

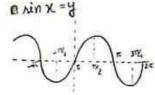


Maths Formulas Book

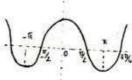


Trigonometry

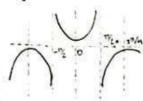
Graphs:



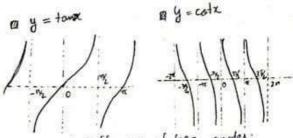
ay = cosx



ay = nec x



By = cosec x



@ Sum and Difference of two angles:

$$B \sin (A - B) = \sin A \cos B - \cos A \sin B$$

 $B \cos (A + B) = \cos A \cos B - \sin A \sin B$
 $B \cos (A + B) = \cos A \cos B + \sin A \sin B$

$$a \cos(A+B) = \cos A \cos B + \sin A \sin B$$

 $a \cos(A-B) = \cos A \cos B + \sin A \sin B$
 $a \cos(A-B) = \cos A \cos B + \sin A \sin B$

$$a + an (A \pm B) = \frac{+ an A \pm tan B}{1 \mp tan A + an B}$$

$$\mathbf{B} \cot (\mathbf{A} \pm \mathbf{B}) = \frac{\cot \mathbf{A} \cot \mathbf{B} \mp \mathbf{I}}{\cot \mathbf{A} + \cot \mathbf{B}}$$

a
$$2 \text{ min } A \text{ sin } B = \text{min } (A + B) + \text{min } (A - B)$$

$$= 2 \text{min } A \text{ sin } B = \text{min } (A + B) - \text{min } (A - B)$$

a
$$2 \text{ Ain} A \text{ Ain} B = \text{Ain} (A+B) + \text{Ain} (A-B)$$

B $2 \text{ cos} A \text{ Ain} B = \text{Ain} (A+B) + \text{cos} (A-B)$
A $2 \text{ cos} (A+B) + \text{cos} (A+B) + \text{cos} (A+B)$

$$g$$
 2 cos Anin B = $Ain (A+B)$ - $Ain (A-B)$
 g 2 cos Acos B = $Ain (A+B)$ - $Ain (A+B)$
 g 2 $Ain A$ $Ain B$ = $Ain (A-B)$ - $Ain (A+B)$

$$g = 2 \sin A \sin B = \cos (A - B) - \cos (A - B)$$

Multiple angles

Multiple angles
$$\alpha \sin 2A = 2 \sin A \cos A = \frac{2 \tan A}{1 + \tan^2 A}$$

o Sam or difference into product. a sin (+ sin) = 2 sin ((+0) cos ((-0))

a sin (+ sin D = 2 sin (
$$\frac{C-D}{2}$$
) cos ($\frac{C+D}{2}$)
a sin C - sin D = 2 sin ($\frac{C-D}{2}$) cos ($\frac{C-D}{2}$)

a cas
$$2A = \cos^2 A - \sin^2 A = 1 - 2\sin^2 A$$

$$A cos C + cos D = 2 cos (\frac{C+D}{2}) cos (\frac{C-D}{2})$$

$$A cos C - cos D = 2 nin (\frac{C+D}{2}) nin (\frac{D-C}{2})$$

A
$$COSC - COSD = 2 Ain (\frac{CSD}{2}) Ain (\frac{CSD}{2})$$

Special Truis: a $COSA COS (60-A) COS (60+A) = \frac{COS}{4}$

Special Truis: a $COSA COS (60-A) COS (60+A) = \frac{COS}{4}$

a tan 2A =
$$\frac{2+\alpha A}{1-+\alpha n^{1}A}$$
 a tan A tan (60-A) $\frac{2}{4}$ (60+A) = $\frac{2+\alpha A}{4}$ a tan A tan (60-A) $\frac{2}{4}$ tan $\frac{2}{4}$

$$\begin{array}{lll}
\mathbf{a} & \tan 2\mathbf{A} &= \frac{2 \tan A}{1 - \tan 1 \mathbf{A}} & \mathbf{a} & \sin \mathbf{A} & \sin (60 - \mathbf{A}) & \sin (60 - \mathbf{A}) & \sin (60 - \mathbf{A}) & - \frac{4}{1 - \tan 3\mathbf{A}} \\
\mathbf{a} & \tan \mathbf{A} & + \frac{60 - \mathbf{A}}{1 - \tan (60 - \mathbf{A})} & - \frac{4}{1 - \tan 3\mathbf{A}} & - \frac{4}{$$

Btan 3A =
$$\frac{3\tan A - \tan^3 A}{1 - 3\tan^2 A}$$

Btan 3A = $\frac{3\tan A - \tan^3 A}{1 - 3\tan^2 A}$

Conditional Identities (A+B+C=U)

Btan 2A = $\frac{1 - \cos^2 A}{1 + \cos^2 A}$

Btan 3A + $\tan B$ + $\tan B$ + $\tan B$ = $\tan A + \tan B$ to C

Btan 2A + $\tan B$ + a + a

a cat
$$3A = \frac{\cot^3 A - 3\cot A}{3\cot^2 A - 1}$$

• GP of Angles

$$A \stackrel{\text{Ain}}{A} + A \stackrel{\text{Ain}}{A} \stackrel{\text{Ain}}{A} = \frac{A \text{Ain} 2^{\text{MA}}}{A \text{Ain} 2^{\text{MA}}} \quad 0 \quad A + B + C = \frac{12}{2}$$

