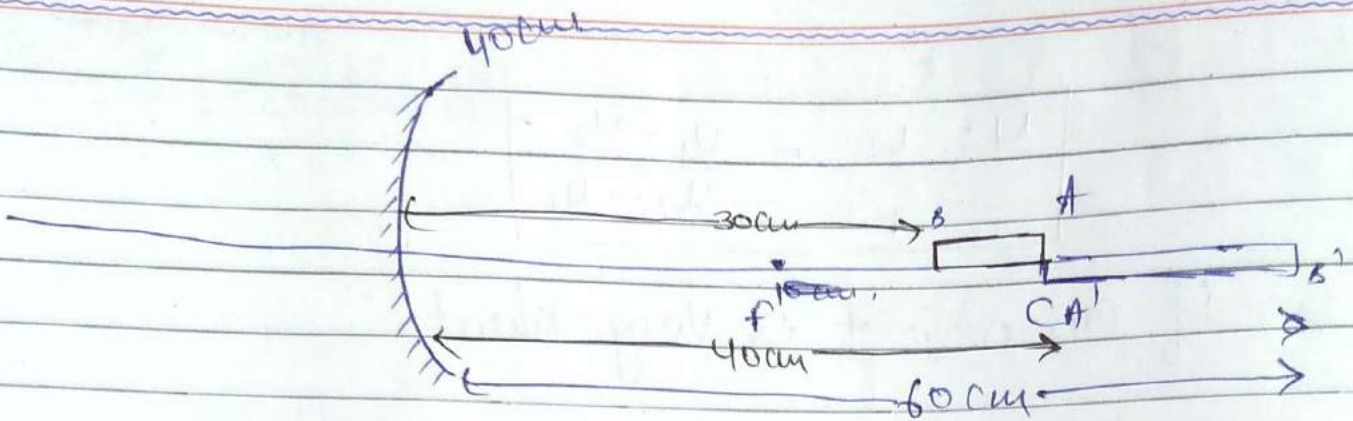
(ii) In the above Ques if a cube of length side length 1 millimeter is placed at a distance of 60 cm from the same mirror. find volume of the image obtained.



Trance - RA I

Long P-A 1126

(1)



$$\frac{v}{u}$$

$$\frac{40}{30} = \frac{10}{u}$$

$$\frac{1}{u} + \frac{1}{u} = \frac{1}{f}$$

$$u = -30 \quad f = -20$$

$$v = ?$$

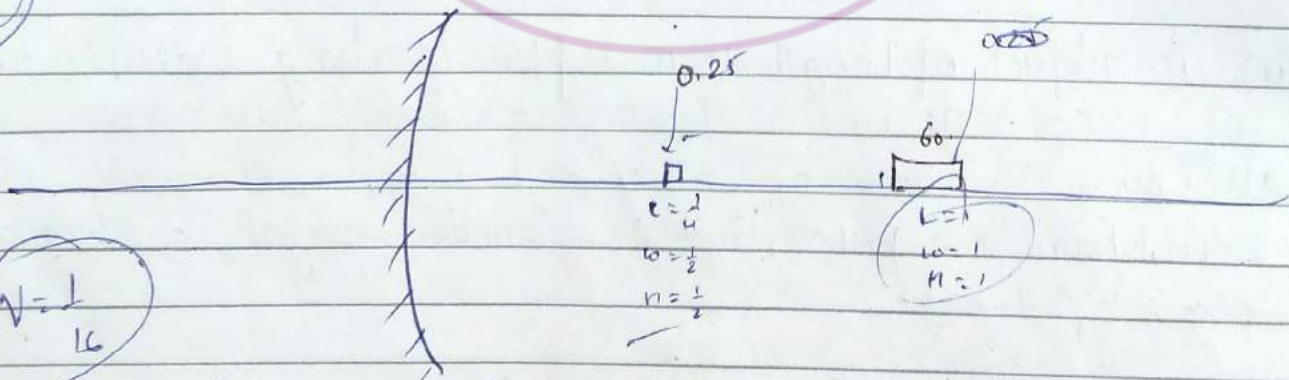
$$v = -60$$

$$L_f = 20$$

$$\frac{60 - 40}{40 - 30} = 2$$

$$M_L = \frac{60 - 40}{40 - 30} = \frac{20}{10} = 2$$

(2)



$$v = \frac{1}{10}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$u = -60 \quad f = -20$$

$$v = -30$$

$$\frac{dv}{du} = \left( \frac{v^2}{u^2} \right) = \left( \frac{10}{2} \right)^2 = \frac{1}{4}$$

convex  
~~convex~~ focus  
 convex  
 +ve focus

$$\frac{h_i}{h_o} = \frac{-v}{u}$$

$$L = \frac{1}{4}$$

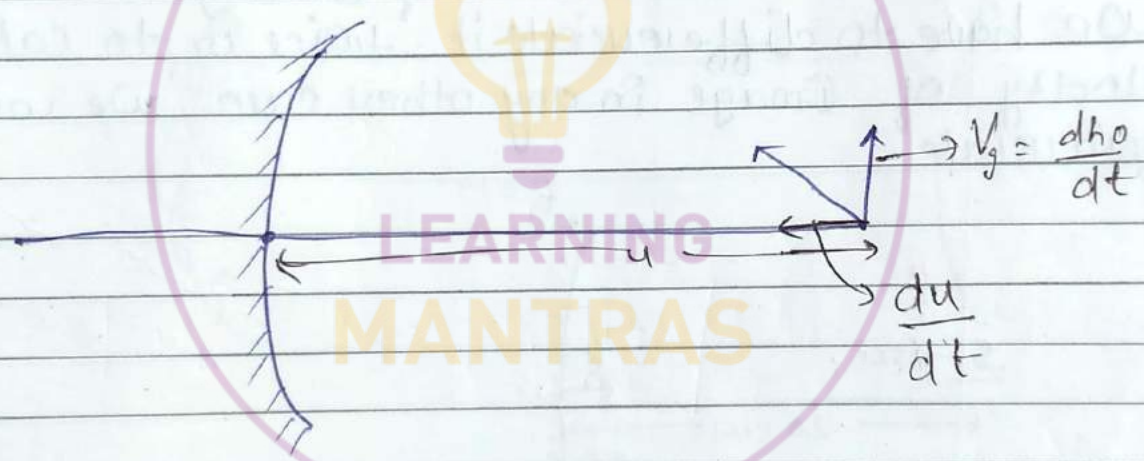
$$w = \frac{1}{2}$$

$$\frac{h_i}{1 \text{ mm}} = \frac{1}{2}$$

$$H = \frac{1}{2}$$

$$= \frac{1}{1.6}$$

(iii) Velocity of Image and object for a spherical mirror.



$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$-\frac{1}{v^2} \frac{dv}{dt} - \frac{1}{u^2} \frac{du}{dt} = 0$$

$$V_f = \frac{-v^2}{u^2} V_o \text{ // principle axis}$$

(b)  $\frac{h_i^0}{h_o} = \frac{v}{u}$  [if  $v$  is constant]

$h_i^0 = \frac{v}{u} h_o$

$\frac{dh_i}{dt} = \frac{v}{u} \frac{dh_o}{dt}$

$v_i$

$v_o$

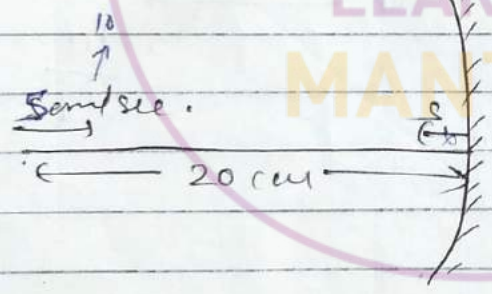
$v_i = -\frac{v}{u} v_o$

Note: To calculate acc. of an object we have to differentiate it twice or to calculate velocity of image in any other case we will differentiate

$f = 15$

LEARNING MANTRAS

Q.



find velocity of image with ground.

$f = 15$     $u = 20$

$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$\frac{1}{v} = \frac{1}{f} - \frac{1}{u}$

$= \frac{1}{15} - \frac{1}{20} = \frac{4-3}{60} = \frac{1}{60}$

$v = 60$

$v_i = -\left(\frac{v}{u}\right)^2 v_o$

$= -(9)v_o$

$v_i = -90$

$$N_{PM} = 90 = v_f - v_m$$



$$90 + v_m = v_f$$

$$90 + 5 = v_f$$

$$v_f = 95$$

\* Direction of Velocity of Image can be predicted by making ray along velocity

And velocity of Image is along the reflected ray



LEARNING  
MANTRAS

\* Power of a Mirror!

$$= \frac{1}{f}$$

|   |
|---|
| Power of mirror = $\frac{1}{f}$ dioptre |
|---|

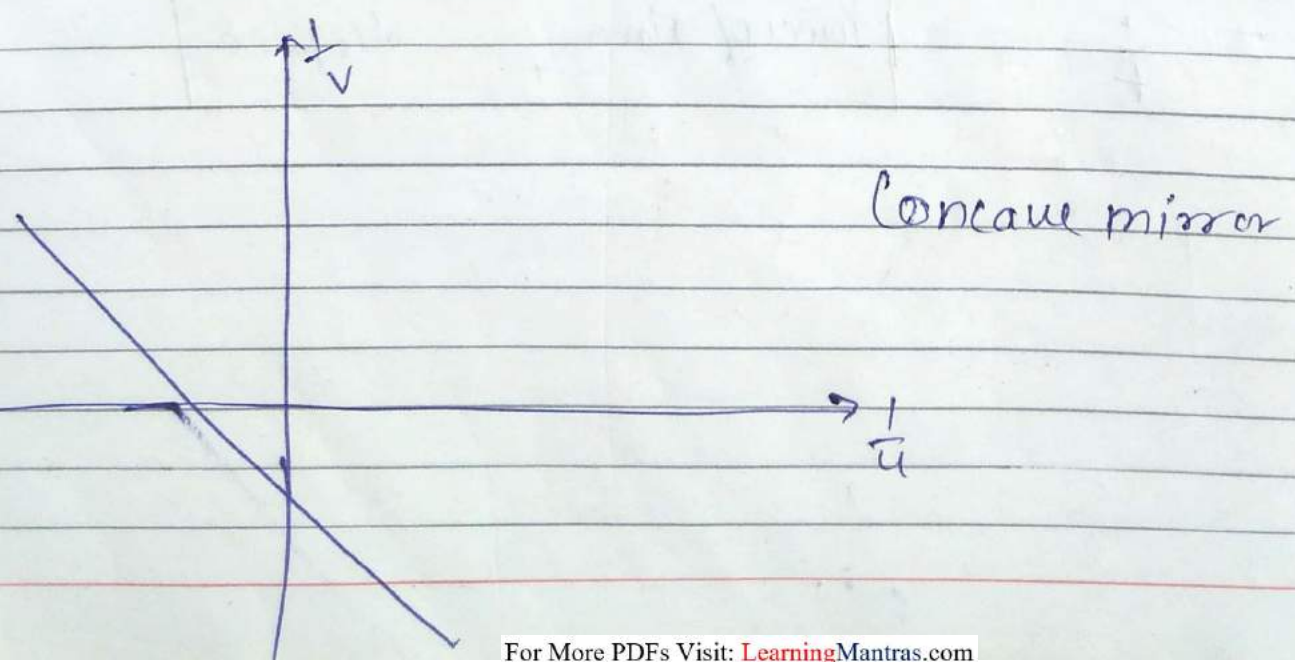
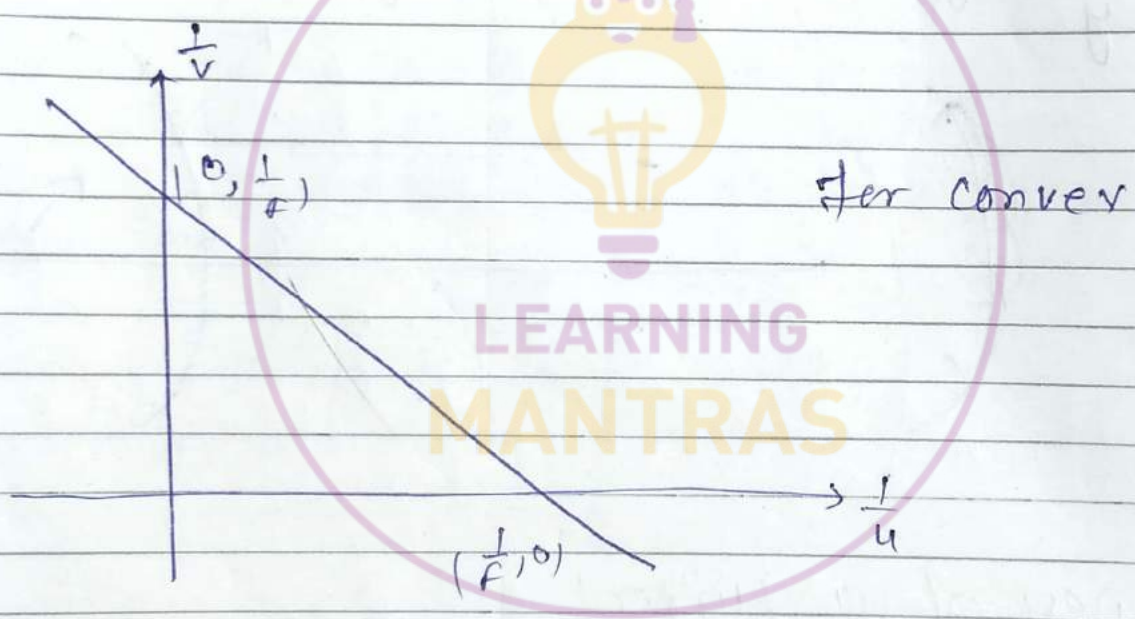
- F cm

# \* Graph of Spherical Mirror:

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$\left[ \frac{1}{v} = \frac{1}{u} + \frac{1}{f} \right]$  → for convex mirror

$\left[ \frac{1}{v} = -\frac{1}{u} - \frac{1}{f} \right]$  → for concave mirror



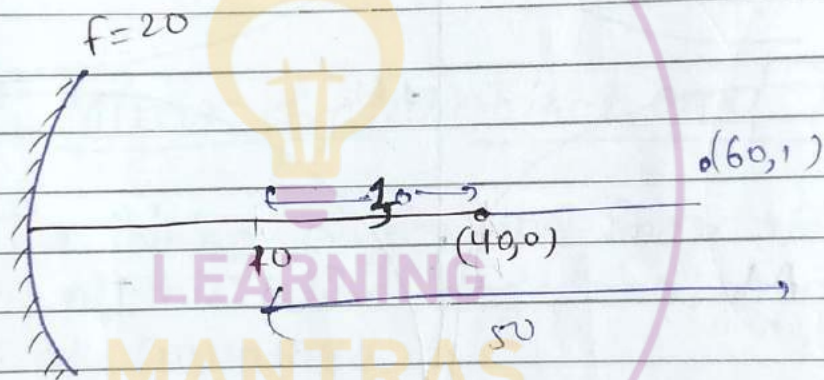
\* Newton's formula :

$$x_1 x_2 = f^2$$

where  $x_1$  and  $x_2$  are the distances of object and image from focus

object and image both lies on the same side of focus.

Ques:



$$20 \times x_1 = 10 \times 10$$
$$x_1 = 5$$

= 15 cm

$$30 \times v = 100$$

$$v = \frac{100}{30} = \frac{10}{3}$$

$$= 10 + \frac{10}{3} = \frac{40}{3} \text{ cm}$$

(ii)

$$50 \times x = 10 \times 10$$

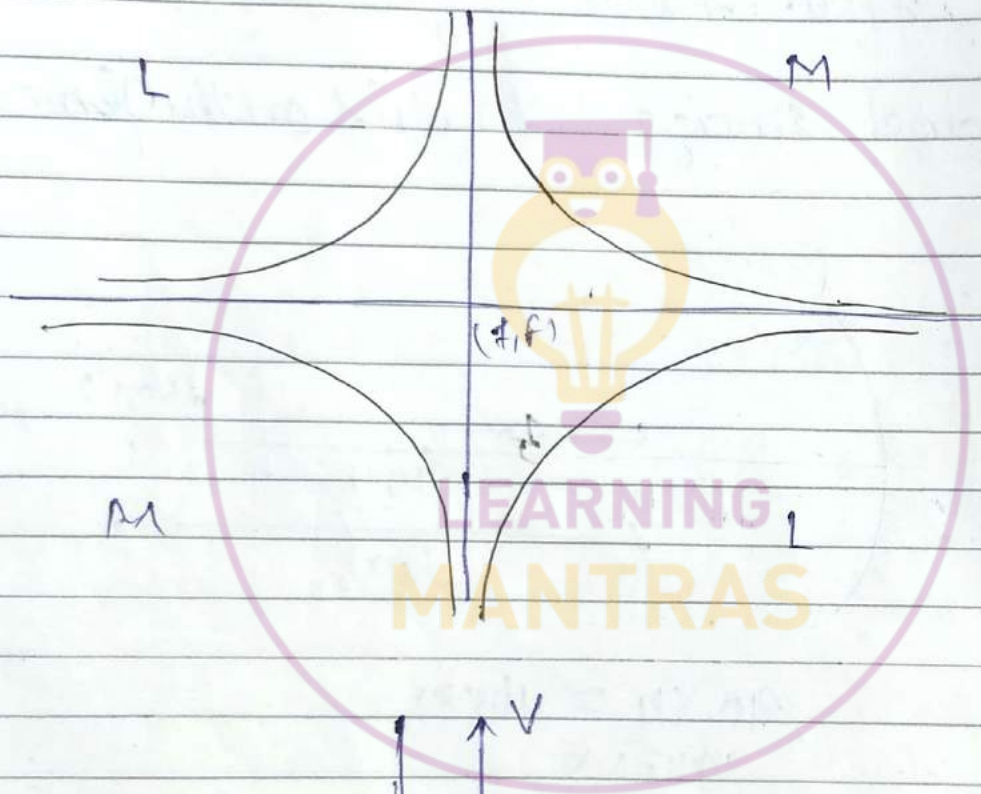
$$x = 2$$

$$\text{Ans} = 10 + 2 = 12$$

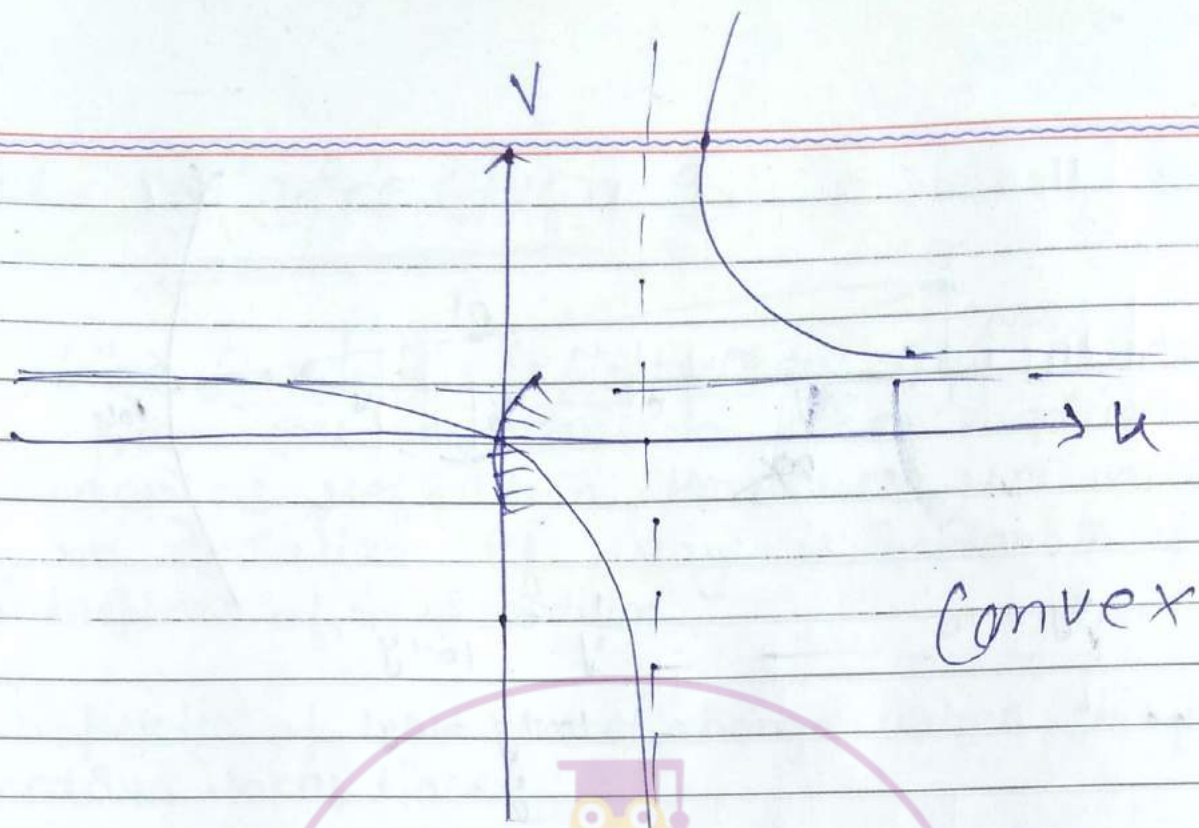
$$\frac{xy}{r^2} = \text{Constant}$$

$$x_1, x_2 = f^2$$

$$(y-f)(u-f)$$



Concave



Convex

\* Location of mirror from object and image:

\* Draw a line joining object and image point of intersection of this line and principle axis gives centre of curvature

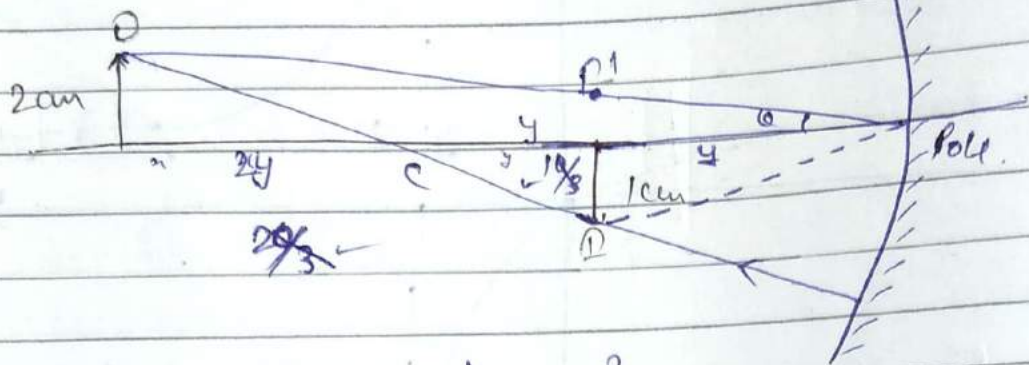
\* Draw a conjugate point (reflection of object or image in principle axis is known as conjugate point) and join with other point

Line  $OI'$  or  $I'O'$   
where  $O'$  &  $I'$  are conjugate points

Intersection of this line with principle axis gives Pole.



or  $2\text{cm}$



$$3y = 10$$

$$\frac{1}{y} = \frac{2}{10+y}$$

$$10+y = 2y$$

$$y =$$



LEARNING  
MANTRAS

## \* Refraction :

Defn Bending of light when ray passes from one medium to other medium is known as refraction. However there will be no deviation if ray is incident normally on interface of two medium.

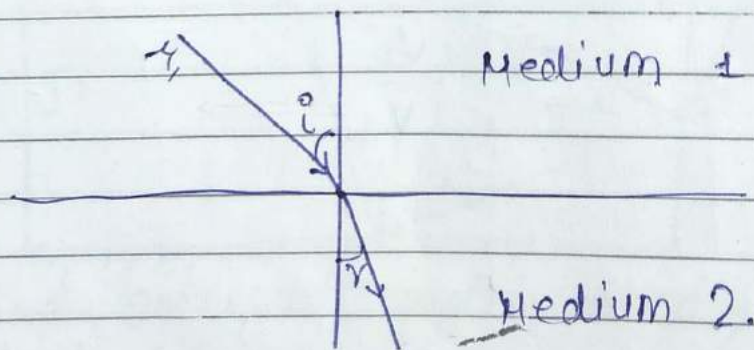
Property of light make change when change in medium takes place.

## \* Law of Refraction : 'Snell's law'

Law: 1: Incident ray, normal ray and refracted ray all three lies in same plane.

$$\hat{i} \cdot (\hat{n} \times \hat{r}) = 0$$

## Law 2 (Snell's)



$$\frac{\sin(i)}{\sin(r)} = \mu = \text{refractive index}$$

$$\mu_1 \sin i = \mu_2 \sin r$$

Q

$$\mu_1 [\hat{e} \times \hat{n}] = \mu_2 [\hat{r} \times \hat{n}]$$

Snell's Law

## \* Refractive Index:

Ratio of velocity of light in Vacuum to that of velocity of light in medium is known as refractive index.

$$\mu = \frac{c}{v_1}$$

$$\uparrow$$

RI of Medium w.r.t Air.

$$\mu_2 = \frac{v_1}{v_2}$$

$$\mu_2 = \frac{c}{v_2}$$

$$\frac{\mu_2}{\mu_1} = \frac{c/v_2}{c/v_1}$$

refractive of 2 w.r.t

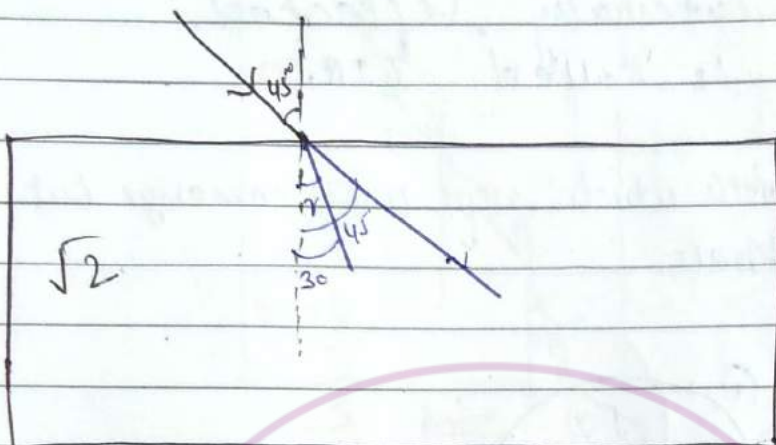
$$= \frac{v_1}{v_2}$$

G atomke

b - neg  
c - term.

Next Row  
 $\mu = 2$   $0 \rightarrow 1$  to  $17$   
New =  $\phi$  1 to 10

Q Find angle of refraction and deviation produce in the ray.  
Refractive  $\mu$  of Medium is  $\sqrt{2}$



$$\frac{\sin 45}{\sin r} = \sqrt{2}$$

$$\frac{\sin r}{\sin 45} = \frac{1}{\sqrt{2}}$$

$$\frac{\cancel{\sqrt{2}} \sin r}{\cancel{\sqrt{2}} \sqrt{2}} = \frac{\cancel{\sqrt{2}}}{2}$$

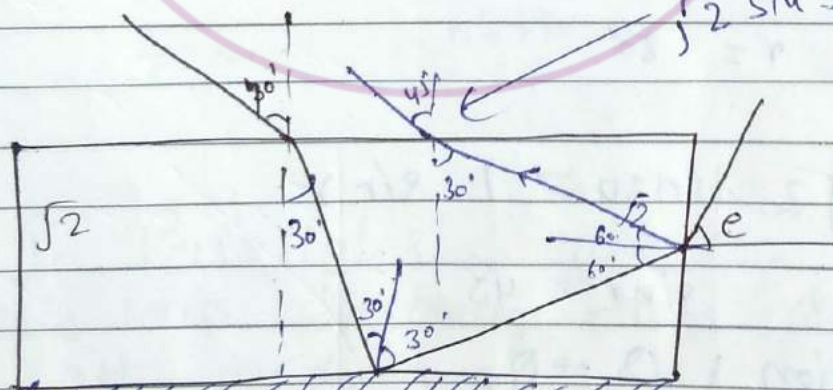
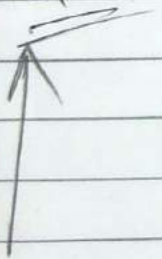
$$\sin r = \frac{\sqrt{2}}{2}$$

$$\sin 45^\circ = \sqrt{2} \sin r$$

$$\frac{1}{\sqrt{2}} = \sqrt{2} \sin r$$

$$\Rightarrow \sin r = \frac{1}{2} \Rightarrow r = 30^\circ$$

Q.