a nec A + nec B + nec C 2 6 [Acute] a care A + case (& + costs), 6 &

00 tan 34 -tan 24 - tan 4 = tan 3 A tan 2 A tan A

Progression & Series

- Anithemic Progression a, a+d, a+2d,, a+(n-v)d nth term (General term): tn = a+(n-v)d, tn = l-(n-v)d
- 0 3 terms in AP consideration a-d, a, a+d 0 4 terms in A.P. a-3d, a-d, a+d, a+3d
- 9f a, a, a, a, an-1, an are in A.P., a, + an = a, + an-1 = a, + an-1 = = a, + an-1
- © Sum of n terms in an AP: $S_n = \frac{n}{2} [2a + (n-1)d] = \frac{n}{2} [a+1]$ © Of $S_n = an^2 + bn + e$, $t_n = S_n S_{n-1}$
- Anithmotic mean: AM $(x_1, x_2) = \frac{x_1 + x_2}{2}$, AM $(x_1, x_2, x_3, ..., x_N) = \frac{x_1 + x_2 + x_3 + + x_N}{N}$
- $\bullet A_1 + A_2 + \dots + A_n = n\left(\frac{a+b}{2}\right)$
- · Geometric Progression a, ar, ar, ar, and onth term (General term): tn = arn-1
- Sum of n terms: $S_n = \frac{a(1-r^n)}{1-r} \left(1>r\right] = \frac{a(r^n-1)}{r-1} \left[r>1\right] = \frac{g_f \times_1, \times_2 \times_3 -...}{are in GP, log \times_1, log \times_2}$
- @ 3 tours in GP: $\frac{a}{r}$, a, ar @ 4 tours in GP: $\frac{a}{r^3}$, $\frac{a}{r}$, ar, ar³ @ Sum of Infinite GP. $S_{\infty} = \frac{a}{1-r}$ [|r|<1]
- @ Greametric means: GM (x1, x2) = (x, x2)/2, GM (x1, x2, x2,, x4) = (x, x2 x3 -.... x4)/n
- 0 G,G2G3 Gn = (Tab)"
- Harmonic progression: a,, az, az ---- are in H.P. if la,, \(\frac{1}{az}, \frac{1}{az}, \) are in AP.
- @ nth term (General term): $t_n = \frac{1}{t_n \circ f AP}$ @ Harmonic Mean: $HM(x_1, x_2) = \frac{2x_1x_2}{x_1 + x_2}$, $HM(x_1, x_2 x_1) = \frac{N}{t_1 + t_2 + \cdots + t_n}$
- @ Inequalities: A & G & H & G = AH
- Special series: $\Sigma n = \frac{n(n+1)}{2}$, $\Sigma n^2 = \frac{n(n+1)(2n+1)}{6}$, $\Sigma n^3 = \frac{n^2(n+1)^2}{4}$
- @ Anithmetico Geometric Progression (AGP):-S=a+ (a+d)r+ (a+2d)r2+---

$$S = a + (a+d)r + (a+2d)r^2 + ---$$

$$-rS = ar + (a+d)r^2 + ---$$

$$S(i-r) = a + d(r+r^2 + ----)$$

- Difference Series: $5 = 1+2+4+7+11+16+-----+t_0$ $5 = 1+2+4+7+11+----+t_0$ $0 = 1+(1+2+3+-----)-t_0$
- $\sum_{r=1}^{n} \frac{1}{r(r+1)(r+2)(r+3)} = \sum_{r=1}^{\infty} \frac{1}{3} \left[\frac{(r+3)-r}{r(r+1)(r+2)(r+3)} \right] \otimes \sum_{r=1}^{\infty} r(r+1)(r+2)(r+3) = \sum_{r=1}^{\infty} \frac{1}{5} \left(\frac{(r+4)-(r-1)}{5} \left(\frac{(r+4)-(r-1)}{5} \left(\frac{(r+3)-r}{(r+2)(r+3)} \right) \right) \right]$
- Cleighted mean: $a_1^m + a_2^m + \cdots + a_n^m > \left(\frac{a_1 + a_2 + a_3 + \cdots + a_n}{n}\right)^m$ of m < 0 or m > 2
 - 1 a, m + a, m + . . . + a, m < (a, + a, + . . . + an) m 9 f o < m (1

- 10 let p be a given prime and n, any positive integer. Then the maximum power of p present in n! is $\left[\begin{array}{c} n \\ p \end{array}\right] + \left[\begin{array}{c} n \\ p \end{array}\right] + \left[\begin{array}{c} n \\ p \end{array}\right] + \cdots$ (9hor [.] -> Greatest Integer function orxr!="Pr • Number of permutations of n different things taken r at a time $\rightarrow {}^{n}P_{r} = \frac{n_{l}}{(n-r)!}$ · Number of permutations of n different things taken all at a time - n! © Number of permutation of n things [pare aller, or are alie, r are alies] → n!

 © Number of combinations (selections) of n different things taking r at a time → nCr = r!(n-r)! OBTC = "Cn-r B"Cr+"Cr-1 = "+'Cr , & r. "Cr = n "-'Cr-1 & "Cr = "-'Cr-1 & "Cr = "-r+1 Tr = "-Cr-1 & "Cr = "-r+1 Tr = "-Cr-1 & "Cr-1 & " © When n is even, max value of "Cr → "Cn/2 or "Cn-1 cincular manner → (n-1)! cincular manner → (n-1)!

 © When n is odd, max value of "Cr → "Cn-1 or "Cn-1 cincular manner → (n-1)!

 © When ACW/CW doesn't matter (e.g. nechlace, gardard), a cincular arrangement → (n-1)! Total no of relections of a things, of primiles, or similes, ralike] - (including 0) → (P+1)(4+1)(r+1) @ 95 N = $P_1 \times P_2 \times P_3 \times P_4 \times P_5 \times \dots$ where a, b, C_1 are asso nongetonegative integers, $P_1, P_2, P_3 \times \dots \times P_n \times P_$ Then $\rightarrow \otimes$ Total No of Divisors = $(a+1)(b+1)(c+1)-\dots$ B Sum of all divisors = $(\frac{p_1^{a+1}-1}{p_1-1})\times(\frac{p_2^{b+1}-1}{p_2-1})\times(\frac{p_3^{b+1}-1}{p_3-1})$ BINO of usays of writing N as a product of test natural nos - [= (a+1)(b+1)(c+1)-...] if Nisrit a perfect and is a perfect square if a, b.c. all are even [-\frac{1}{2}(a+1)(b+1)(c+1) \dots +1] if N is a perfect

 and is a perfect square if a, b.c. all are even [-\frac{1}{2}(a+1)(b+1)(c+1) \dots +1] if N is a perfect. ON is a ported whe if 0, b, c -- all are multiples of 3. N = 2^a x3^b x5^cx
 e If N is odd, a = 0, b,c,d ≥ 0 e If N is even, a ≥ 1, b,c,...... ≥ 0 Sum of all n-digit numbers formed using n digits = (n-1)! (Sum of all n digits) × (111......1)