Then too  
ray become  
parallel.

find emergent angle  $e$  angle with which  
light ray  $\neq$

$$\sqrt{2} \sin 60 = 1 \sin e$$

$$\sin e = \frac{\sqrt{3}}{2}$$

$$\sin e = \frac{\sqrt{3}}{2}$$

$$\sqrt{3} \sin 60 = \sin e$$

$$\sqrt{3} \frac{\sqrt{3}}{2} = \sin e$$

$$\sin e = \frac{\sqrt{3}}{2}$$

never

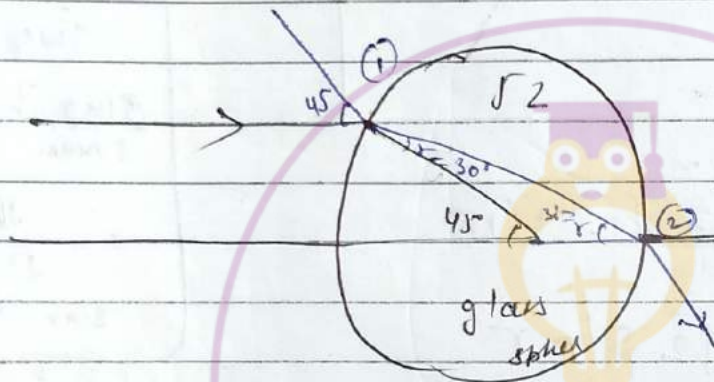
$\sin e > 1$

ray not come  
in  $e$  part

$\sin \theta > 1$  never.  $\rightarrow$  Imp.

Ray will get internally reflected.  
this phenomenon is called TIR.

Ques! find angle with which ray will emerge out from the glass sphere



$$\sin 45^\circ = \sqrt{2} \sin r$$

$$\frac{\sqrt{2}}{2} = \sqrt{2} \sin r$$

① — (M)  $\sin i = \mu_2 \sin r$   
because in Air  $\mu_1 = 1$   
 $1 \cdot \frac{1}{\sqrt{2}} = \sqrt{2} \sin r$

$$\frac{1}{2} = \sin r$$

$$r = 30^\circ$$

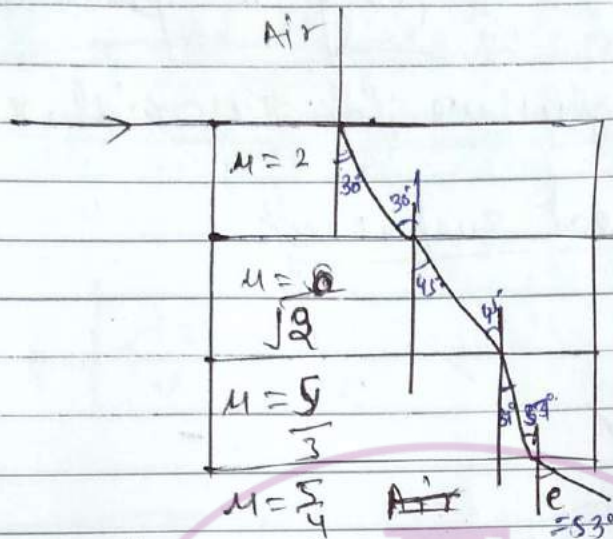
②  $\sqrt{2} \sin 30 = 1 \sin r$

$$\sin r = \frac{\sqrt{2}}{2}$$

deviation  $\theta_1 + \theta_2$

$$\frac{4}{5} = \sin r$$

Ques



$$\mu = 2$$

$$1 \sin 90 = \frac{5}{4} \sin r$$

$$1 = \frac{5}{4} \sin r$$

$$\frac{4}{5} = \sin r$$

Find angle of emergence of the ray of the glass ray. (3) reflection

$$1 = 2 \sin r \quad \sin r = \frac{1}{2} = \sin 30^\circ$$

$$2 \sin 30^\circ = \frac{2 \times 1}{2} = \sqrt{2} \sin r$$

$$\frac{1}{\sqrt{2}} = \sin r \quad \sin r = \frac{1}{\sqrt{2}} = \sin 45^\circ$$

$$\frac{5}{3} \times \frac{3}{5} = \frac{5}{4} \sin r$$

$$\sqrt{2} \sin 45^\circ = \frac{5}{3} \sin r \quad \sqrt{2} \times \frac{1}{\sqrt{2}} = \frac{5}{3} \sin r$$

$$\frac{3}{5} = \sin r \quad \sin r = \frac{3}{5} = \sin 37^\circ$$

$$\frac{4}{5} = \sin r \quad e = r = 53^\circ$$

Note: In Parallel slab we can apply Snell's law directly to first medium and last medium.

Snell's law is independent from intermediate medium if reflecting surfaces are parallel to each other.

Dmp. Board

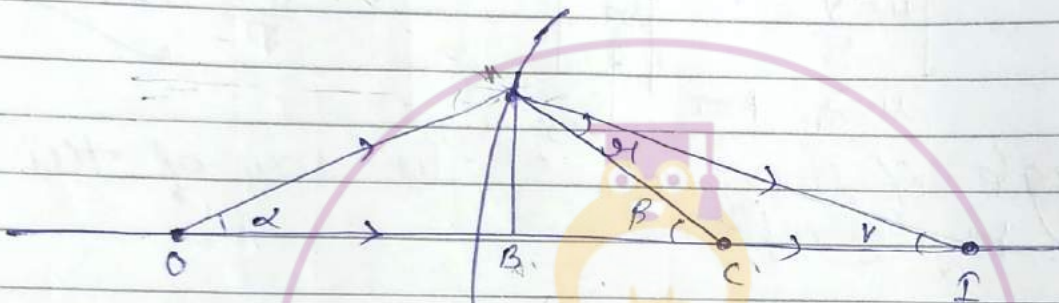
$r \rightarrow \infty$  plane

\* Apparent depth:

(only for small angle)

Refraction at plane surface for paraxial rays

Refraction at curved surfaces



$$\tan \alpha = \frac{AB}{rO} = \frac{AB}{u} \quad \alpha + \beta = i^{\circ}$$

$$\tan \beta = \frac{AB}{BC} = \frac{AB}{R} \quad r + u = R$$

$$\mu_1 \sin i^{\circ} = \mu_2 \sin \beta$$

$$\mu_1 i^{\circ} = \mu_2 \beta$$

$$\mu_1 (\alpha + \beta) = \mu_2 (\beta - r)$$

$$\mu_1 \alpha + \mu_2 r = (\mu_2 - \mu_1) \beta$$

$$\mu_1 \frac{AB}{u} + \mu_2 \frac{AB}{r} = (\mu_2 - \mu_1) \frac{AB}{R}$$

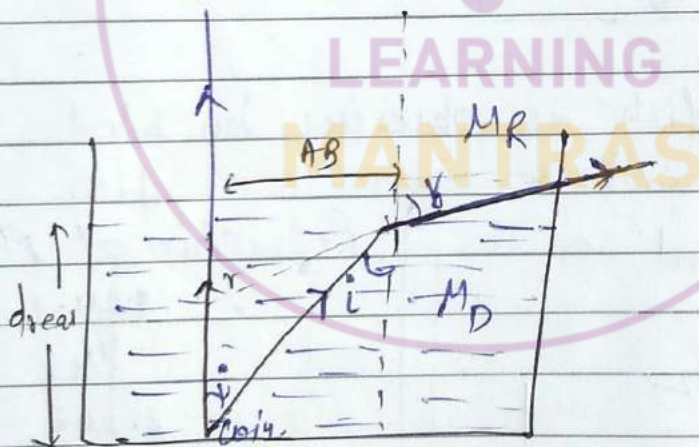
By putting sign convention  
to make nature free

$$\frac{\mu_1}{-u} + \frac{\mu_2}{v} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{\infty} \quad \text{for plane mirror}$$

$$\frac{\mu_2}{v} = \frac{\mu_1}{u}$$

\* Apparent depth!



$$\mu_D \sin i^\circ = \mu_r \sin r$$

$$\mu_D i^\circ = \mu_r r$$

$$\mu_D \frac{AB}{d_{\text{real}}} = \mu_r \frac{AB}{d_{AB}}$$



$$d_{app} = \frac{d_{real}}{\frac{\mu_o}{\mu_r}} \quad \text{or} \quad \frac{d_{real}}{\mu_{object} / \mu_{observer}}$$

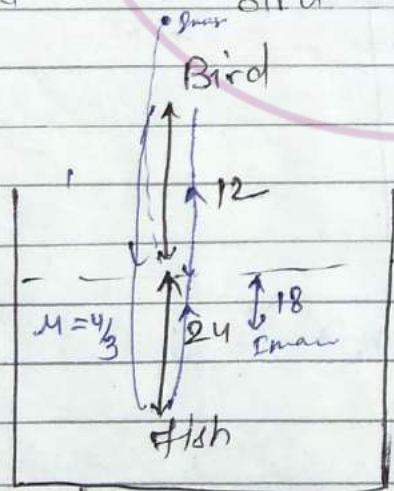
$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{\infty}$$

$$\frac{\mu_R}{v} + \frac{\mu_o}{d_{real}} = 0$$

$$\frac{\mu_R}{v} = -\frac{\mu_o}{d_{real}}$$

$$-\mu_R \frac{d_{real}}{\mu_o} = v$$

Q. find dist. of fish as observer by bird.



Refraction at plane surface

$$= \frac{0.24 \cdot 1}{\frac{4}{3}}$$

$$= \frac{3 \cdot 24 \cdot 6}{4} = 18.$$

$$= 18 + 12 = 30$$

$$= \frac{12 \cdot 4}{1 \cdot \frac{3}{4}} = \frac{36 \cdot 4}{3} = 48$$

Refraction at plane surface

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = 0 \Rightarrow \frac{1}{v} - \frac{4}{3(-24)} = 0$$

$$18 + 12 = 30 \quad v = -18$$

②

$$\frac{u_2}{v} - \frac{u_1}{u} = 0$$

$$\frac{4/3}{v} + \frac{1}{12} = 0$$

$$\frac{4}{3v} + \frac{1}{12}$$

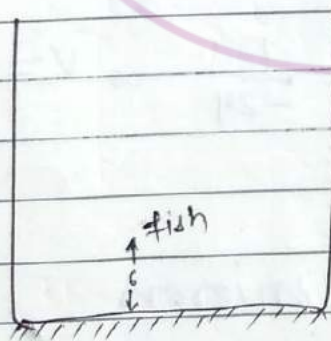
$$\frac{4}{3v} = -\frac{1}{12}$$

$$\frac{3v}{4} = -12$$

$$v = \frac{-12 \times 4}{3} = -16$$

$$16 + 24 = 40 \text{ cm}$$

Ques: find

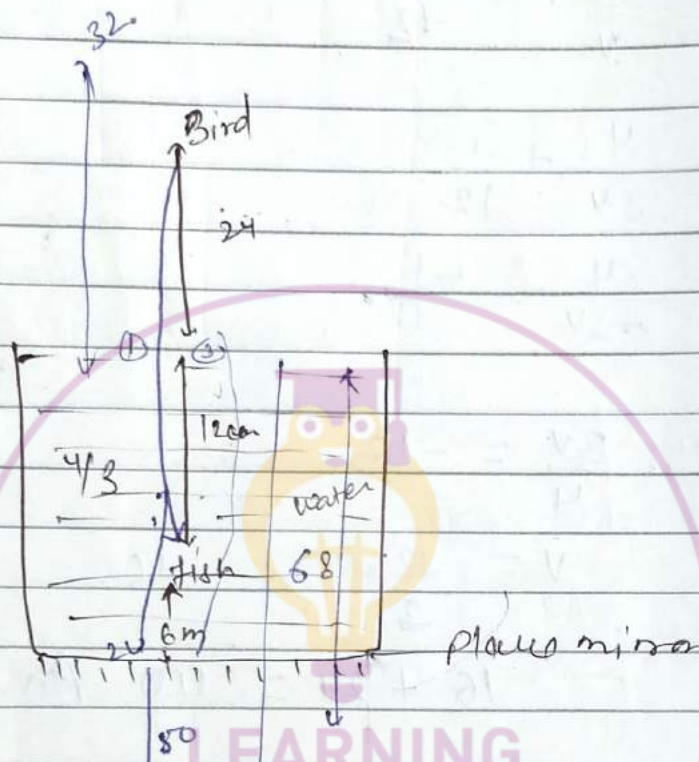


Ques: find distance of image of bird as observed by fish in the mirror

(i) find " " " " " in the mirror as observed by bird

(ii) find the I of fish as observed by

(iv) find dist of image of fish as observed by bird, if  
no mirror



(i) Refraction at plane surface

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{\infty}$$

$$\frac{\mu_2}{v} = \frac{\mu_1}{u} \Rightarrow \frac{4}{3v} = \frac{1}{-24} \Rightarrow v = -32$$