 n+imes

 n/2-21 • No of diagonals of n sided polygon $-1^{n}C_{2}-n=\frac{n(n-3)}{n-1}$. (Sum of notions) ntimes on of squares of in two system of perpendicular parallel lines (Cohen 1st set contains m lines and 2nd set contains n lines) is equal to $-\sum_{r=1}^{\infty} (m-r)(n-r)$; (m<n)
- @ Deavrangements: No of ways so that no letter goes to the correct address. Dn = 10! [1-11+21-11+41 ----+(-1) 1-11]

```
Complex Number
@ Z= X+iy, X, y∈R and i=J-1 = Re(Z)=X, Im(Z)=y = 150.
The property Taste = Sab is valid only if at least one of $10 and b is non negative, if
   a and b are both negative, then Ja 16 = - Jiall b)
    0 a+ib>c+id is meaningful only if b=d=0 0 If a+ib=c+id, a=c, b=d

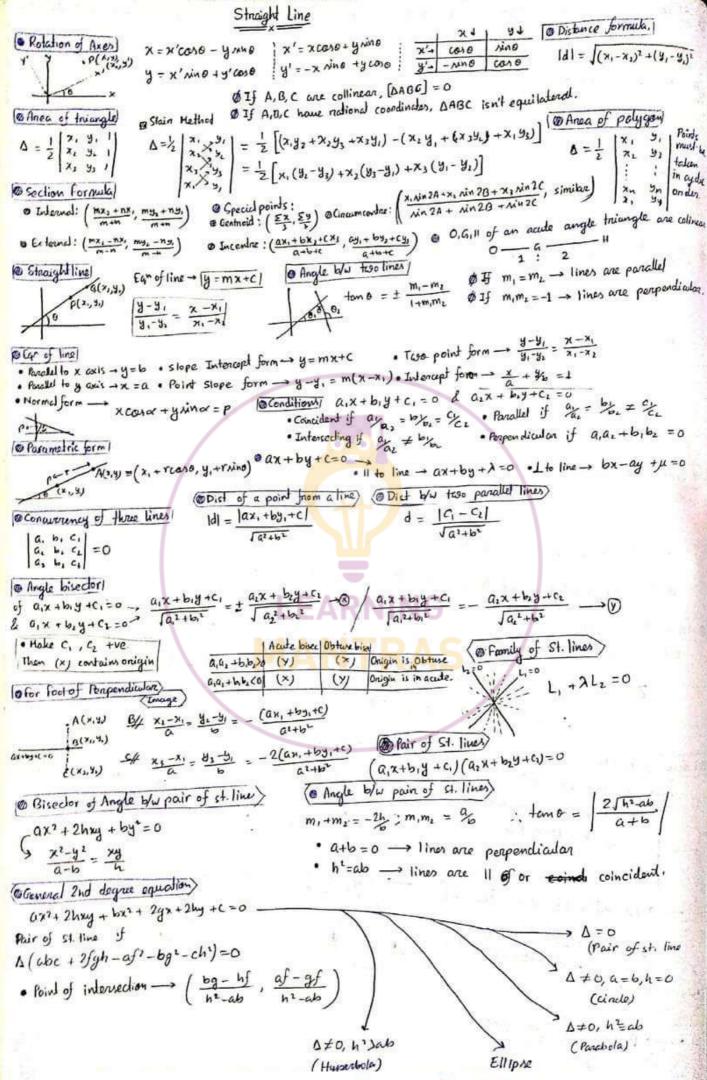
    In new no system, a²+b²=0, a=b=0. Rut ₹,²+₹,²=0 daes Not mean Z,=₹,=0.

0 \ i = \int_{-1}^{-1} , \ i^2 = -1, \ i^3 = -i , \ i^4 = 1 \ ; \ i^{4n+2} = i , \ i^{4n+2} = -1, \ i^{4n+3} = -i , \ i^{4n} = 1
D Square Root of a Complex No! Ja+ib = x+iy = a = x2-y2; 2my=b solve.
                                      Sign of b decides whether x and y are of same sign or opposite sign,
                                         Argument/amplitude of (N, 0 = tan-1 ( 1/2) = tan-1 (2)
Modulus of CN3 121 = r = Jx2+y2 10 Amplitude of CN1
                                           1 from the neal axis. any (2) \in [-\pi, \pi]
            p(2)= X+iy
Principle Angument
                                                                  ■ Quel = (x(0, y(0))
    @ Quad I/ (x>0, y>0) @ Qud I/ (x(0, y)0)
                                                                         x 00 arg(2)=0
                                             arg (2) = 0
              arg(2) = ox
               = tam-1 1/2
                                              = TE - tam-1 3/x
                                                                            -I = tom-1/2/-T
1 Polan form | 

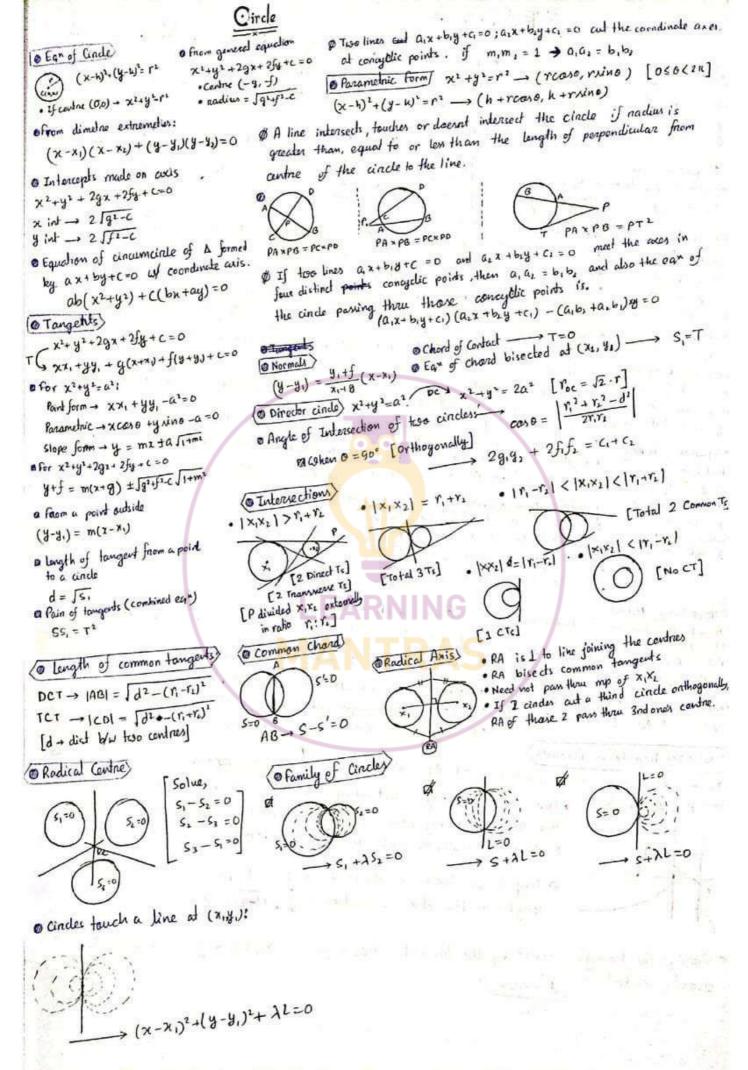
∅ Z = x+iy = r(coso + i rino) | © Eulers form | Z = r(coso + i rino) = reio
                                                                        : e io = coso + i sino
                              1 Poperties of Conjugates
                                \#(\overline{z}) = \overline{z} + \text{if } \overline{z} = \overline{z}, \overline{z} \text{ is purely need } \# \overline{z}, \overline{z}_{2} = \overline{z}_{1} \cdot \overline{z}_{2}
© Conjugate of a CN:
      P(2) Z = X+iy
                                                                           # Z," = (2)" # (21/21) = 21/2
                               # Z+Z=0, Z is purely imaginary
               = x-i4
                               # 2 = 22 # 2, +2, = 2, +2,
                                                                                     @ Angle b/w line joining
                                          @ Properties of Arguments
 2+2 = 2 Re(2)
                                                                                       E, and E, & Zs, Z4
 2-ē = 2 Im(ē)
                                      # org (2,2) = boarg (2,) + org (2)
                                       # arg ( 2, 22 -.. 24) = arg (21) + -... + bag (24)
@Properties of modulus
(40 \# |\mathcal{E}| = 0 \Rightarrow \mathcal{E} = 0 = \operatorname{Im}(\mathcal{E}) = \operatorname{Re}(\mathcal{E}) \# \operatorname{arg}\left(\frac{\mathcal{E}_1}{\mathcal{E}_1}\right) = \operatorname{targ}\left(\mathcal{E}_1\right) - \operatorname{targ}\operatorname{arg}\left(\mathcal{E}_1\right)
                                      H any (=) =- any (2)
# |2|=|2|=|-2|=|-2|
                                                                                    6 = \arg\left(\frac{z_4 - z_3}{z_1 - z_1}\right)
                                      # arg (2") = n arg (2)
# - 121 & RO (21 5 121
                                      # arg (=) = - trig (2)
H-121 & Im (21 & 121
                                                                              @ If Z, Z, and Z, are vertices
                                      # If z is purely imaginary.
# 2.2 = | 212 + |2" = |2"
                                                                                of an equilateral triangle. Then
                                                   arg(z) = ± 1/2
H | Z, Z2 ---- |Zn | = |Z1 | |Z2 | ---- |Zn |
                                                                               7-3+ --3+ --3=0
                                     + of z is purely neal,
# (21) = (21)
                                                 ang (2) = 0/11
H |Z1+242 = (212+1212+212(2122)
                                              @ Angle b/w 2 lines
H | Z1 - Z1 2 = | Z12+ (Z12 - 2Re(Z1Z2)
                                                                            2,2+2,2+232=2,22+2223+2371
# 12,+212+12,-212= 2(12,12+12,12)
                                                                           @ Square Root of 2=a+ib are
# |Z, - Zd -> dict b/w Z, & Zz
                                                 \alpha - \beta = avg \left( \frac{z_3 - z_1}{z_2 - z_1} \right)
# 12, + 21 5 | 2, 1 + 1221
# |2,+22+...+2n| \le |2,1+ |221+...+ |2n|
# 12,+22//21-121
```