(ii) Reflection at plane mirror

$$\frac{1}{v} + \frac{1}{u} = \frac{2}{R = \infty}$$

$$\frac{1}{v} = -\frac{1}{u}$$

$$u = -v$$

50 m below the mirror

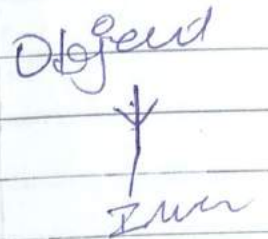
Obj ray  $\rightarrow$  Image

### (3) Refraction at Plane surface

$$\frac{\mu_2}{v} = \frac{\mu_1}{u} \Rightarrow \frac{1}{v} = \frac{4}{3(68)}$$

$$v = \frac{3(68)}{4}$$

$$v = 51$$



(i)  $\frac{1}{v} = \frac{4}{3(12)}$   $v = 9$

(ii) 66 ans

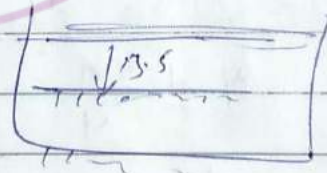
(iii) 12 Ans

(iv)  $\frac{1}{v} = \frac{4/3}{246}$

$$v = 18$$

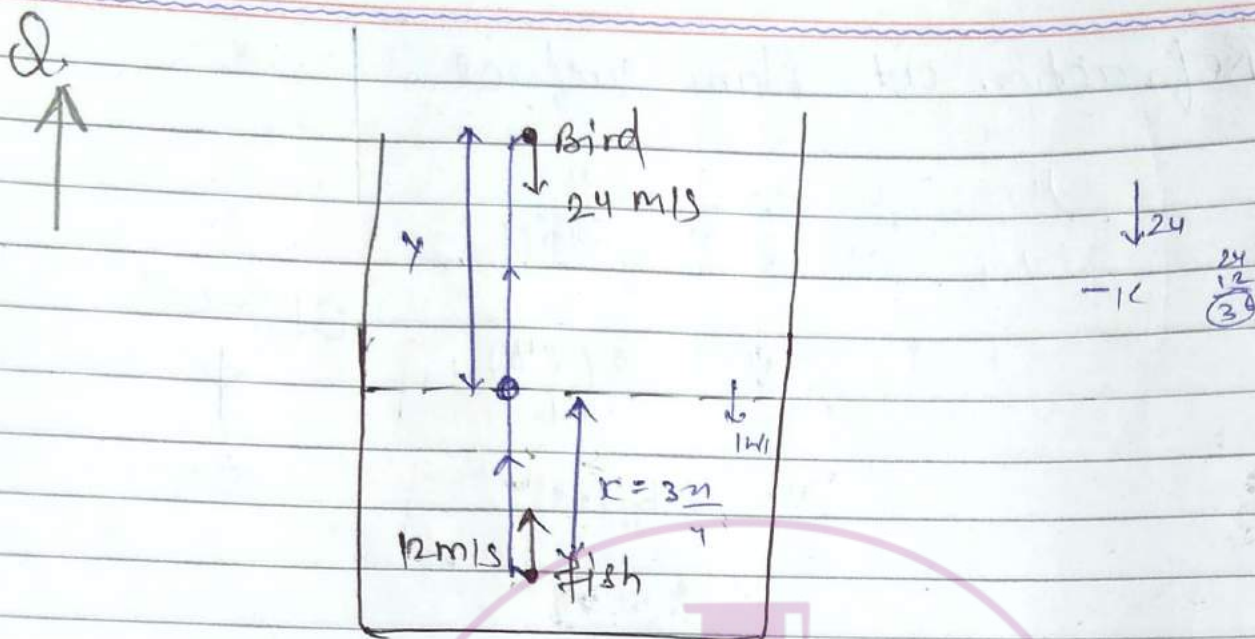
$$\frac{1}{v} = \frac{4}{3(18)}$$

$$v = \frac{54}{4} = 13.5$$



$\frac{24}{12}$   
 $3^c$

$$\frac{d(\text{distance})}{dt} = \text{velocity}$$



Ques: find the velocity of fish as observed by Bird

$$\frac{u_2}{v} = \frac{u_1}{4}$$

$$\frac{1}{v} = \frac{4}{3(n)}$$

$$v = \frac{3n}{4}$$

$$\frac{u_2}{v} = \frac{u_1}{4} \Rightarrow \frac{u_2}{\frac{3n}{4}} = \frac{24}{4}$$

$$u_2 = \frac{24 \times 3n}{4 \times 4} = \frac{18n}{4} = \frac{9n}{2}$$

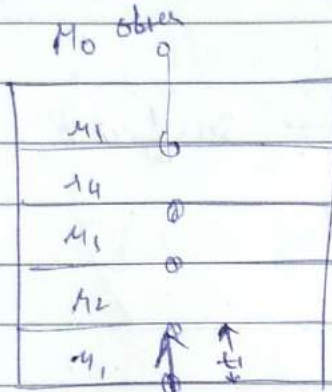
$$D_{FB} = y + \frac{3n}{4}$$

$$V_{FB} = \frac{dy}{dt} + \frac{3}{4} \frac{dn}{dt}$$

$$24 + \frac{3}{4} (12)^2 = 24 + 9 = 33 \text{ m/s}$$

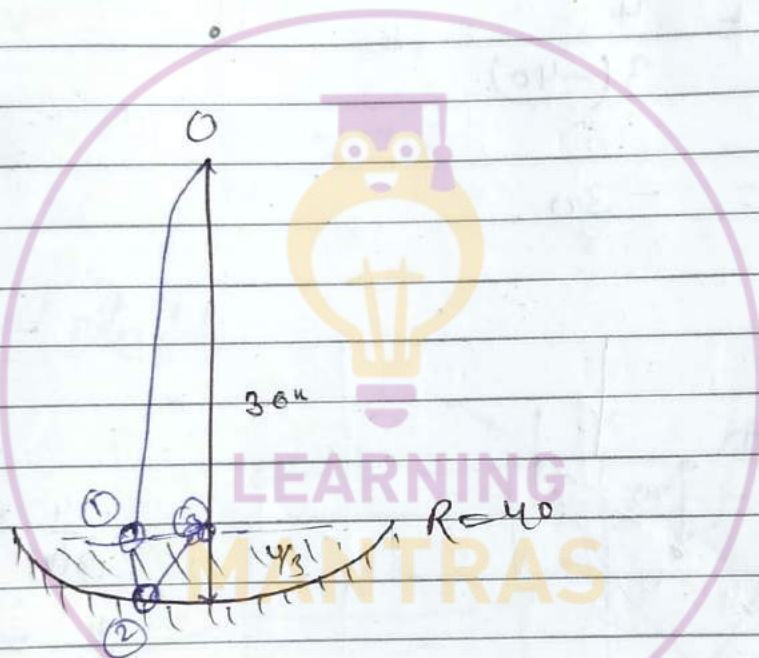
# \* Refraction through of glass slab

Note:



$$\frac{t_1}{\mu_1} + \frac{t_2}{\mu_2} + \frac{t_3}{\mu_3} + \frac{t_4}{\mu_4} + \frac{t_5}{\mu_5}$$

Q



$$\frac{4}{30} - \frac{1}{40} = \frac{1}{v}$$

Find position of final image of an object  $O$  in the given diagram

① Refraction of plane surface

$$\frac{1}{v} - \frac{1}{30} = \frac{1}{20}$$

$$\frac{\mu_2}{v} = \frac{\mu_1}{u} \Rightarrow \frac{1}{3(v)} = \frac{1}{-30} \Rightarrow v = -40$$

② Refraction at curved surface:

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \quad u = -40 \quad f = -20$$

$$v = -40$$

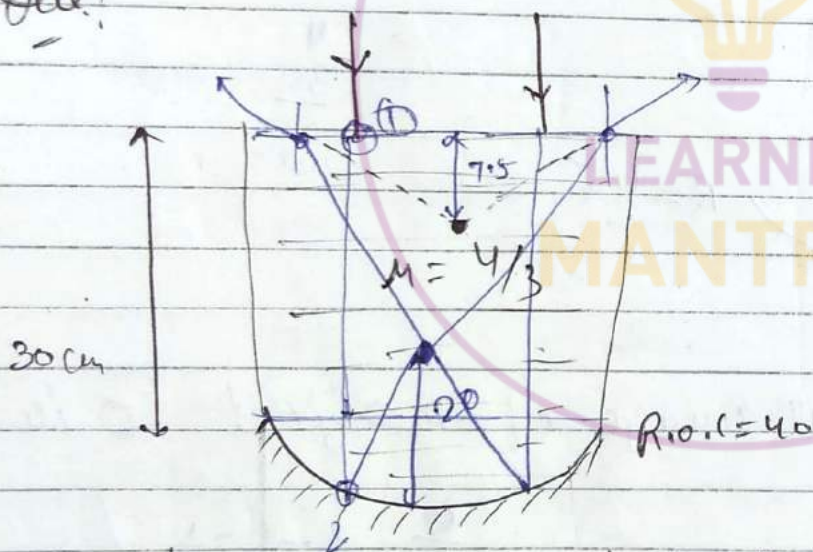
(3) Refraction at plane & Mirror surface

$$\frac{\mu_2}{v} = \frac{\mu_1}{u}$$

$$\frac{1}{v} = \frac{4}{3(-40)}$$

$$v = -30$$

Ques!



$$\frac{4}{3(v)} = \frac{1}{\infty}$$

$$\frac{4}{3(v)} = \frac{4}{3(\infty)}$$

find the position of final image

①  $\frac{\mu_2}{v} = \frac{\mu_1}{u}$

$$\frac{4}{3v} = \frac{1}{\infty}$$

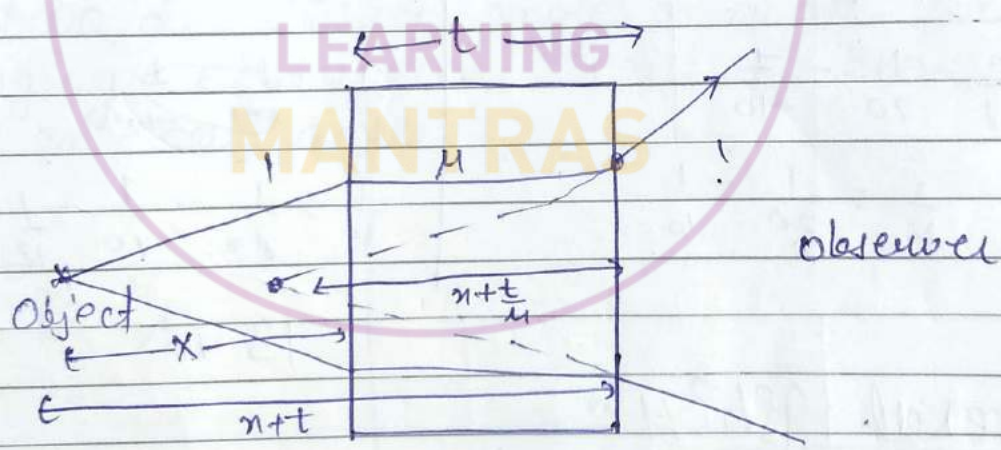
$$v = \infty$$



②  $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$        $u = \infty$        $f = -20$   
 $\frac{1}{v} + \frac{1}{\infty} = \frac{1}{-20}$        $v = ?$   
 $v = -20$

③  $\frac{1}{v} = \frac{4}{3(10)}$   
 $v = \frac{30}{4} = 7.5$

\* Normal shift :



N.S =  $t \left[ 1 - \frac{1}{\mu_{\text{relative}}} \right]$        $\times \text{Dist.}$

①  $\frac{\mu}{v} = \frac{1}{n}$   
 $\sqrt{v} = \mu n$

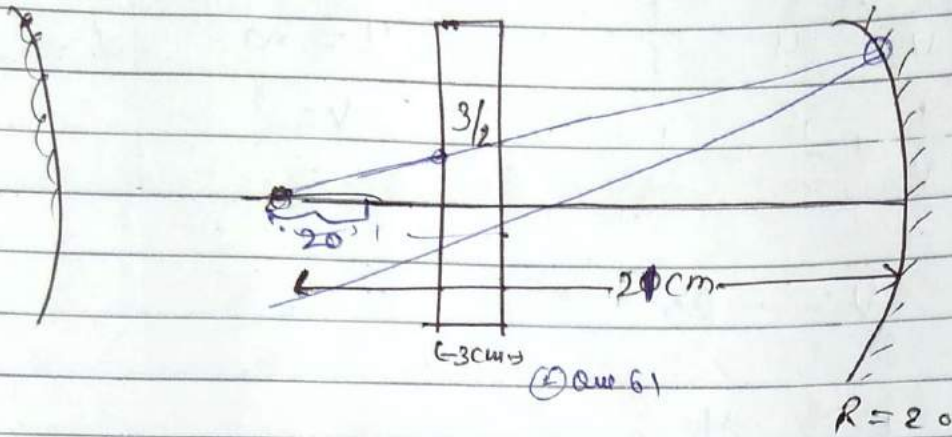
②  $\frac{1}{v_f} = \frac{\mu}{[ \mu n + t ]}$   
 $v_f = \frac{\mu x + t}{\mu}$

$v_f = n + \frac{t}{\mu}$



Ex-1  $3 \times \frac{2}{3} = 2$

Ques!