10 At 21, 21, 21 are medican of an isoscalar night angled triangle, by right angle at 2 s. The (2, - 20) = 2(2, - 22)(2, -2) O De Howard Theorem) $(\cos \alpha + i \sin \alpha)^n = (re^{i\alpha})^n = r^n (e^{in\alpha}) = (\cos (n\alpha) + i \sin (n\alpha))$ $0 (\cos - i \sin s)^n = \cos ns - i \sin ns$ $0 = \frac{1}{\cos - i \sin s} = (\cos s - i \sin s)^{-1} = \cos s - i \sin s$ B (time + icone) + time + icone = (cone, - i rine) + come, - inino) $\mathbf{B} \left(\text{Ning} + i \cos \theta \right)^n = \left[\cos (x - \theta) + i \sin (x - \theta) \right]^n = \left[\cos n(x - \theta) + i \sin (x - \theta) \right]$ a Cube Poots of Uniting $Z=1^{i_1}=1$, ω , ω^2 where $\omega=-\frac{1}{2}-i\sqrt{3}$, $\omega^2=-\frac{1}{2}-i\sqrt{3}$ $\omega=e^{i2\sqrt{3}}$, $\omega=-\frac{1}{2}e^{-i2\sqrt{3}}$ m sum of roots is 0; 1 + w + w2 = 0 m Phoduct of roots 1; 1.w. w2=1 11 1 - 15 - 152" = {3, nis a multiple of 3} as a control of an equilatoral triangle on Angand Plane of an equilatoral triangle on Angand Plane Section formula 2. Internally, $Z_3 = \frac{m Z_2 - n Z_1}{m - n}$ Externally, $Z_3 = \frac{m Z_2 - n Z_1}{m - n}$ © current of A formed by Z., Zz and Z3 → Z,+Zz+Z3 e of cincumcentus of an Δ is origin, then orthocenture \rightarrow $z_1+z_2+z_3$ h rest of writy |