Final final position of an image

$$M.S = t \left[ 1 - \frac{1}{\mu_{rel}} \right] = \frac{3 \left( 1 - \frac{2}{3} \right)}{3 \left( \frac{1}{2} \right) - 1} \quad \text{①} = \frac{3}{2(\mu)} = \frac{1}{\mu}$$

M-2

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{20} = \frac{1}{-10}$$

$$\frac{1}{v} = \frac{1}{20} - \frac{1}{10}$$

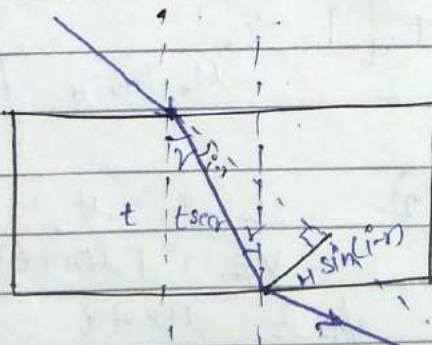
Ans-2

$$\frac{1}{v} - \frac{1}{20} = \frac{1}{-10}$$

$$\frac{1}{v} = \frac{1}{20} - \frac{1}{10} = \frac{1}{12}$$

13 D

lateral shift



$$\frac{t}{H} = \cos r$$

$$L.S =$$

$$L.S = \frac{t \sin(i-r)}{\cos r}$$

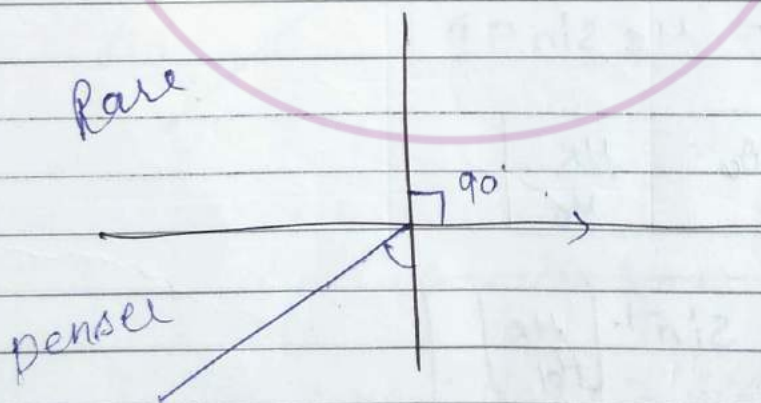
Shift  
toward the  
Normal.

### \* Total Internal Reflection (TIR)

When Ray moves from ~~more~~ denser to rarer medium it may reflect back into the medium for the angle greater than Perpendicular angle. This phenomena is known as total internal reflection.

### \* Critical angle!

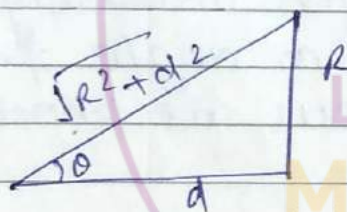
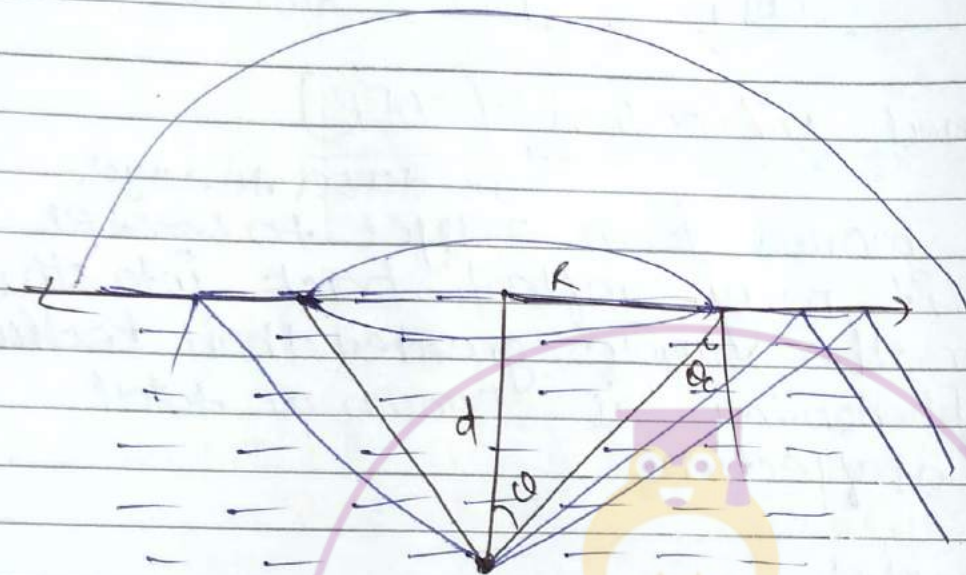
Angle after which ray gets internally reflected is known as Critical angle or angle for which grazing emergence occur is known as critical angle.



$$\mu_D \sin \theta_c = \mu_R \sin 90^\circ$$

$$\sin \theta_c = \left( \frac{\mu_R}{\mu_D} \right)$$

∴ Total illuminance circle



$$\mu \sin \theta_c = \mu_e \sin \theta$$

$$\sin \theta_c = \frac{\mu R}{\mu_e d}$$

$$\theta = \sin^{-1} \left[ \frac{\mu R}{\mu_e d} \right]$$

$$\frac{R}{\sqrt{R^2 + d^2}} = \frac{\mu R}{\mu_e d}$$

$$\frac{R^2}{R^2 + d^2} = \frac{\mu_r^2}{\mu_0^2}$$

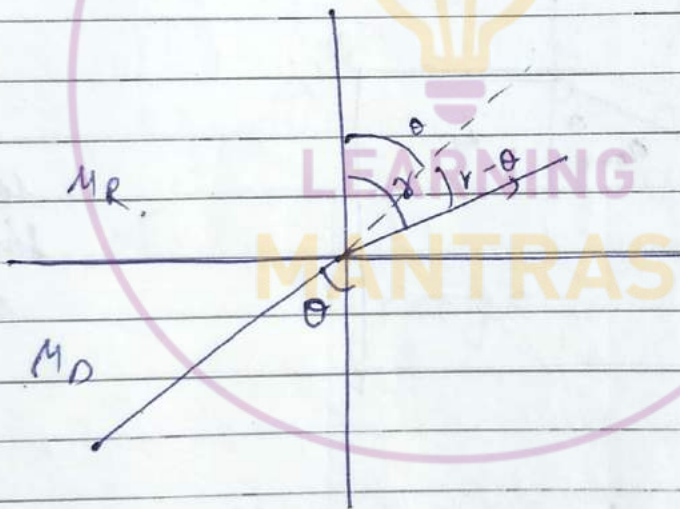
17% goes out

$$R^2 \mu_0^2 = \mu_r^2 R^2 + \mu_r^2 d^2$$

$$R^2 = \left( \frac{\mu_r}{\sqrt{\mu_0^2 - \mu_r^2}} \right) d$$

### \* Deviation of a Ray:

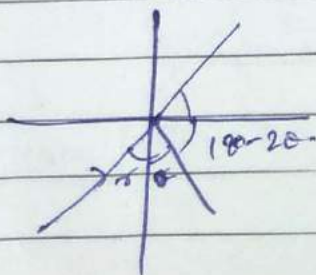
When it moves from denser to rarer medium.



$$\sin \theta = \frac{\mu_r}{\mu_0}$$

$$\mu_0 \sin \theta = \mu_r \sin r$$

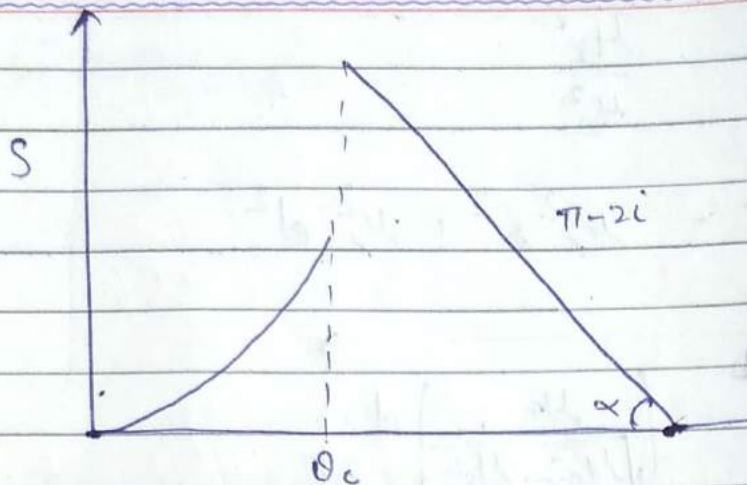
$$\frac{\mu_0}{\mu_r} (\sin \theta) = \sin r$$



$$\sin^{-1} \left( \frac{\mu_0 \sin \theta}{\mu_r} \right) = r$$

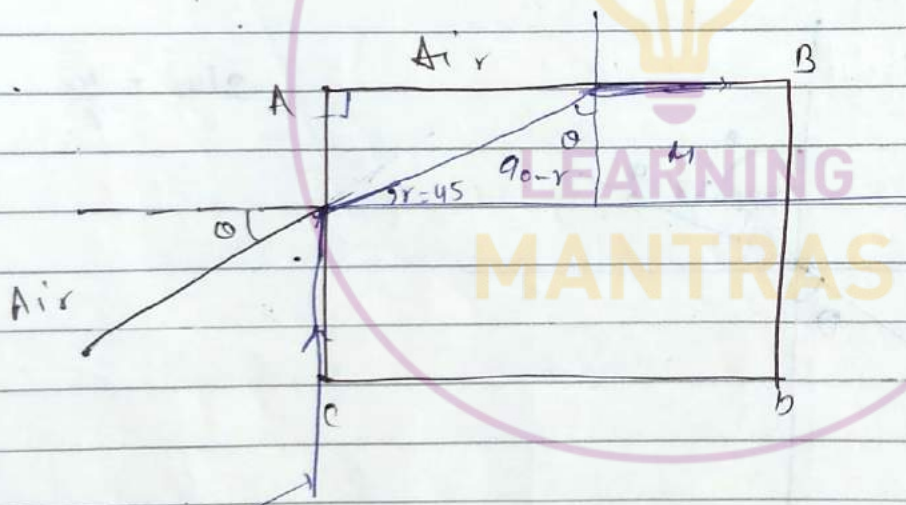
20  
19/20

Critical angle  $\theta_c = \sin^{-1}\left(\frac{1}{\mu}\right)$



Ques

Find Refractive index of the glass slab ABCD so, that ray does not leave out of the glass slab from its lateral side ABCD.



Let

$$\sin \theta = \mu \sin 90^\circ$$

$$\sin \theta = \mu$$

$$\theta = \sin^{-1} \mu$$

ray will go at  $\theta_c$

$$1 \sin 90^\circ = \mu \sin r$$

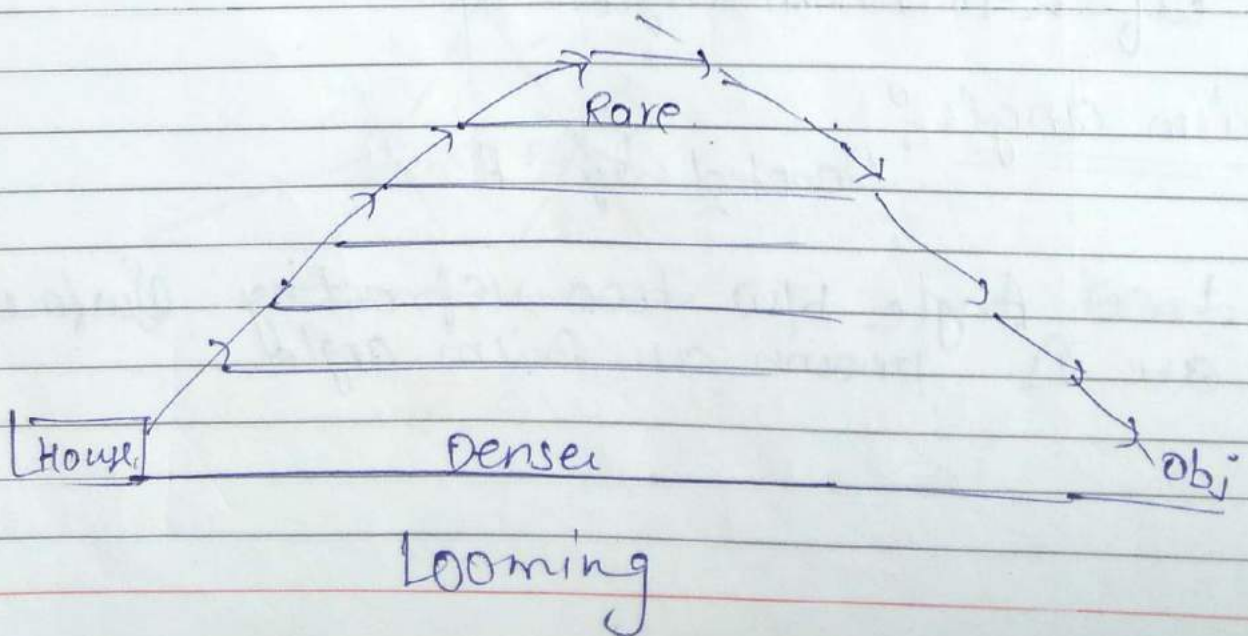
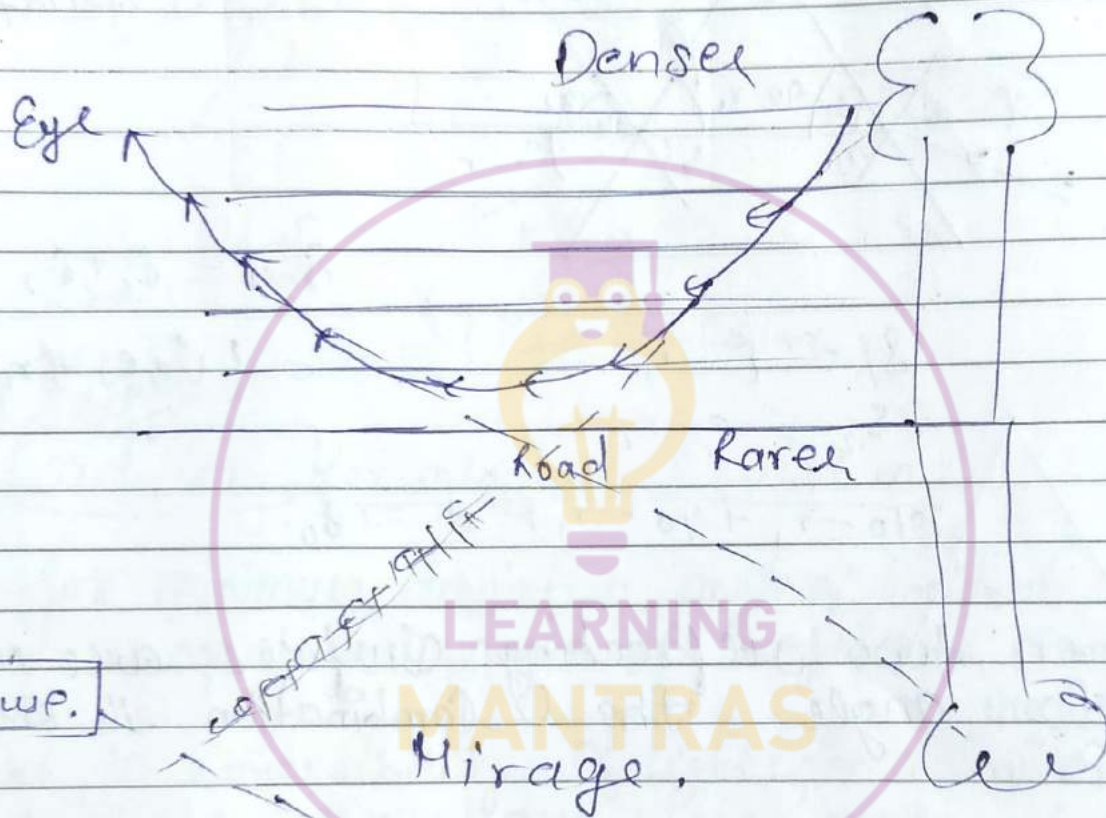
$$\mu \sin (90 - r) = 1 \quad (1)$$