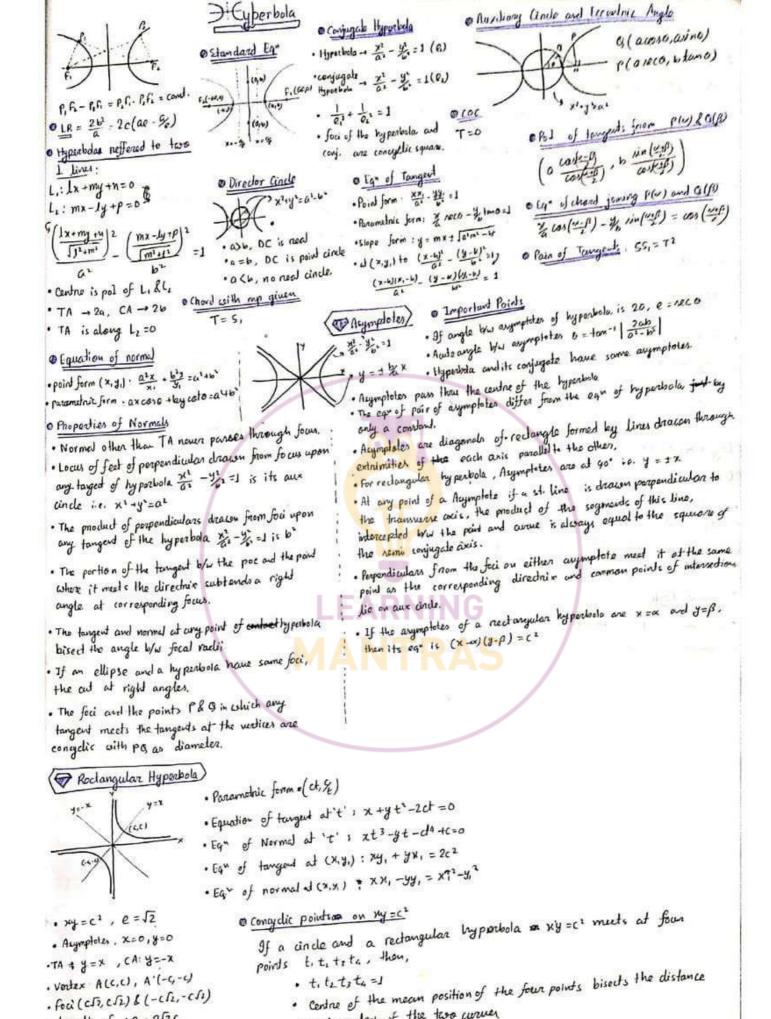
O Sum of all oth roots of writy = 0 O Reductof all roots = 1.0.0 \times ... $\times^{n-1} = \begin{cases} 1 & n \text{ is odd} \\ -1 & n \text{ is onen} \end{cases}$ onth root of unity! $Z = 1^{\frac{1}{n}}$ $\Rightarrow Z = \left(\cos 2k\pi t + i \cos 2k\pi \right)^{n} = 20 \left(\cos \frac{2\pi}{n} + i \sin \frac{2\pi}{n} \right)^{k}$: 0 = cas 21 +i sin 21 OLOCUR of a CN (2, and 2, are fixed, 2 is a variable point) → | = - = | +17 - Te | = | = , - Ze | -> | Z - Z. | = | Z - Z. | → Z lien on perpendialar wisedor of the مردما- $\rightarrow \arg\left(\frac{2-2i}{2-2i}\right) = \pm \frac{\pi}{2} \longrightarrow \arg\left(\frac{2-2i}{2-2i}\right) = \frac{\pi}{2}$ --- | z-z|2+ 12-z,12= |2,-212 -> cinele with z, and ze an dismosten entrimeties. - ang (2-21) of (fixed)



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b/w the centres of the two curves

· foci (csz, csz) & (-csz, -csz)

· length of Le = 252c · Aux circle - n2+42====

Theory of Equations and Logarithm

claws of log

$$\log_{a}(x) = \log_{a}x$$

@ Common Roots

• 2 common
$$\rightarrow \frac{G_1}{G_2} = \frac{G_1}{G_2} = \frac{C_1}{G_2}$$

@ Relation b/w roots and co-eff

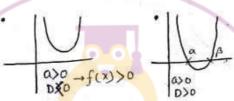
$$0 \cdot \chi^n + a_1 \chi^n + a_2 \chi + a_3 \chi^n + a_4 \chi^n + a_5 \chi^$$

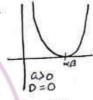
Disociminant & Nature of Roots

Disordinated Nature of Rabis
$$ax^{2} + bx + C = 0 \rightarrow x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

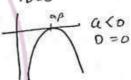
$$D = 0 \rightarrow 1001$$
.
 $D < 0 \rightarrow 1001$ are imaginary.

$$f(x) = y = ax^2 + bx + c$$











Binomial Theorem (x+0) = "C, x"+ "C, x"'a + "C, x"-2a2 + +"Cxx"-ax+-...+"Cn-, x'a"-1+ "C,x"ax

-> General Term: Tr+1 = "Cr x"-rar

 $(x-a)^n = {}^n C_a x^n - {}^n C_i x^{n-1} a + {}^n C_i x^{n-2} a^2 - \dots + (-1)^n {}^n C_n x^{n-r} a^r + \dots + (-1)^n {}^n C_r x^{n-r} a^r$ -+ Gieneral Term: Tr+1 = (-1) * *Cr x "-ra"

@ Hiddle form: (i) (1 +1) th term, if nis even. Ty+1 = "Cry x" a"2

(ii)
$$\left(\frac{n+1}{2}\right)$$
th $\ell\left(\frac{n+3}{2}\right)$ th town, if n is odd.