$$\sin 90^\circ = \mu \sin r$$

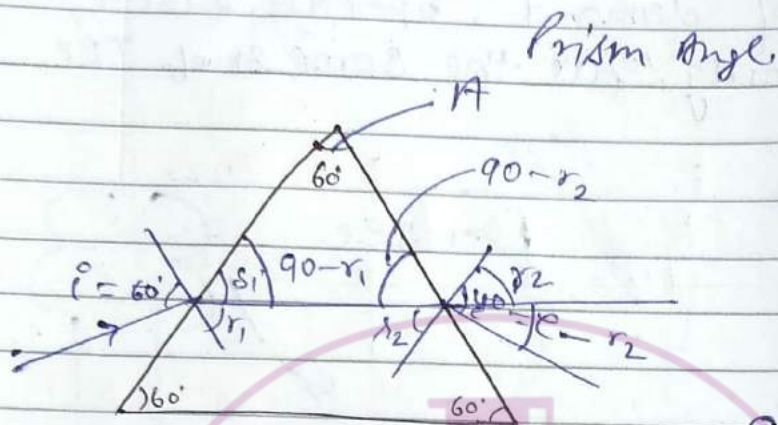
(52)

## \* Application of TIR :

sparkling of diamond, optical fiber, Mirage and looming are the some ex of TIR.



## \* Prism



$\delta \Rightarrow$  deviation

$$S_{net} = \delta_1 + \delta_2$$

$$= (i + e) - (r_1 + r_2)$$

$$\delta_1 = i - r_1$$

$$\delta_2 = e - r_2$$

$$90 - r_1 + 90 - r_2 + A = 180$$

When two refracting surfaces are at an angle the combination is known as Prism.

Glass slab can also be considered as Prism of zero Prism angle.

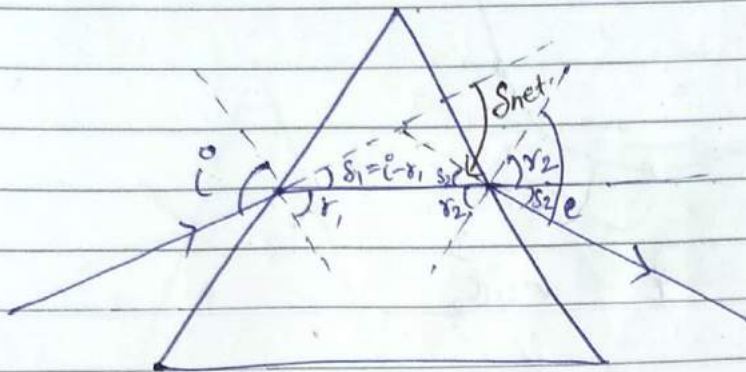
Prism angle :

Denoted by 'A'

$\Rightarrow$  Angle b/w two refracting surfaces is known as Prism angle.

$$\mu_{\text{net}} = \mu_{\text{air}}$$

$$\mu_{\text{cv}} = 1 - \mu - 2\mu$$



$$S_1 = i - r_1$$

$$\phi = S_1 + S_2$$

$$S_2 = (i + e) - (r_1 + r_2)$$

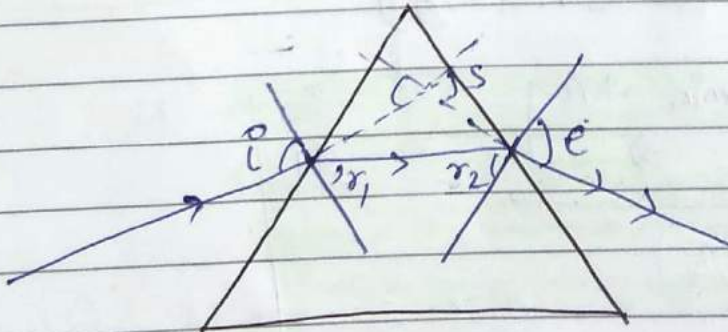
Deviation.

Imp. for sound

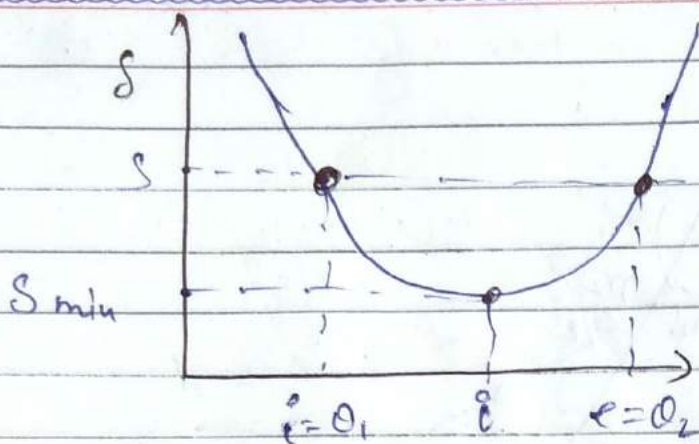
\* Condition for minimum Deviation:

for minimum deviation, angle of Incidence of a ray is equal to angle of reflection. Emergence.

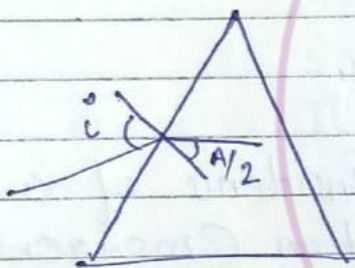
Due to Reversibility of light for a Particular deviation there are two angle of Incidence







Therefore for minimum deviation angle of Incidence is equal to angle of emergence.



$$\delta = i + e - (r_1 + r_2)$$

$$\delta_{\min} = 2i - (A) \quad \Rightarrow \quad i = \frac{\delta_{\min} + A}{2}$$

$$r_1 + r_2 = A \Rightarrow 2r = A$$

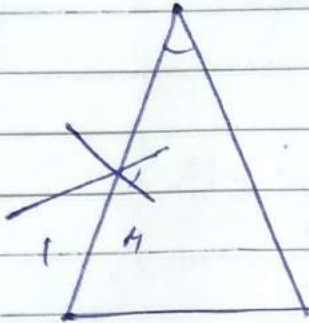
Snell's law

$$1 \sin i = \mu \sin (A/2)$$

$$\frac{\sin \left( \frac{\delta_{\min} + A}{2} \right)}{\sin (A/2)} = \mu$$

Note: If rays undergoes minimum deviation and the glass prism is isosceles or equilateral then refracted ray will pass parallel to Base.

\* Small Prism Angle: (for angle  $i$  to  $5^\circ$ )



$$\delta = A[\mu - 1]$$

$$\delta = i + e - A = i + e - (r_1 + r_2)$$

for small angle

$$i \sin i = \mu \sin r_1$$

$$i = \mu r_1$$

$$\sin e = \mu \sin r_2$$

$$e = \mu r_2$$

$$\delta = \mu(r_1 + r_2) - (r_1 + r_2)$$

$$\delta = A[\mu - 1]$$

~~Cauchy's formula~~

\* Cauchy's formula:

$$\mu = A + \frac{B}{\lambda} + \frac{C}{\lambda^2}$$

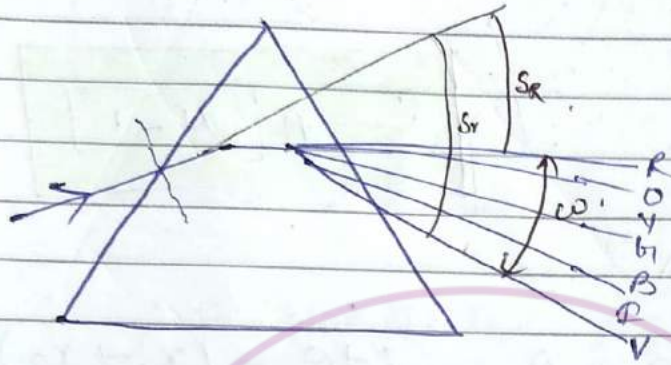
$$\mu \propto \frac{1}{\lambda}$$

$$\frac{V \text{ I B G Y O R}}{E \downarrow \quad \uparrow A}$$

$$\mu \uparrow \downarrow \mu \downarrow$$

for red colour  $\mu_r \propto \frac{1}{\lambda}$

small deviation.



### \* Dispersion:

Splitting of white light in seven colour is known as dispersion

$$D.A = \delta_v - \delta_r$$

$$= A[\mu_v - 1] - A[\mu_r - 1]$$

$$D.A = A[\mu_v - \mu_r]$$

### \* Dispensing power (w)

Ratio of Dispersion angle to that of mean deviation is known as Dispensing power

$$\text{Smean. } D.P = \frac{\mu_v - \mu_r}{2}$$

$$W = \frac{D \cdot A}{S_{\text{mean}}} = \frac{A[\mu_v - \mu_r]}{A[\mu_y - 1]}$$

$$\mu_y = \frac{\mu_v + \mu_r}{2}$$

\* Dispersion without deviation

$$s_1 + s_2 = 0$$

$$A_1(\mu_1 - 1) + A_2(\mu_2 - 1) = 0$$

$$\theta = \theta_1 + \theta_2$$

$$= A_1(\mu_{v1} - \mu_{r1}) + A_2(\mu_{v2} - \mu_{r2})$$

1046

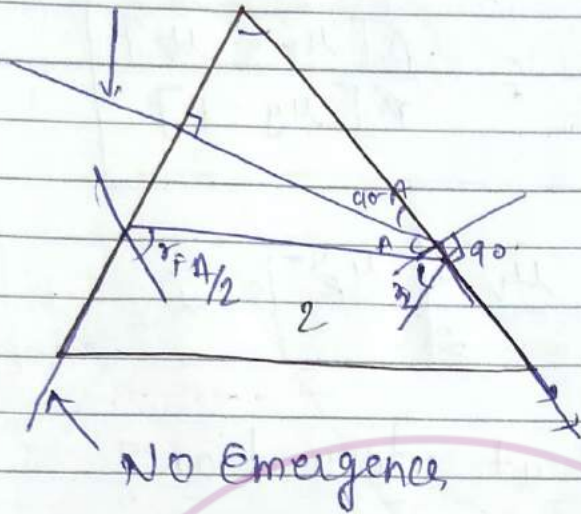
\* Deviation without Dispersion (Achromatic Combination)

$$\theta = \theta_1 + \theta_2$$

$$0 = A_1(\mu_{v1} - \mu_{r1}) + A_2(\mu_{v2} - \mu_{r2})$$

\* Condition for no emergence

All Emergence



No Emergence

Condition for all emergence!

$> 30^\circ$

$$\mu \sin A = 1 \sin 90^\circ$$

$$\sin A = \frac{1}{\mu}$$

$$A = \theta_c$$

No Emergence  $> 60^\circ$

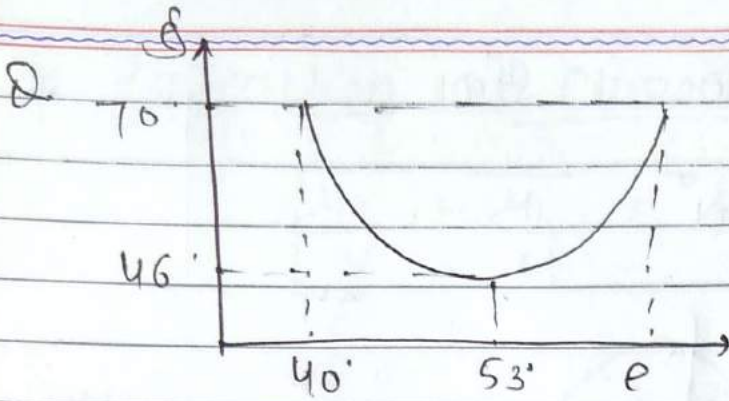
$$1 \sin(90) = \mu \sin \frac{A}{2}$$

$$\sin \theta_c = \sin \frac{A}{2}$$

$$\theta_c = \frac{A}{2}$$

$$A = 2\theta_c$$

$$D = i + e - A$$



find angle of prism emergent angle & refractive index for the given deviation vs incidence graph for the prism?

$$D = i + e - A$$

$$46 = 53 + 53 - A$$

$$A = 60$$

$$70 = 40 + e - 60$$

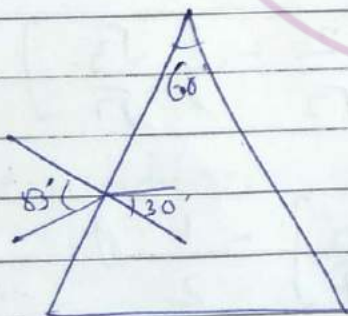
$$90 = e$$

$$A = 60 = i_1 + i_2 \quad i_1 = i_2 = 30 \text{ (for mini-deviation)}$$

$$\sin 53 = \mu \sin 30$$

$$\mu = \frac{4}{3}$$

$$\frac{4}{3} = \mu$$

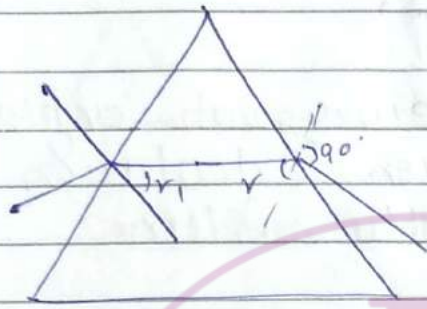


Q. for a prism  $A = 60^\circ$ , refractive index  $\mu = \frac{4}{3}$ . find the minimum possible

angle of incidence so, that the second surface of deviation?

$$\frac{\sqrt{7}}{3} \times \sin 30^\circ = 1 \sin \lambda$$

$$\frac{\sqrt{7}}{6} = \sin \lambda$$



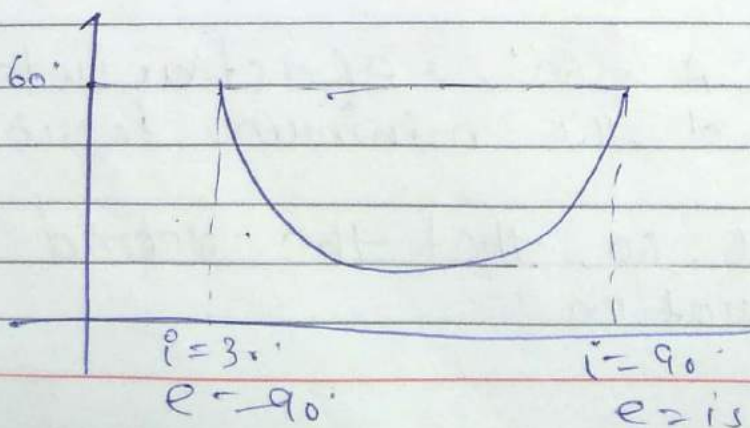
$$\frac{\sqrt{7}}{3} \sin \lambda = 1$$

$$\sin \lambda = \frac{\sqrt{3}}{\sqrt{7}}$$

$$1 \sin \lambda = \frac{\sqrt{7}}{\sqrt{3}} \left[ \frac{\sqrt{3}}{2} \cos \lambda - \frac{1}{2} \frac{\sqrt{3}}{\sqrt{7}} \right]$$

$$= \frac{\sqrt{7}}{\sqrt{3}} \left[ \frac{\sqrt{3}}{2} \frac{2}{\sqrt{7}} - \frac{1}{2} \frac{\sqrt{3}}{\sqrt{7}} \right]$$

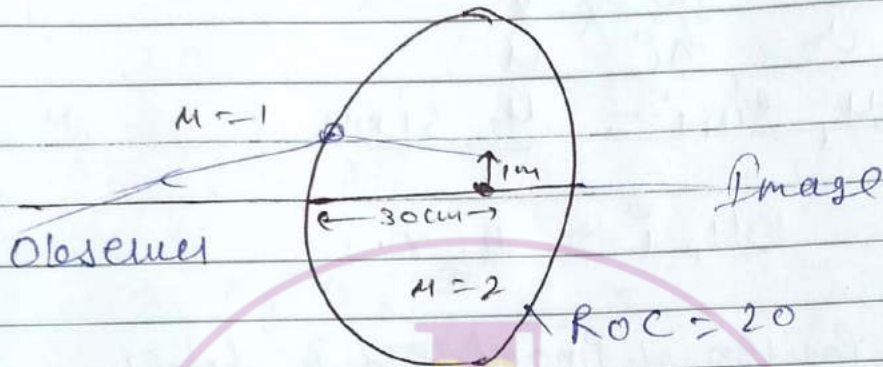
$$= \frac{\sqrt{7}}{\sqrt{3}} \left[ \frac{1}{2} \frac{\sqrt{3}}{\sqrt{7}} \right] = \frac{1}{2} A$$



\* Refraction at curved surface :

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

Q. No.



Find Position of Image.

$$\frac{1}{v} + \frac{2}{30} = \frac{1}{-20}$$

$$\frac{1}{v} = \frac{1}{-20} - \frac{2}{30} = \frac{1}{-60}$$

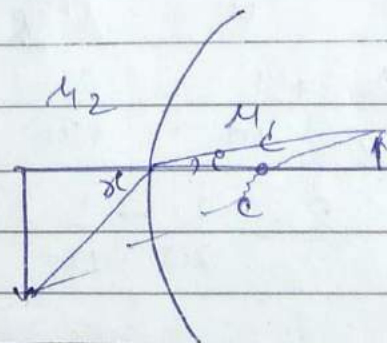
$$v = -60$$

\* Magnification Produced due to refraction :

$$m = \frac{\mu_1 v}{\mu_2 u}$$

Derivation

$$m = \frac{\mu_1 v}{\mu_2 u} \times \frac{h_i}{h_i} = \frac{\mu_1 v}{\mu_2 u} \times \frac{h_i}{h_o}$$



$$m = \frac{h_i}{h_o} = \frac{1}{\mu} \times \frac{v}{u} = \frac{\mu_1 v}{\mu_2 u}$$



$$\tan i^{\circ} = \frac{h_o}{u} \quad (i)$$

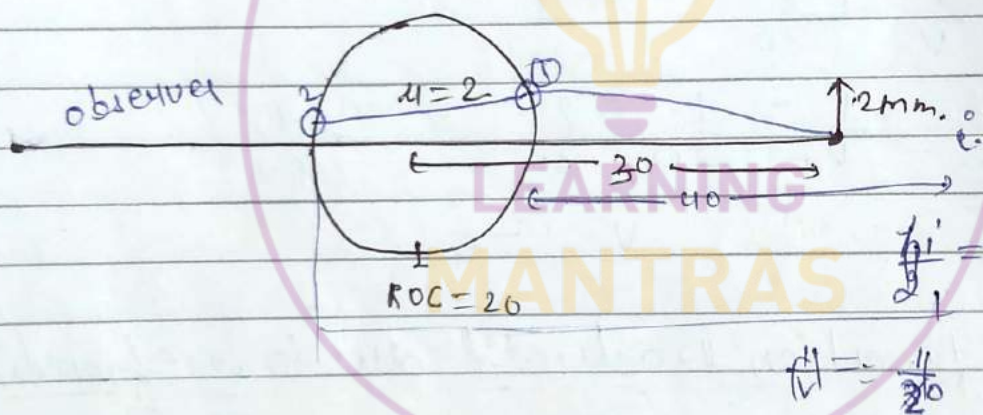
$$\tan r = \frac{h_i}{v} \quad (ii)$$

$$\frac{i}{r} = \frac{h_o}{h_i} \times \frac{v}{u}$$

$$\mu_1 \sin i = \mu_2 \sin r$$

$$\mu_1 i = \mu_2 r$$

Q. Find final position of image and its height.



(i)

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{2}{v} + \frac{1}{10} = \frac{2-1}{+20}$$

$$\frac{2}{v} = \frac{1}{20} - \frac{1}{10} \Rightarrow v = -40$$

(ii)

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{1}{v} + \frac{2}{80} = \frac{1-2}{-20}$$

$$v = 40$$

$$M_1 = \frac{v}{u} \frac{M_1}{u}$$

$$= \frac{+40}{2} \times \frac{1}{+10} = +2$$

$$M_2 = \frac{v}{u} \frac{M_1}{u}$$

$$= \frac{+40}{1} \times \frac{-2}{-80} = -1$$

$$\frac{40}{1} \times \frac{-2}{-80} = -1$$

$$m_{\text{net}} = m_1 \times m_2$$

$$= 2 \times -1 = -2$$

$$\frac{h_i}{h_o} = -2$$

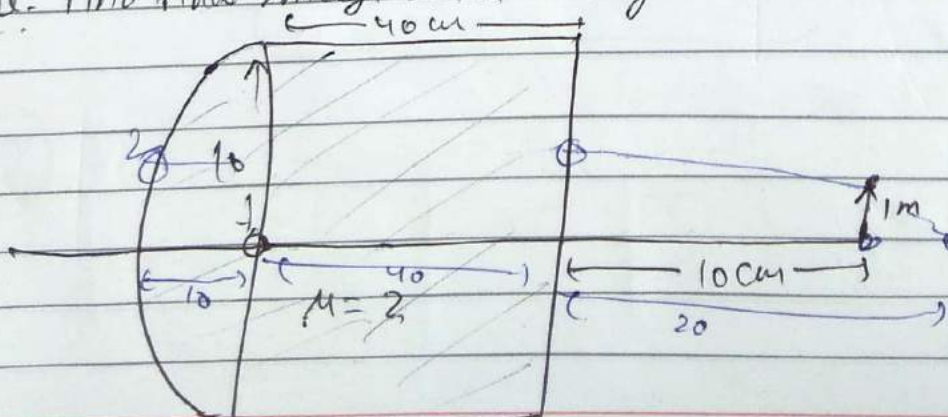
$$h_o$$

$$h_i = -2 \times 2 \Rightarrow h_i = 4$$

Final

Image: Enlarge, Real, Inverted.

Que: Find final Image and its height



$$\frac{2}{v} = \frac{1}{10} = \frac{2-1}{10}$$

$$\frac{2}{v} = \frac{1}{10} + \frac{1}{10}$$

$$\frac{2}{v} = \frac{2}{10}$$

$$v = 10$$

$$\textcircled{1} \rightarrow \frac{M_2}{V} = \frac{M_1}{u}$$

$$\frac{2}{V} = \frac{1}{(-10)}$$

$$V = -20$$

(9)

$$\frac{M_2}{V} - \frac{M_1}{u} = \frac{M_2 - M_1}{R}$$

$$\frac{1}{V} - \frac{2}{(-70)} = \frac{1-2}{-10}$$

$$\frac{1}{V} + \frac{2}{70} = \frac{+1}{+10}$$

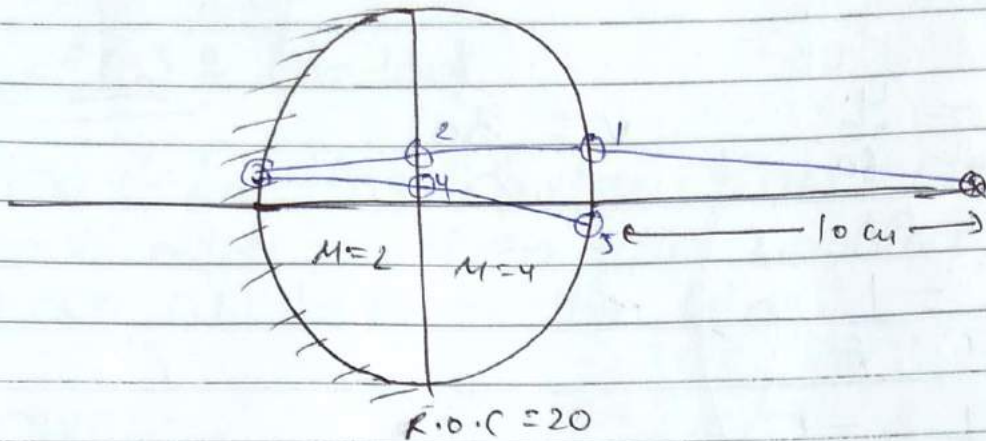
$$\frac{1}{V} = \frac{1}{10} - \frac{2}{70} = \frac{7-2}{70} = \frac{5}{70} = \frac{1}{14}$$

$$V = 14.$$

$$m = \frac{V}{M_2} \times \frac{M_1}{u}$$

$$m = \frac{14}{2} \times \frac{1}{10}$$

2u



① →

$$\frac{M_2}{v} - \frac{M_1}{u} = \frac{M_2 - M_1}{R}$$

$$\frac{4}{v} - \frac{1}{30} = \frac{4-1}{20}$$

$$\frac{4}{v} = \frac{3}{20} + \frac{1}{30}$$

$$= \frac{3+2}{20} = \frac{5}{20}$$

$v =$  **LEARNING MANTRAS**

$$\frac{4}{v} + \frac{1}{10} = \frac{4-1}{20}$$

$$\frac{4}{v} = \frac{3}{20} + \frac{1}{10}$$

$$\frac{4}{v} = \frac{3+2}{20} = \frac{5}{20}$$

$$\frac{4}{v} = \frac{3+2}{20} = \frac{5}{20}$$

$$v = 80$$

②

$$\textcircled{2} \quad \frac{u_2}{v} = \frac{u_1}{u}$$

$$\frac{2}{v} = \frac{4}{60}$$

$$v = 30$$

$$\textcircled{3} \quad \frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{10} = -\frac{1}{10}$$

$$v = -5$$

$$\textcircled{4} \quad \frac{u_2}{v} = \frac{u_1}{u}$$

$$\frac{2}{v} = \frac{4}{60}$$

$$v = 30$$

$\textcircled{5}$

$$\frac{u_2}{v} = \frac{u_1}{u} = \frac{u_2 - u_1}{R}$$

$$\frac{1}{v} + \frac{4}{50} = \frac{1-4}{-20} \quad v =$$

$$\frac{1}{v} = \frac{+3}{+20} - \frac{-4}{50}$$

Important for Board.

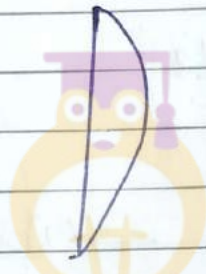
## Lens (Thin Lens)

Two Refracting Surfaces placed close to each other then the combination is known as lens or thin lens.