O Guicodest team
$$\frac{T_{r+1}}{T_r} \geqslant 1$$
 i.e. $\frac{N-r+1}{r} \left| \frac{e}{x} \right| \geqslant 1$

•
$$\sum_{r=0}^{\infty} (-1)^r {}^n C_r = 0$$

• ${}^n C_1 - 2 {}^n C_2 + 3 {}^n C_3 - \dots + n (-1)^{n-1} {}^n C_n = 0$

•
$${}^{n}C_{1}-2C_{2}+3C_{3}$$

• ${}^{n}C_{1}+2{}^{n}C_{2}+3{}^{n}C_{3}+\cdots+n{}^{n}C_{n}=n\cdot 2^{n-1}$

(ii)
$$(\frac{n}{2}+1)$$
th term, if nis even. $1\sqrt{2}+1 = Cr_2 \times Cd$ = $\frac{n}{r} \times Cd$ = $\frac{n+3}{r}$ th $\frac{n+3}{r}$ th term, if nisodd. $\frac{n}{r} = \frac{n}{r} \cdot \frac{n-1}{r-1} \cdot \frac{n-2}{r-1} \cdot \frac{n-2}{r-2} \cdot \frac{n-2}{r-1} \cdot \frac{n-2}{r$

 $\frac{\left(\chi_1 + \chi_2 + \dots + \chi_{\kappa}\right)^2}{\left(\chi_1 + \chi_2 + \dots + \chi_{\kappa}\right)^2} = \sum_{r_1 + r_2 + r_3 + \dots + m} \frac{\eta_1 \chi_1^{r_1} \chi_2^{r_2} \dots \chi_{\kappa}^{r_{\kappa}}}{\left(\chi_1 + \chi_2 + \dots + \chi_{\kappa}\right)^2}$

· no of terms in (x+y+z) " is n+2(2 or (n+1)(n+2)

Expressions

•
$$(1+x)^{-1} = 1 - x + x^2 - 00 - x^3 + \cdots + (-x)^{x} + \cdots$$

$$(1+x)^{-2} = 1-2x + 3x^2 - 4x^3 + \cdots + (r+1)(x)^{r+2}$$

•
$$(1+x)^{-2} = 1-2x + 3x^{2} + 21x^{3} + - \cdots + (r+1)x^{2} + - \cdots = (r+1)x^{2} + \cdots = (r+1)x$$

•
$$(1-x)^{-3} = 1 - 3x + 6x^2 - \cdots + \frac{(r+1)(r+2)}{2!} (-x)^r + \cdots = 0$$

Trigonometric Equation

Or While solving trigo equation, avoid squaring the equation as for as possible. If squaring is necessary check the solution for extransous values (similar values following the same pattern.

 $0 coro = coro \longrightarrow 0 = 2n\pi \pm \infty$, $n \in \mathbb{Z}$ solving the equation.

Extreme values of functions, xeep in mind.

- Solution of the equation of the form acord+brino=C
- -> If ICI>Ja2+6, then no real solution
- → If ICI < Ta2+152, then divide both sides of the equation

by
$$\int a^{2}+b^{2}$$
, then take $\cos \alpha = \frac{a}{\int a^{2}+b^{2}}$,

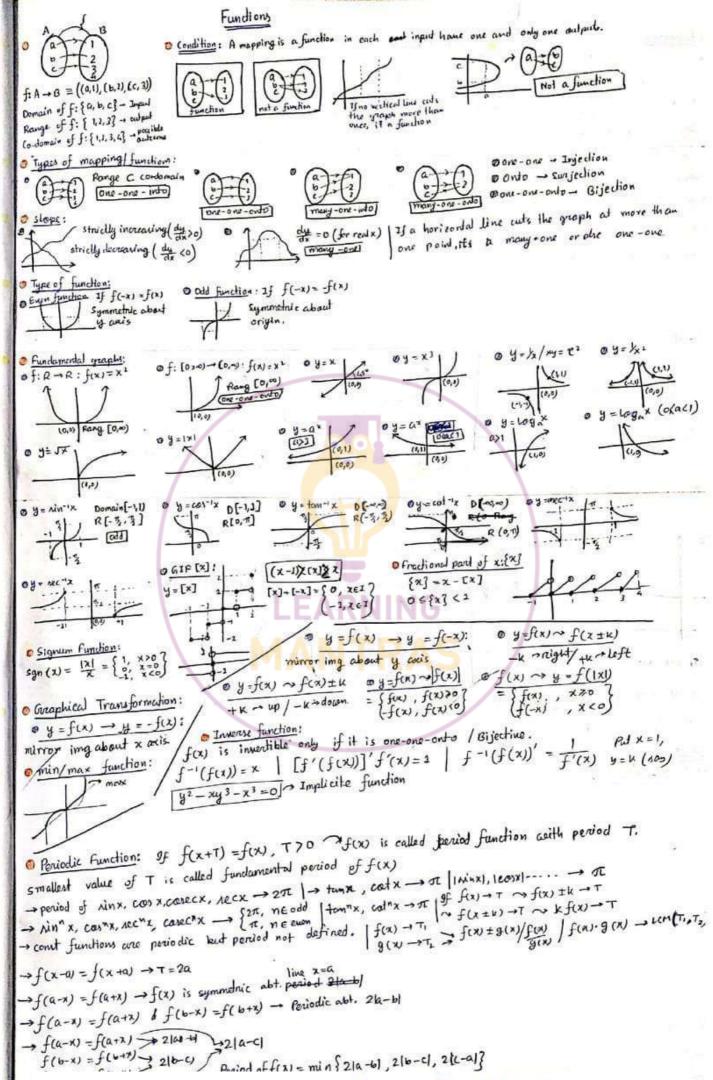
$$Ain \propto = \frac{b}{\sqrt{a^2 + b^2}}$$
, equation will reduce to

$$car(o-a) = car\beta$$
, tohore $tana = \frac{b}{a}$

reduce to
$$Ain(0+\infty) = Ain\beta$$
,

Ain $\beta = \overline{Ia}$

$$\sin \beta = \frac{c}{\sqrt{a^2 + b^2}}$$



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@ Expansions:

 $\alpha \text{ Ain} \chi = \chi - \frac{\chi^3}{3!} + \frac{\chi^5}{5!} - \frac{\chi^7}{7!} + \dots$

0 (a) $x = 1 - \frac{x^1}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \cdots$

0 tanx = x + 33 + = x5

@ log(1+x) = x-왕 +왕-쌀+····

0 log (1-x) = -x - x1 - x1 - x1 - x5 - ...

0 lage = 1+ = + = + = + = + = + = + ...

@ Q1 = 1 + xlng + (xlna)1 + (xlna)3 + ...

1 tan-1x = x - x2 + x5 - x3 + ...