### Convex:



Bi-convex



Plano-convex

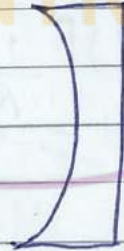


Concavo  
convex

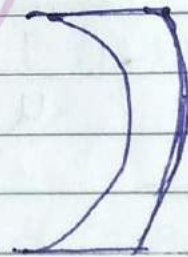
### Concave:



Bi-concave



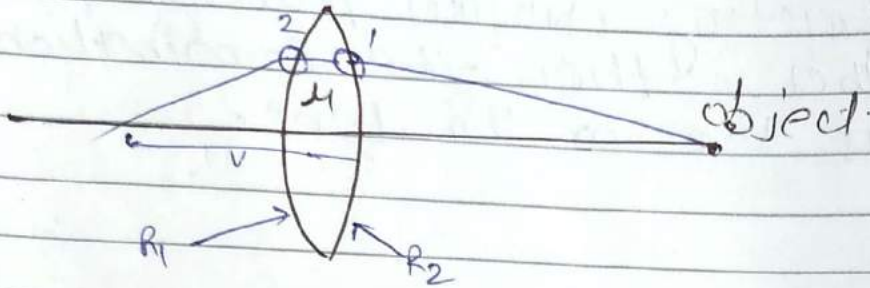
Plano-concave



Convexo  
concave.

Imp for Board

# Lens Maker Formula!



$$f = \frac{M_1}{M_2}$$

$$(1) \quad \frac{\mu + 1}{v_1 \cdot (-u)} = \frac{\mu_2 - \mu_1}{+R_1}$$

$$\frac{\mu}{v_1} + \frac{1}{u} = \frac{\mu - 1}{+R_1} \quad (1)$$

$$(2) \quad \frac{1}{v} - \frac{\mu}{v_1} = \frac{1 - \mu}{-R_2} \quad (2) \quad \text{divide (1) and (2)}$$

$$\boxed{\frac{1}{v} + \frac{1}{u} = (\mu - 1) \left[ \frac{1}{R_1} + \frac{1}{R_2} \right]}$$

only convex Important  
No sign change

To make it nature free Again we use sign

$$\frac{1}{v} - \frac{1}{u} = (\mu - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\Rightarrow \boxed{\frac{1}{v} - \frac{1}{u} = \frac{1}{f_L}}$$

$$\boxed{\frac{1}{f_L} = \left[ \frac{\mu_L - 1}{\mu_S} \right] \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]}$$

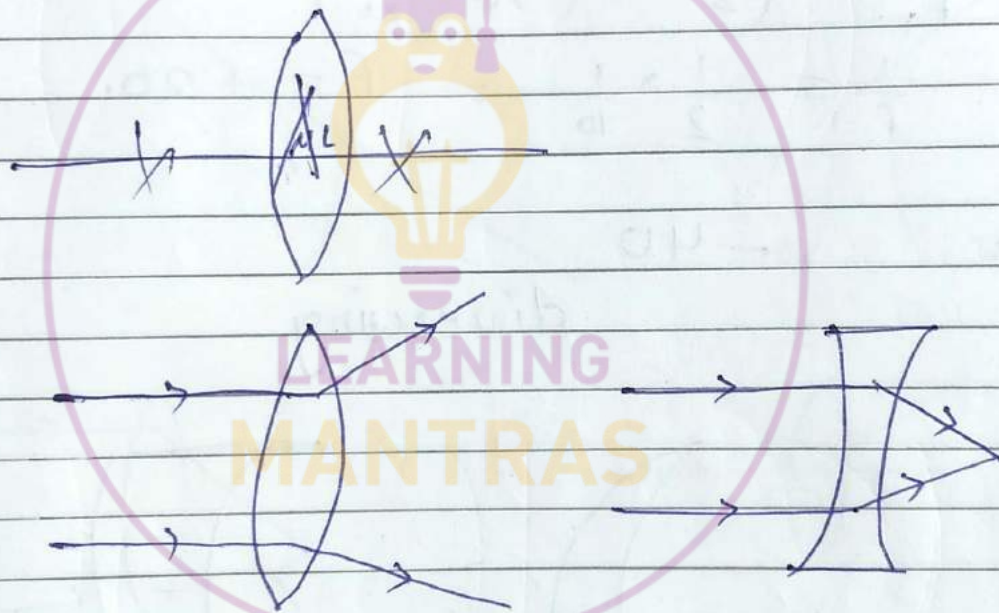
$$TLR = \frac{0-1}{s-1}$$

focal length . + Convex Converging  
(-) Concave Diverging.

1) Focal length of a lens is independent from the direction of incidence Ray.

2) If Refractive Index of surrounding medium is amp greater than Refractive Index of Lens. Lens changes its nature.

Converging becomes Diverging  
Diverging " Converging



Bi Convex

Q. lens having refractive index of material is  $\frac{3}{2}$  of radius of curvature is 20 find its focal length

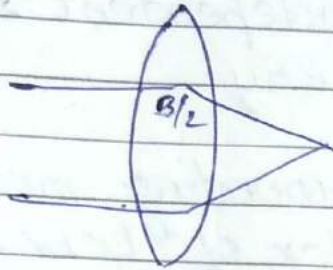
2) A lense is placed in Surrounding medium of Refractive index & find its focal length.



focal length

no. - concave  
no. + convex

Ans!



focal length

(-)  $\Rightarrow$  diverging  
Concave

$$\frac{1}{f} = (n - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$\frac{1}{f} = \left( \frac{3}{2} - 1 \right) \left( \frac{1}{20} + \frac{1}{20} \right)$$

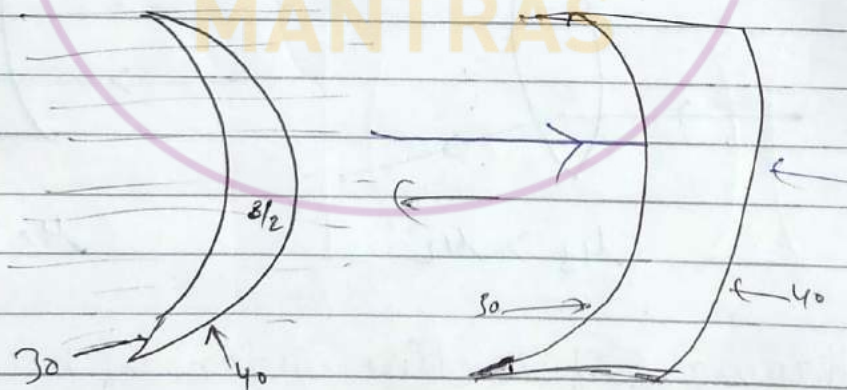
$$\frac{1}{f} = \frac{1}{2} \times \frac{1}{10} \Rightarrow f = +20.$$

(11)  $\Rightarrow$

-40

diverging

Ques!



- i) Determine the sign name the
- ii) find f.l if ray is incident from right
- iii) from left lens placed in air

right

$$\frac{1}{f_l} = \left( \frac{3}{2} - 1 \right) \left( \frac{1}{40} - \frac{1}{30} \right) =$$

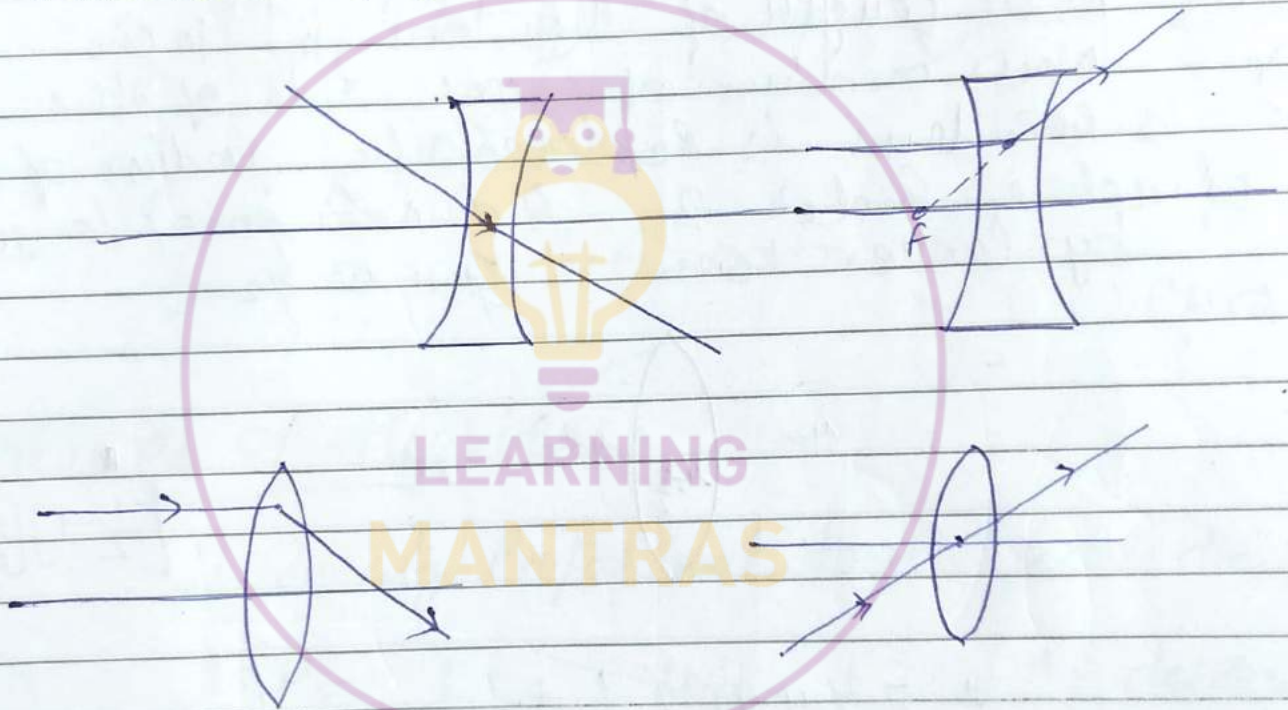
$$\frac{1}{f_l} = \frac{1}{2} \times \frac{3-4}{120} = \frac{1}{2} \times \frac{-1}{120} \Rightarrow \underline{\underline{f = -240}}$$

Note: focal length of a lens does not depend on ray =

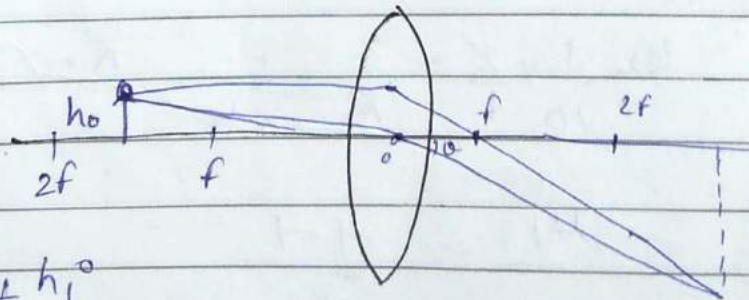
## x Magnification of Lense

### Ray Tracing

Light ray passing from optical centre will pass undeviated ~~into~~ the lens.



### Magnification:



$$\frac{+h_o}{+u} = \frac{+h_i}{+v}$$

$$\frac{v}{u} = \frac{h_i}{h_o} = m_T$$

$$A + B = C$$

$$\frac{-B}{A} = \text{magnification}$$

Convex

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$m = - \left[ \frac{-1/4}{1/10} \right]$$

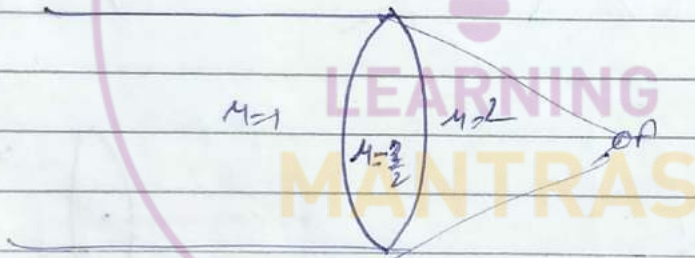
Note.

To find focal length of any system light is incident on a system at an angle of parallel to principle axis.

Ques! focal length of thin lens in Air is 10 cm

Ans! New medium of one side of the lens is replaced by medium of refractive index 2 find new focal length by convex lens.  $\mu = 3/2$

Ans!



$$\left[ \frac{1}{2} - 1 \right] \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = (\mu - 1) \left( \frac{1}{R} + \frac{1}{R} \right) \quad P$$

$$\frac{1}{10} = \left( \frac{3}{2} - 1 \right) \left( \frac{2}{R} \right)$$

$$\frac{1}{10} \times \frac{2}{1} = \frac{2}{R} \quad \Rightarrow \quad R = 10$$

$$\frac{\mu_2}{v} - \frac{\mu_1}{\infty} = \frac{\mu - 1}{R}$$

$$\frac{2}{f} - \frac{\mu}{\infty} = \frac{2 - \mu}{-R}$$

focal length  $\infty$  = sun glass

$$\frac{2}{f} = \frac{M}{R} - \frac{1}{R} - \frac{2}{R} + \frac{M}{R}$$

$$\frac{1}{f} = 0$$

$$\frac{2}{f} = \frac{M-1-2+M}{R}$$

$$\frac{2}{f} = \frac{2M-3}{R}$$

$$\frac{2}{f} = \frac{1}{R} (2M-3)$$

$$\frac{2}{f} = \frac{1}{R} (2 \times \frac{3}{2} - 3)$$

$$\frac{2}{f} = \frac{1}{R} (0)$$

$$\frac{2}{f} = 0$$

$$f = \infty$$

$$\begin{matrix} f = \infty \\ p = 0 \end{matrix}$$

\* Power of the lens

is inversely proportional to its focal length

$$P \propto \frac{1}{f}$$

$$P = \frac{1}{f}$$

$$\text{unit} \Rightarrow \frac{1}{m} = m^{-1} = \text{dioptre}$$

$\Rightarrow$  Dioptre



Learning Mantras

Our Guidance, Your Success