@ nin-1x = x + 23 + 30 x5+....

imits

 $\lim_{x \to 0} \frac{\lambda i n x}{x} = \lim_{x \to 0} \frac{\lambda}{\lambda i n x} = \lim_{x \to 0} \frac{\lambda}{x} = \lim_{x \to 0} \frac{\lambda}{x} = 1$

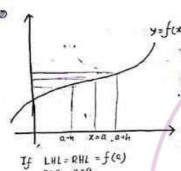
 $0 \lim_{x \to 0} \frac{\lambda i u^{-1} x}{x} = \lim_{x \to 0} \frac{\tan^{-1} x}{x} = 1$

o lim ax-1 = lna

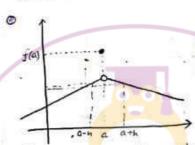
1 lim ln (1+x) =1

 $0 \lim_{x \to a} \frac{x^n - a^n}{x - a} = na^{n-2}$

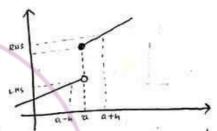
Continuty



 \rightarrow y=f(x) is continuous at x=a



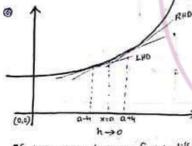
, If LHL = EHL +f(a), Discontinuous at x = a, point discontinuty/Removable discontinuty.



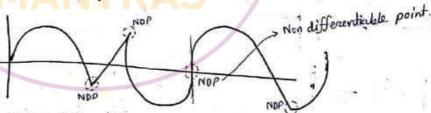
LHL \neq RHL. Discontinuous at x=a. Jump Discontinuity.

Differentiability

- Sharp twons lead to non-differentiable points.
- Smooth curves are generally differentiable at all points.
- @ Tangents must have finite slope to make function differentiable.



If LHD = RHD at x = a, f(x) is differentiable



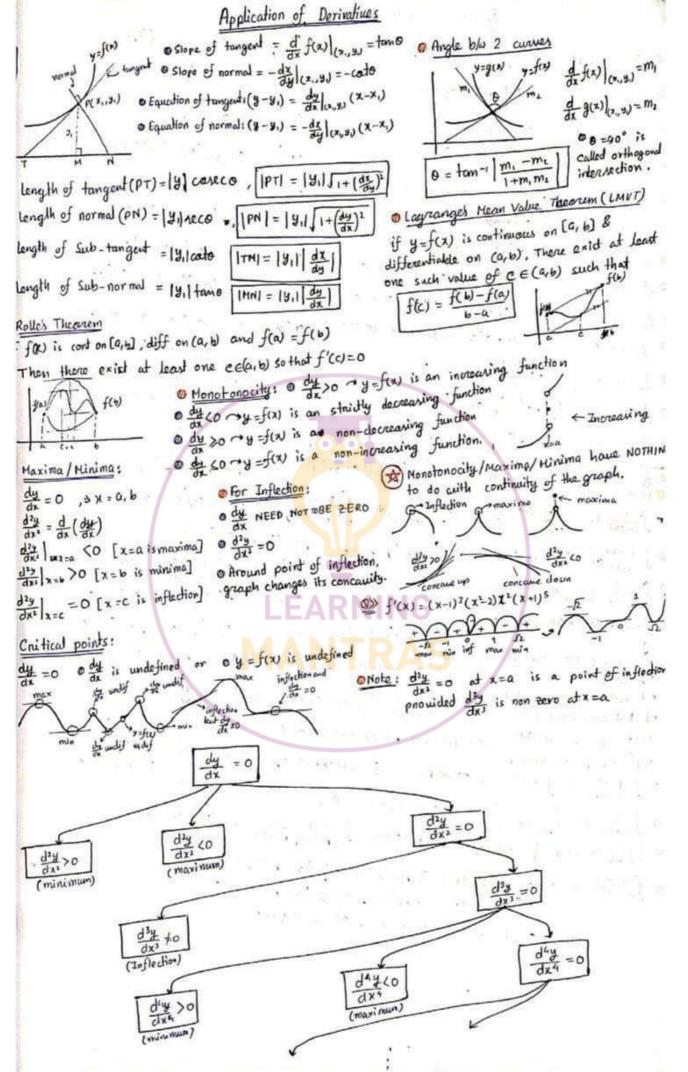
RHD at x=a

$$Rf'(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$$

LHO at x=a Lf'(a) = lim f(a-1)-f(a) @ Discontinuous >> non-differentiable

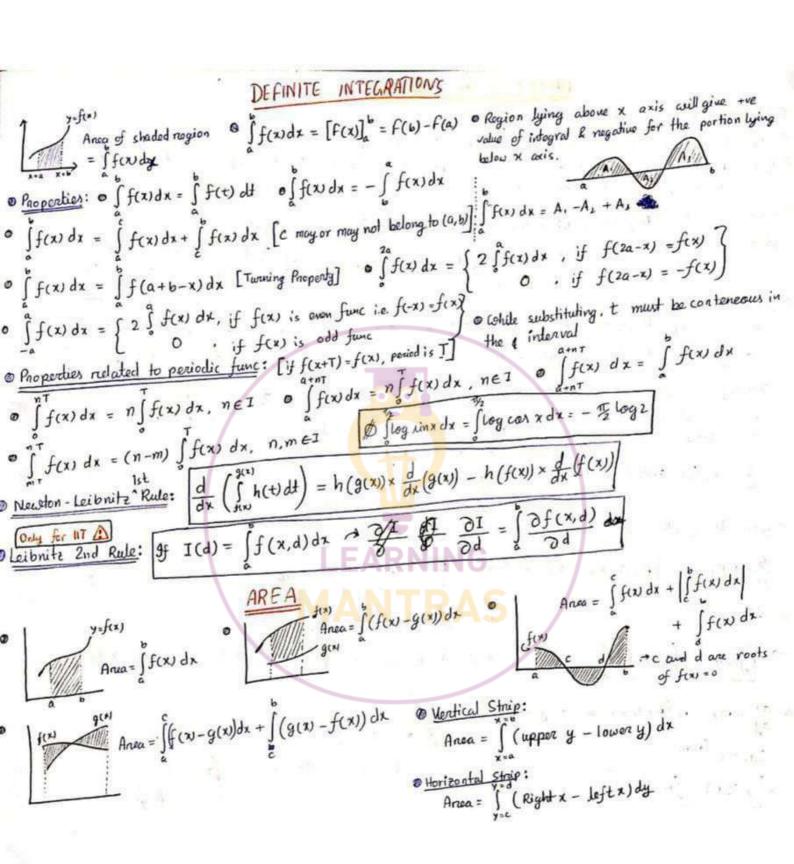
O Differentiable > continuous.

. $f(x) \rightarrow diff$ $\rightarrow f'(x) \rightarrow cont / f''(x) \rightarrow cont / f'(x) \rightarrow diff$



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Indefinite antique O Total dx - Am e Jair dx = 1 tam 1 (76) te * d x" = 11x" - - " [x" dx - x"] +c e ∫ 1 | dx = d nec -1 (%) +c & d logx = 1 - 1 dx = logx 10 0 J 1 apr 1 log (x-a) +c od ex sex - Serdx sex o d ax = ax lna Sards - ax 10 oflow dx = log | nece | +c o d ainx = cosx - fearx dx = ainx +c of colx dx = log [ninx] + C of carx - - rink - finlegral frink dx - - consec or Sheexdx = Log | necx +tem x 1+C of tank - recix - lace x dx - lemx 10 .. = log |tam (3/43) |+c od catx = -carec'x - Scarecix dx = - codx +c od Accx = secx tonx - frecx lebix dx = secx +c o scarcexdx = log conecx -cotx +c o de concx = - con x cala - Scorex colx dx = concx 10 = log | tam 3/ +c e $\frac{d}{dx}$ $Ain^{-1}x = \frac{1}{\sqrt{1-x^2}} \rightarrow \int \frac{1}{\sqrt{1-x}} dx = Ain^{-1}x + c$ consciences comes finitis the Ist MATE Junction 1 is by pards o d ton-1x = 1 -1x dx = ton-1x 1c Tinge Myelmic @ dx Acc-1x = 1 - 1 x/x2-1 dx = Acc-1x1c OBy Ruls: SI-II dx = I SIdx - S((\$x 1) (SI dx) dx = Sex(Sim)+5'(x)) = ex fin)+c of I linear dx = log [linear] ac of [linear] adx = (linear) at - c of log x dx = x log x-x+c $\oint \int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C \quad o \int (f(x))^n f'(x) dx = \frac{\left(\int (x)\right)^{n+1}}{(n+2)} + C \quad \text{Guad}$ $\oint \int \frac{1}{a \sin x + b \cos x} dx \rightarrow \text{put } \sin x = \frac{2 \tan^{\frac{n}{2}}}{1 + \tan^{\frac{n}{2}} x}, \cos x = \frac{1 - \tan^{\frac{n}{2}} x}{1 + \tan^{\frac{n}{2}} x} \quad \text{of } dx$ · Jak = 1 tom -1 (%) · [dx = 1 ln | x-a | +c O Sain x cos x dx (m, nen) , o J dx , Jathain'x , Jathain'x July dx = 1 in | a+x | +e · 9f m,n c odd, subs adamy Janinx + bears), Jan printx + com divide Nr & Dr ley comx . If one is odd, sub our · If both are even, use trigo o ∫ Pcasx + gainx +r dx ~ wR, Nr = 2 (Dr) + μ(dDr) + δ ·95 both are rational and o Biquadratic - sub (x+从) or (x-从)=七 m+n-2 is -ve int. then @ Spx+4. dx. Spx+a dx > w8 px+9 = dx (ax1+bx+c)+je @ Slinear Jauad > L= m(B)'+n O States dx, Stock, Stock dx → sub L, =t2 O Stock → sub = L © ∫ \$\frac{1}{6,16}, dx \rangle \chi = \frac{1}{4} \rangle Integrand will become \$\frac{1}{(p+1+4)(r+1+1)} \rangle \tau \tau = rt'+5 Ø SJ Quad dx → · SJa2+x3 dx = 2 Ja2+x3 + 42 ln | x+Ja2+x2 +c · (1x2-a2dx = 3/x2-a2 - a2 lu |x+ 1x1-a1+c · (Jai-x2 dx = 2 Jai-x2 + 9 min-1 (2)+c



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DIFFERENTIAL EGUATION DE represents a family of curves. · Eq involving x, y d differentials co-efficient. Order: Order of highest order derivative present in the egm is the order of D.E. Dogree: Degree of the highest order derivative present in the equ is the degree of DE, provided the eq" is polynomial in different co-eff and eq" is free from radicals. * Formation of DE: (Dograe of a DE = No of arbitrary constants present in eqn) (1) DE of all lines pursing throw origin: y = mx + c $y = dy = \sqrt{x} dy - y dx = 0$ dy = m dy = m dy = m dy = m $\frac{dy}{dx} = m$, $\frac{d^2y}{dx^2} = 0$ De Solution of DE: Ovariable - seperable form: dx = ex + x 2 ex - @ Eqn Roducible to Variable Separable form dy = f(ax + by +c), comider, ax+by+c = t = dy = ex+x2 = ferdy = f(2 +x1)dz Homogeneous Form: $\frac{dy}{dx} = \frac{f(x,y)}{g(x,y)}$ where f and g are order. ·[9f aB = Ab or A+b =0] x= X+ h y= Y+k $\frac{dy}{dx} = \frac{ax + by + ah + bk + c}{Ax + By + Ah + Bk + D}$ $\frac{dh + bk + c}{Ah + Bk + D}$ $\frac{dh + bk + c}{Ah + Bk + D}$ $\frac{dh + bk + c}{Ah + Bk + D}$ dy = h(次) assume 炎=t · Linear Differential Gan: $\frac{dY}{dx} = \frac{ax + bY}{Ax + BY} \rightarrow Homogeneous \rightarrow In the end, X = x-h$ Y = y - k $\Rightarrow \frac{dy}{dx} + Py = Q$ [P&Q one force of x alone] I.F = e SPdx · 9f aB = Ab - (ax + by = t) $\Rightarrow \left[y(1.f) = \int (Q(1.f)) dx\right]$ · If A+b=0 - simply cross multiply & neplace xdy +ydx by ⇒ dx +Mx =N [H&N are func of y alone] Barnoalli Egn $\frac{dy}{dx} \cdot + \frac{y}{x} = y^n$ I.F. = e [Hdy divide by you and then assume \$ 100 eff of x as &

 $\rightarrow \chi(J.F.) = \int (N(J.F)) dy$

here, t = 8 1 4n-1

